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Saint-Petersburg State University

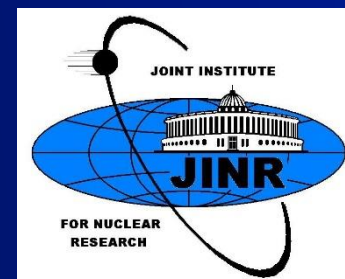
# Determination of classes of events in multiplicity and its relevance to centrality in high energy Pb-Pb and p-Pb collisions in different MC models

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on High Energy Physics Problems**

*"Relativistic Nuclear Physics and Quantum Chromodynamics",*

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## Motivation:

# Centrality and Fluctuation

- **Fluctuations** in physical observables in heavy-ion collisions have been a topic of interest for some years as they may provide **important signals** regarding the formation of **quark-gluon plasma** (QGP)
- For **studying fluctuation** and searching delicate effect it is necessary to determine precisely measurement's parameters (**to fix the centrality classes**) when the induced observable's fluctuation will be minimal.

The relative fluctuation  $\omega_x$  in an observable  $x$



$$\omega_x = \frac{\sigma_x^2}{\langle x \rangle}$$

$$\sigma_x^2$$

- dispersion

$$\langle x \rangle$$

- the mean value

Nucleus is an extended object

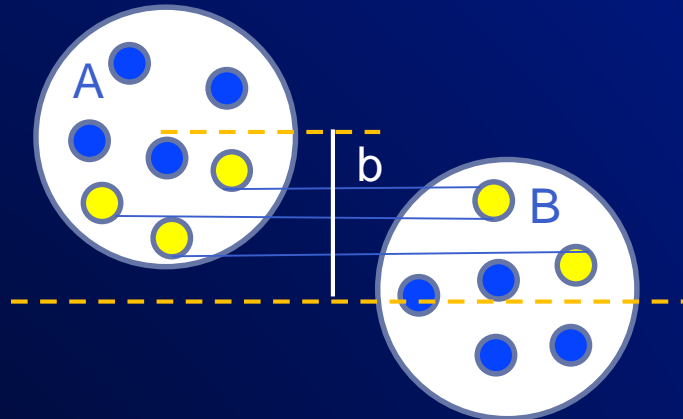


Collisions with nuclei could be characterized by centrality with respect to impact parameter.

# Nucleus-nucleus collision experiment

• Opposite bunches particle scattering

• Fix nucleus-target collision



- $N_B = B - N_{col}^R$
- $N_A = A - N_{col}^L$

- $N_A = A - N_{col}^L$

- $N_{col}^L = \frac{E_{col}^L}{E_0}$

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- $N_{col}^R = \frac{E_{col}^R}{E_0}$

- - Number of wounded nucleons

- - Number of nucleons-spectators

- $E_{col}^L (E_{col}^R)$  - Total Energy of collision fixed by calorimeters

**ALICE**

(LHC)

$E_0$  - Energy of a nucleon

**NA61**

(SPS)

2 methods of fixing centrality:

Multiplicity

Nucleon-spectators



## Aim of the analysis :

- Minimization of trivial fluctuations of observables
- Applicability of the centrality determination methods for **pA** collisions

## Analysis:

Influence of the centrality classes width on the fluctuations of **Number of participants**

## Method:

Monte-Carlo simulation of nucleus-nucleus collision

**Why we use Monte-Carlo (Glauber model; HIJING)?**

Information about

$b$  – Impact Parameter

$N_{part}$  – Number of wounded nucleons



Distinctions for different classes of centrality are evident

# What is the CENTRALITY?

$$\int_x^{x_{max}} dz y(z) = F(x)$$

If  $y(x)$  is a function of events distribution versus of impact parameter of AA collision.

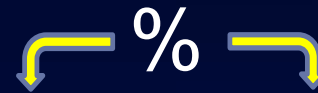
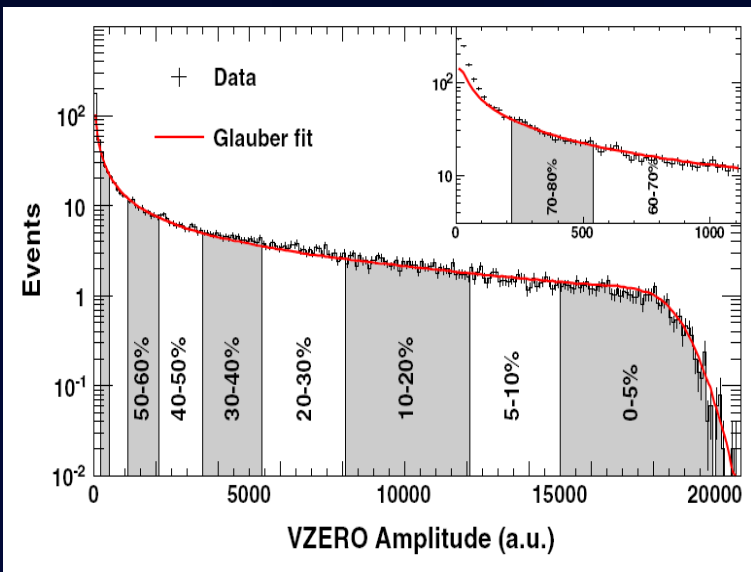
Then  $F(x)$  – square under the plot

Peak value  $F(x) = F(0)$

normalization  $F(x)$  :

$$G(x) = \frac{F(x)}{F(0)}$$

Example:  
Centrality classes in ALICE experiment



**For Impact Parameter**

$$G(0) = 0\%$$

$$G(x_{max}) = 100\%$$

**For Multiplicity**

$$G(0) = 100\%$$

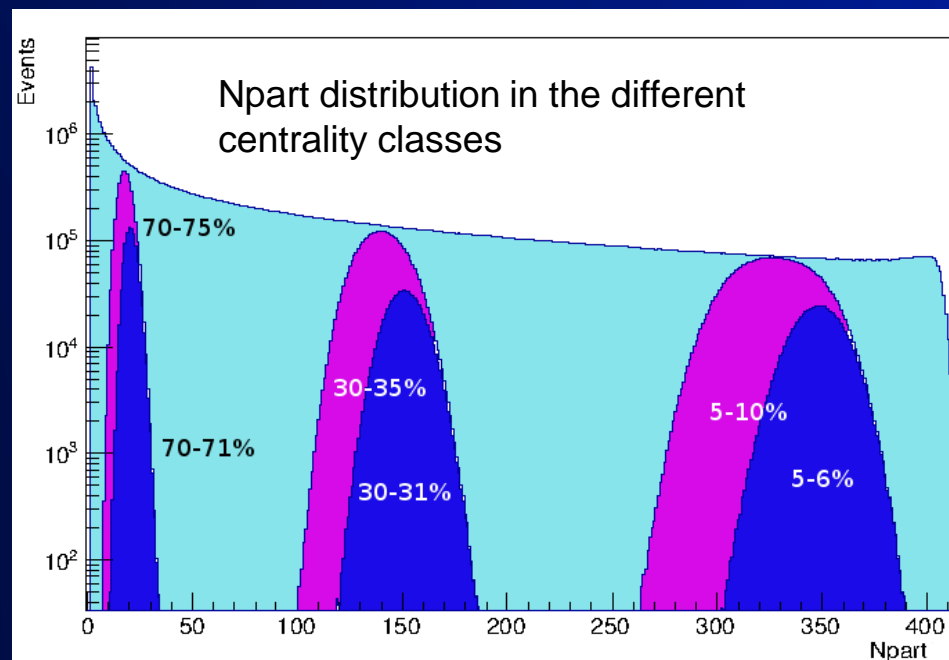
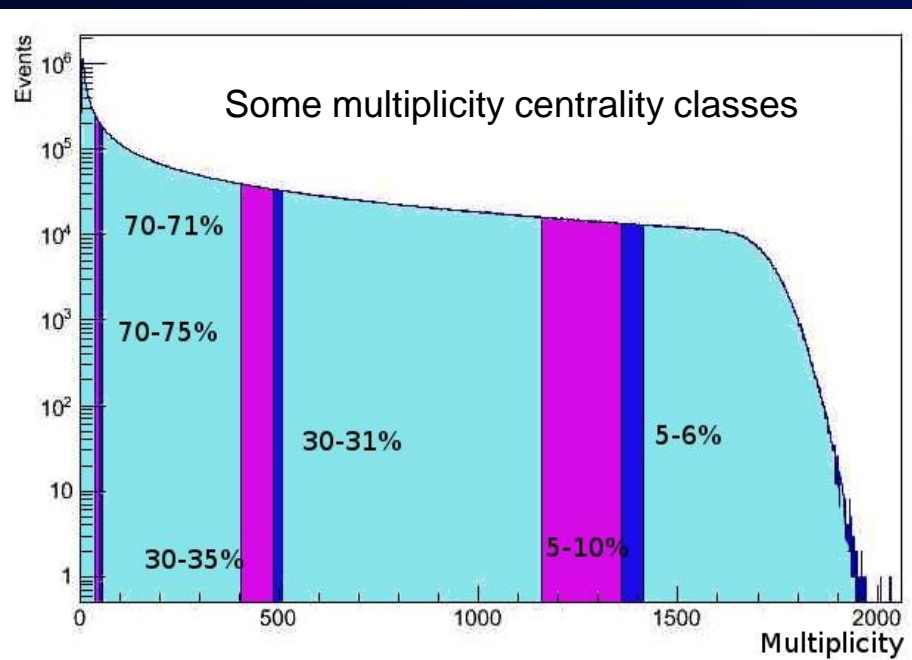
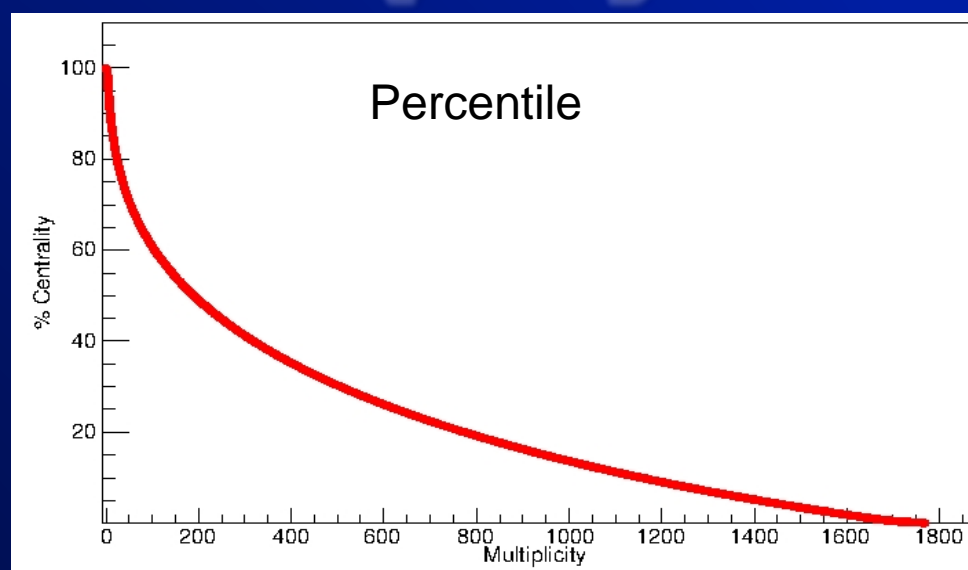
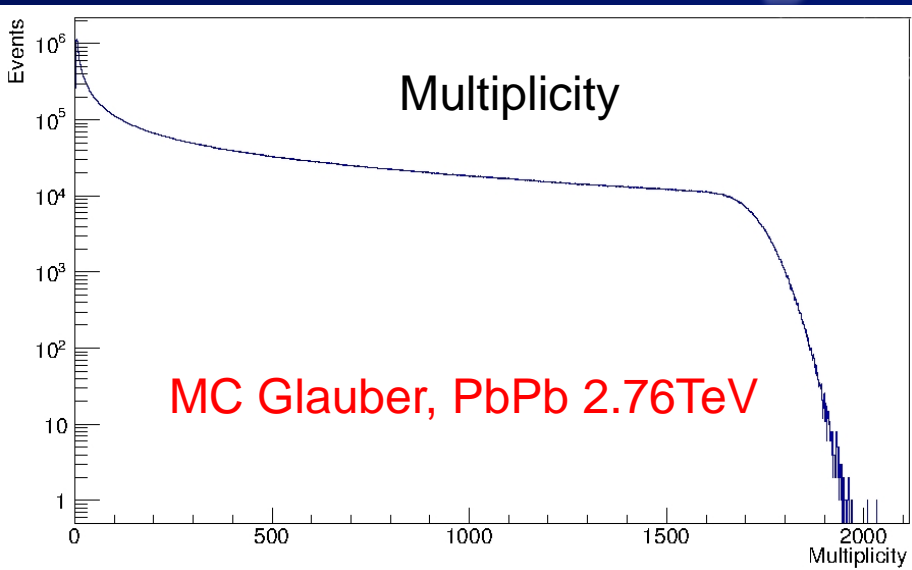
$$G(x_{max}) = 0\%$$

$G(x)$  - function compares value of centrality of the collisions (expressed in percentage) to value of the impact parameter.

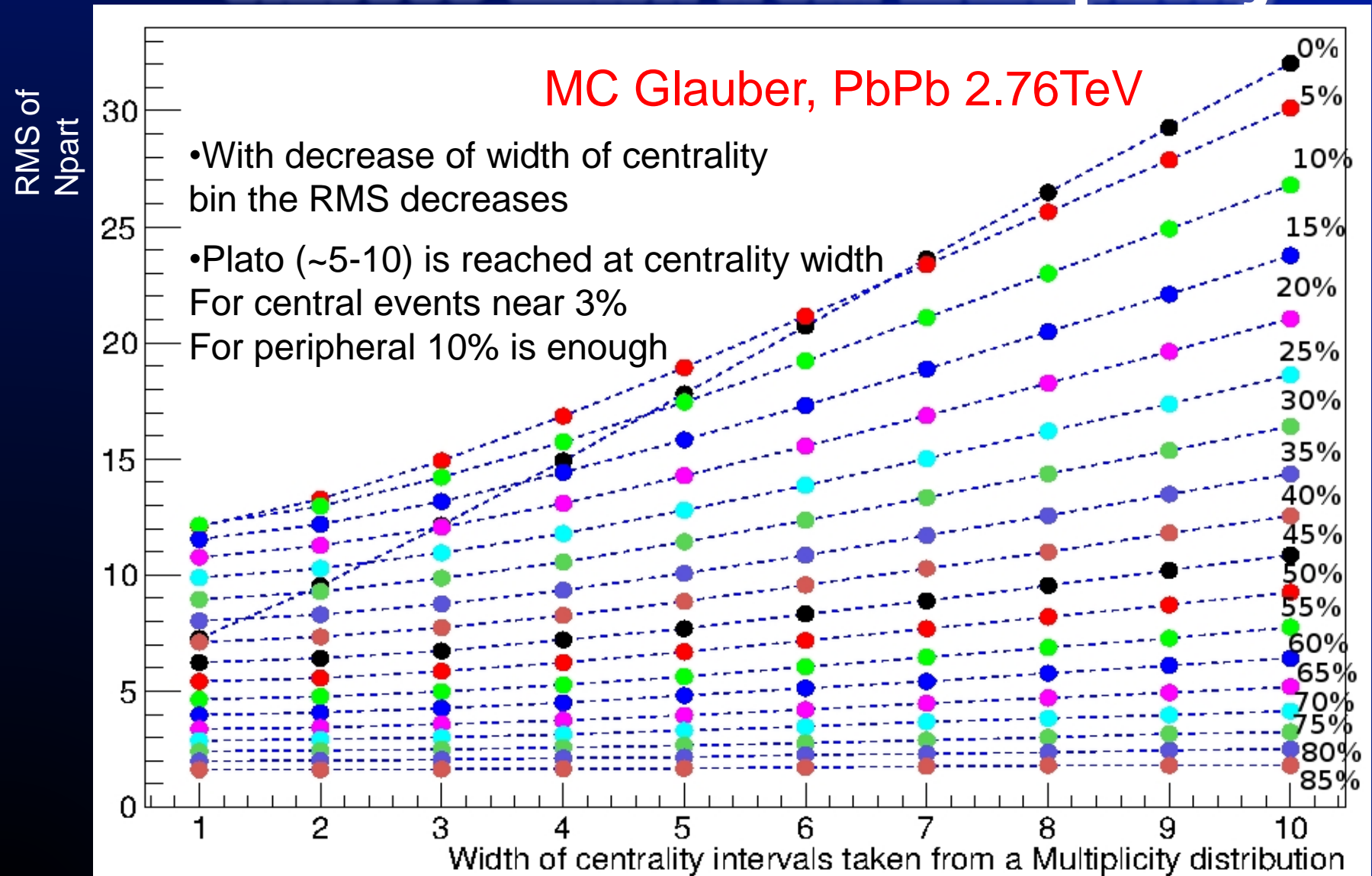
- Borders of intervals of the centrality are equal
- to values of function  $G(x)$  in the points limiting
- the given interval.

Centrality in **Pb-Pb** collisions  
at 2.76 TeV  
based on Glauber Model

# Centrality from multiplicity



# RMS N part in the different centrality classes taken from Multiplicity



\* See details in T.Drozhdzova poster report ISSP 2014



Centrality in **p-Pb** collisions  
at 5.02 TeV

**HIJING 1.38**

# HIJING [1]

- It was based on a two-component geometrical model of minijet production and soft interaction.
- It has incorporated nuclear effects such as nuclear modification of the parton distribution functions (**gluon shadowing**)

## Gluon shadowing [2]

- Without shadowing nucleons interaction will be **independent**
- There are differences between nuclear and proton PDF (parton distribution function) (observed in experiments).
- This leads to **decrease of nucleon-nucleon cross section** at low  $x$ .
- Similar effect is also present in **Models with energy conservation** in elementary nucleon-nucleon collisions (see refs [3-5])

[1] HIJING: A Monte Carlo model for multiple jet production in p p, p A and A A collisions, Xin-Nian Wang and Miklos Gyulassy, Phys.Rev.D 44, 3501 (1991)

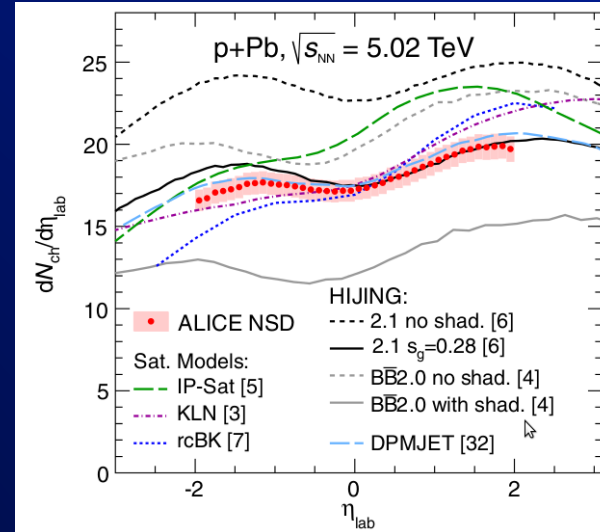
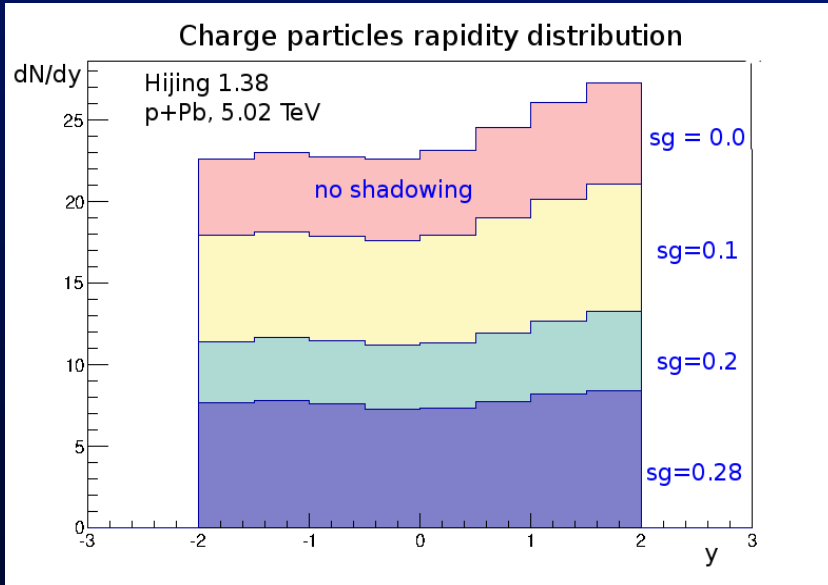
[2] J. Jalilian-Marian arXiv:hep-ph/9909507

[3] G. Feofilov, A. Ivanov, Number of nucleon-nucleon collisions vs energy in modified Glauber calculations // Journal of Physics G CS, 5, (2005) 230-237

[4] Irais Bautista, Carlos Pajares, Jose Guilherme Milhano, Jorge Dias de Deus. Phys. Rev. C 86 (2012) 034909.

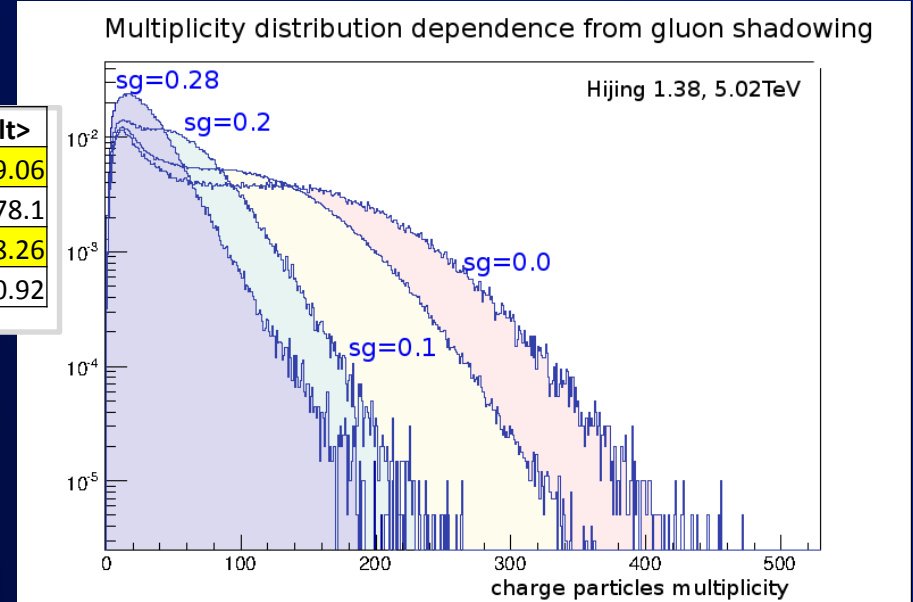
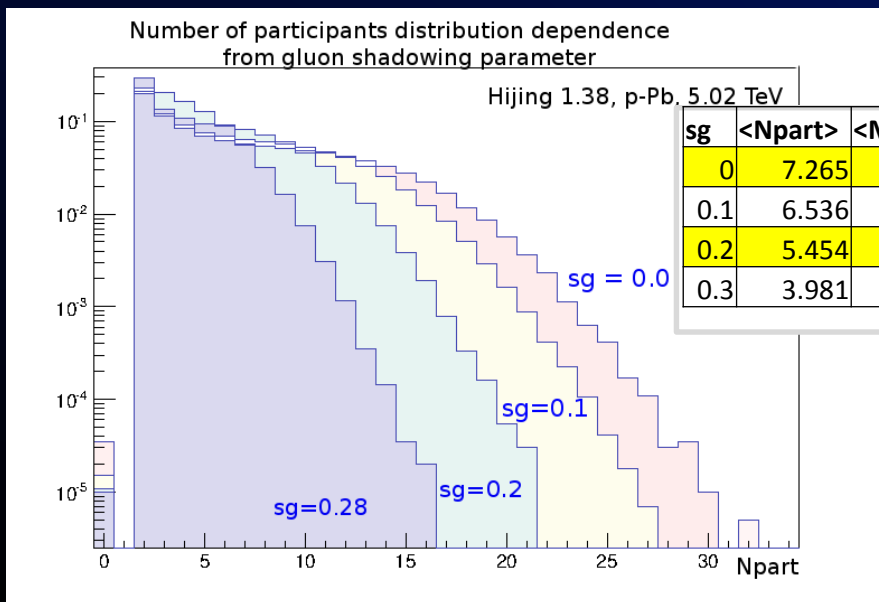
[5] V. Kovalenko, Phys. Atom. Nucl. 76, 1189 (2013), arXiv:1211.6209 [hep-ph]; arXiv:1308.1932 [hep-ph], 2013; V. Kovalenko, V. Vechernin. PoS(BaldinISHEPP XXI) 077, 2012, arXiv:1212.2590 [nucl-th]

# Dependence on a shadowing parameter

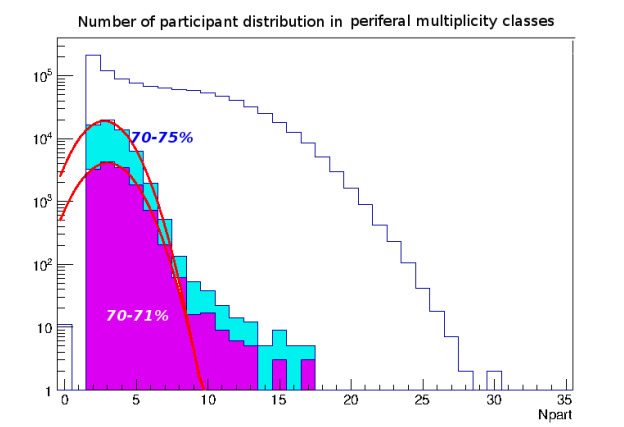
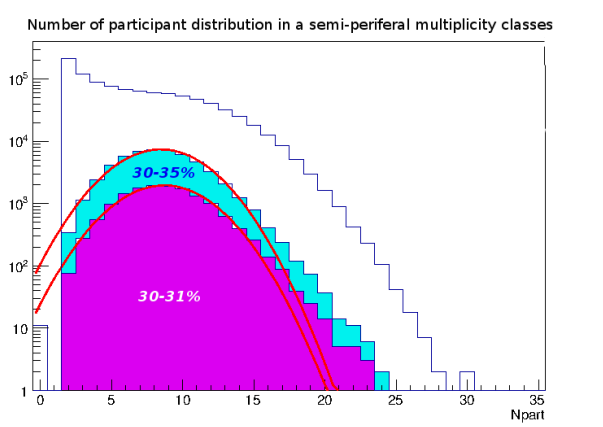
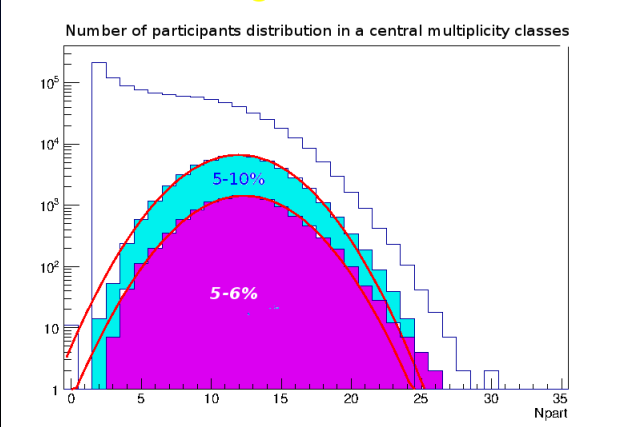
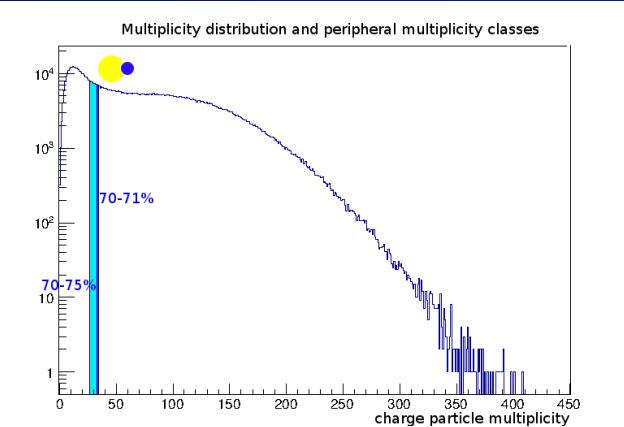
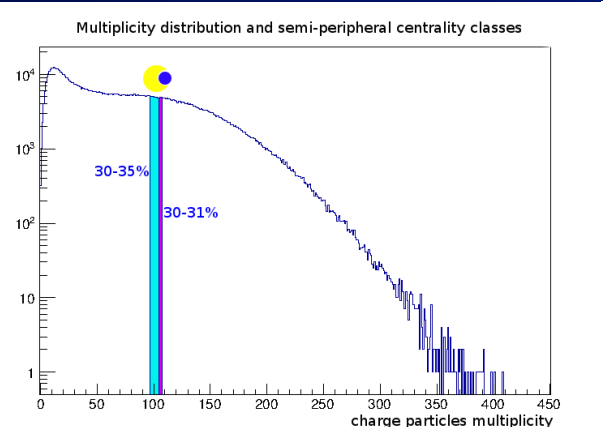
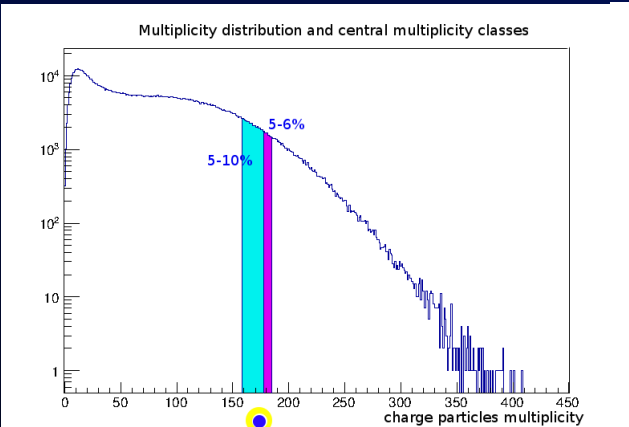
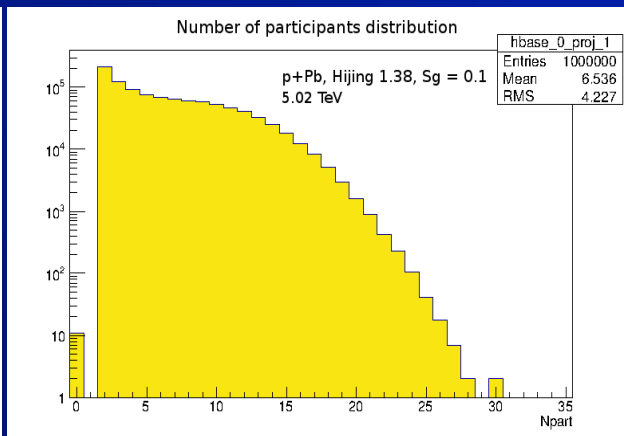
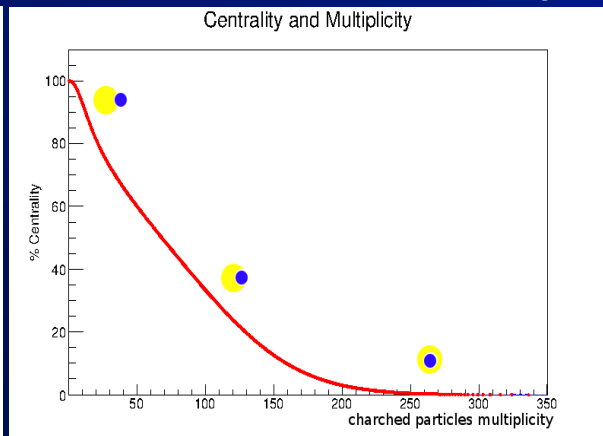
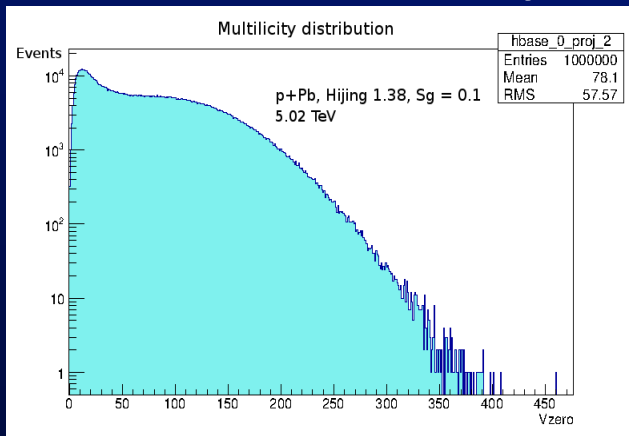


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Experimental data is better described by **HIJING with shadowing**

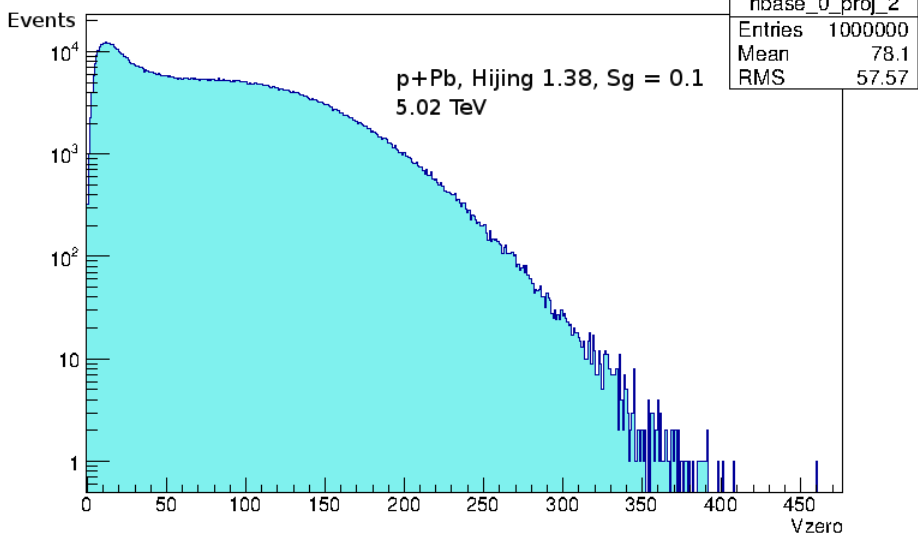


# Centrality from Multiplicity in p-Pb

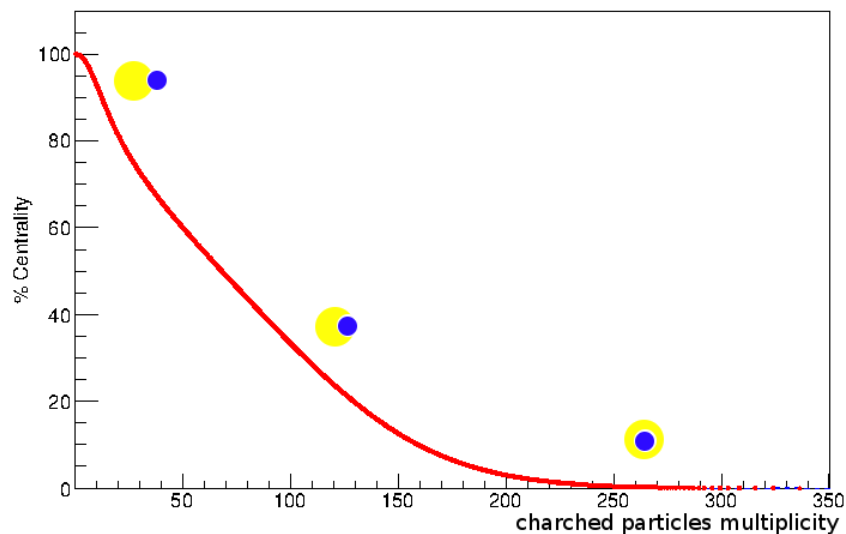


# Centrality from Multiplicity in p-Pb

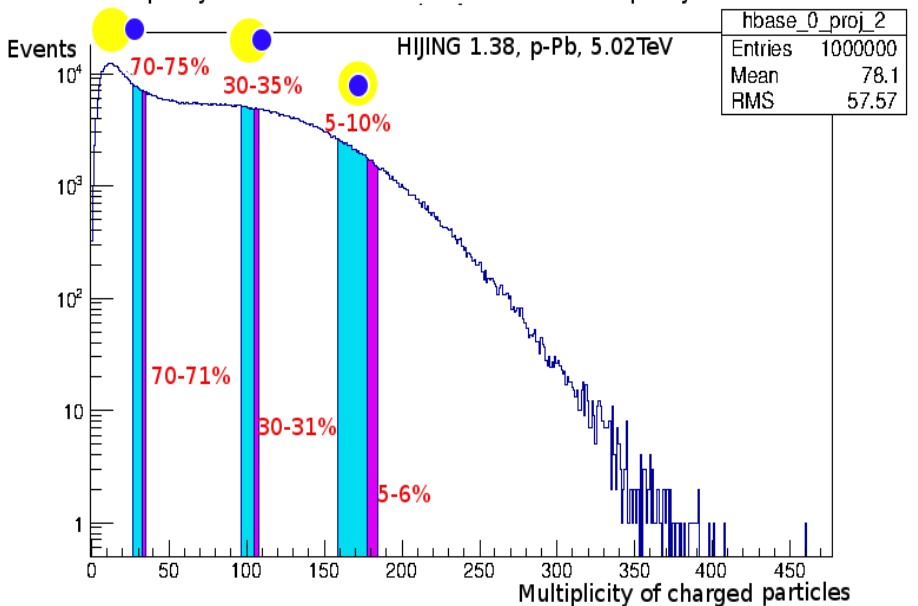
Multiplicity distribution



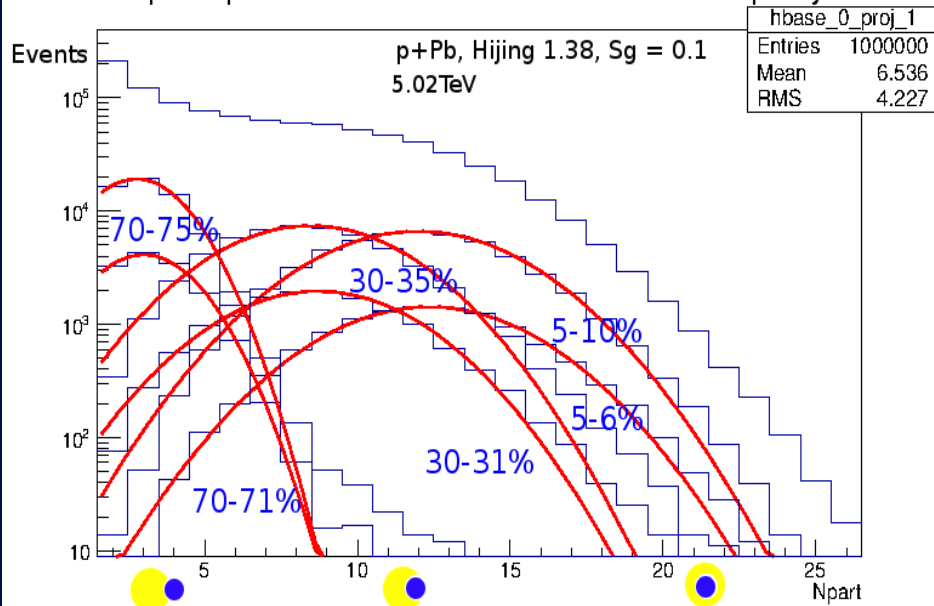
Centrality and Multiplicity



Multiplicity distribution and different width of multiplicity classes

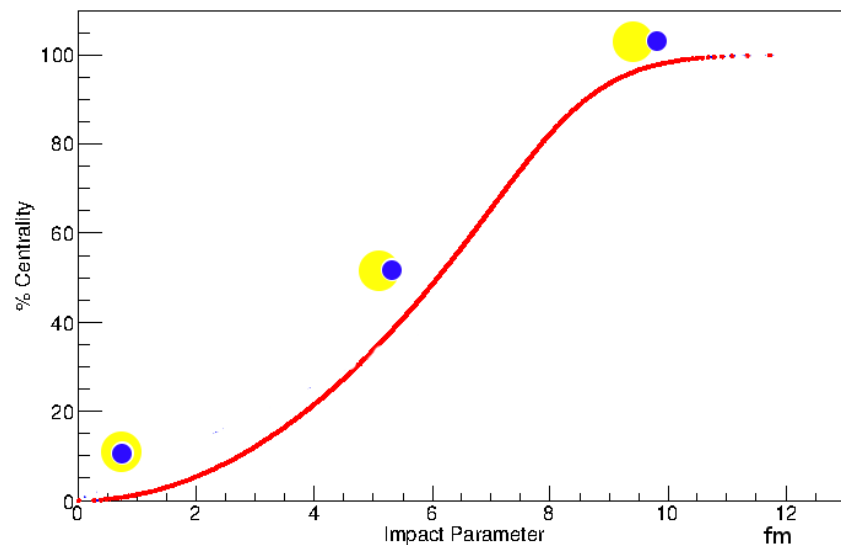


Number of participants distribution in a different width multiplicity classes

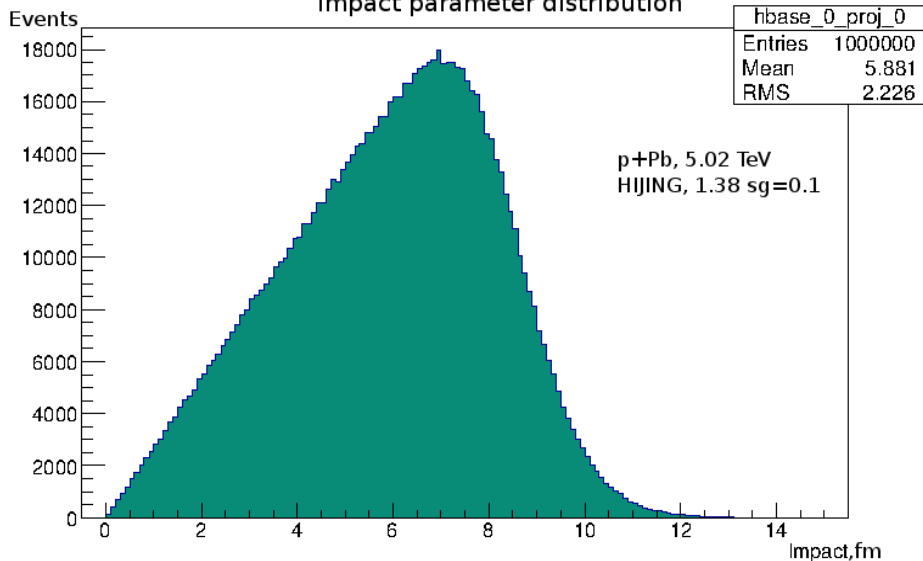


# Centrality from impact parameter p-Pb

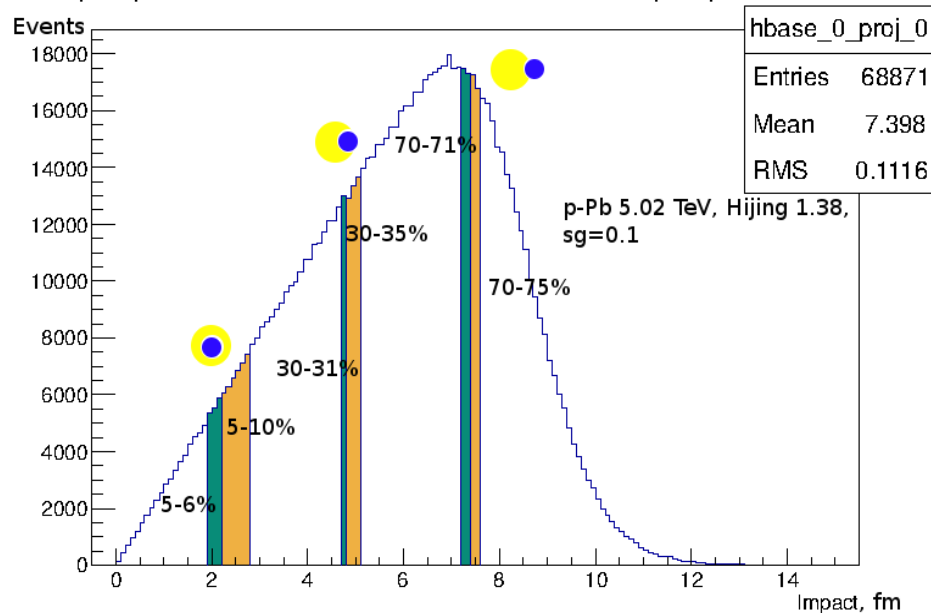
## Centrality and Impact Parameter



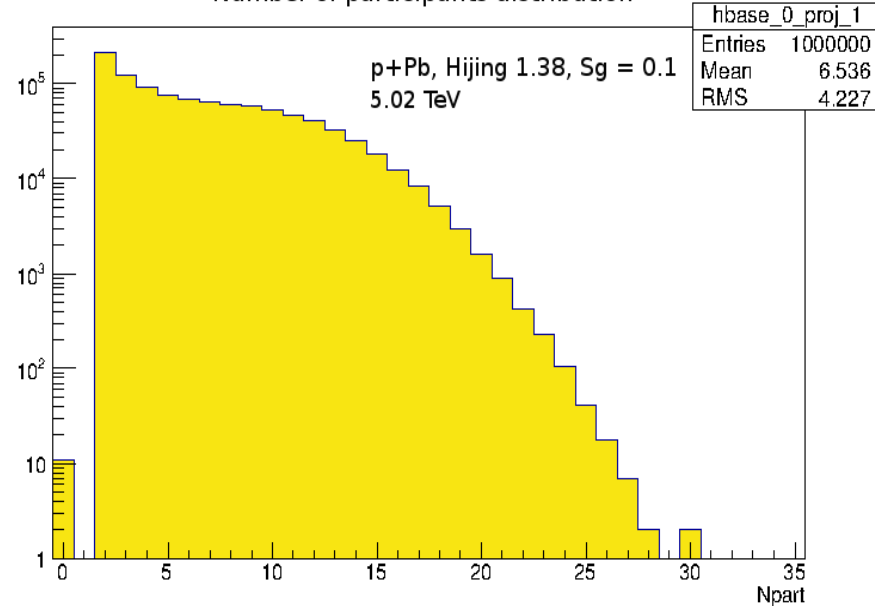
## Impact parameter distribution



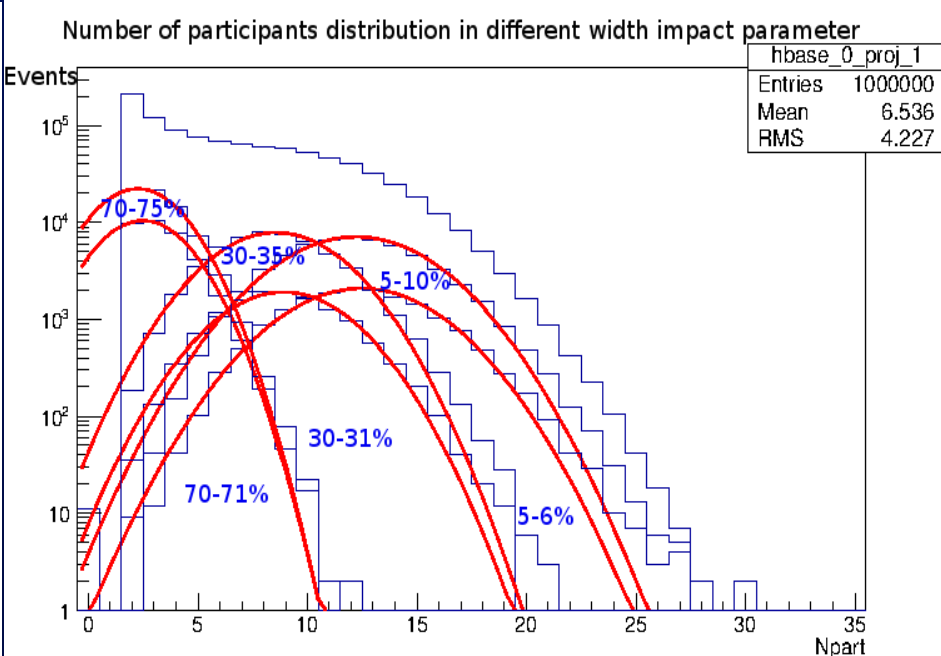
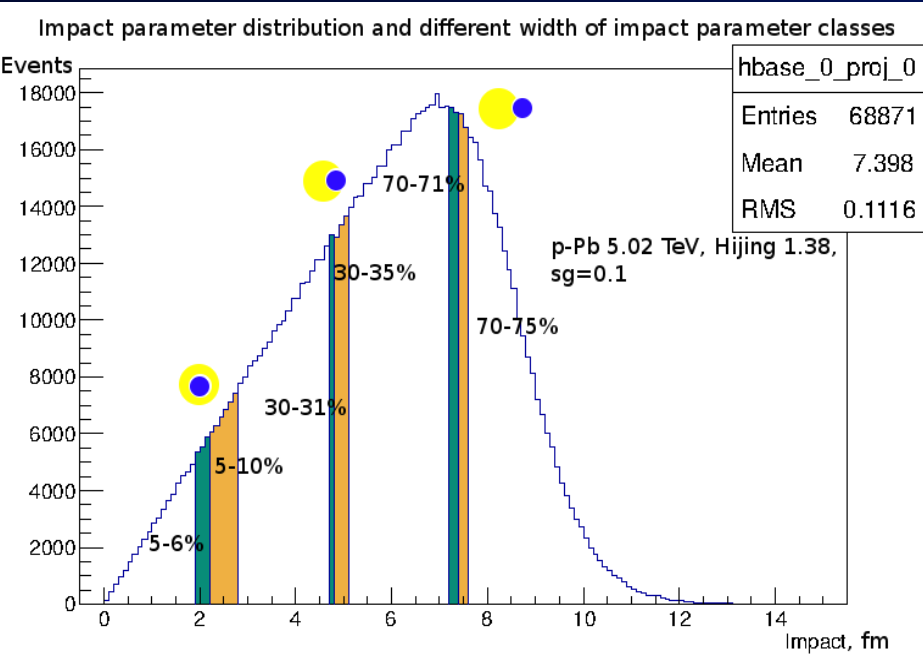
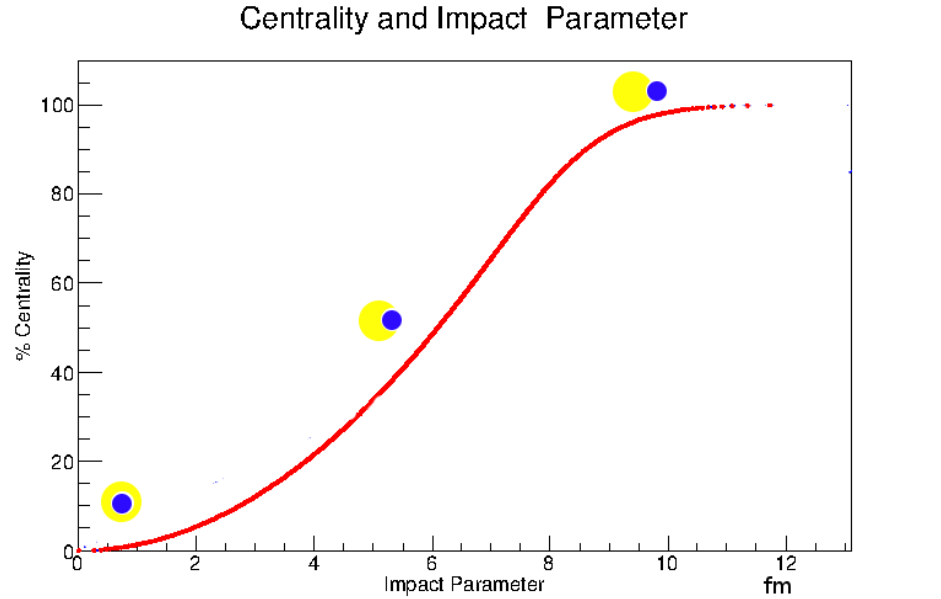
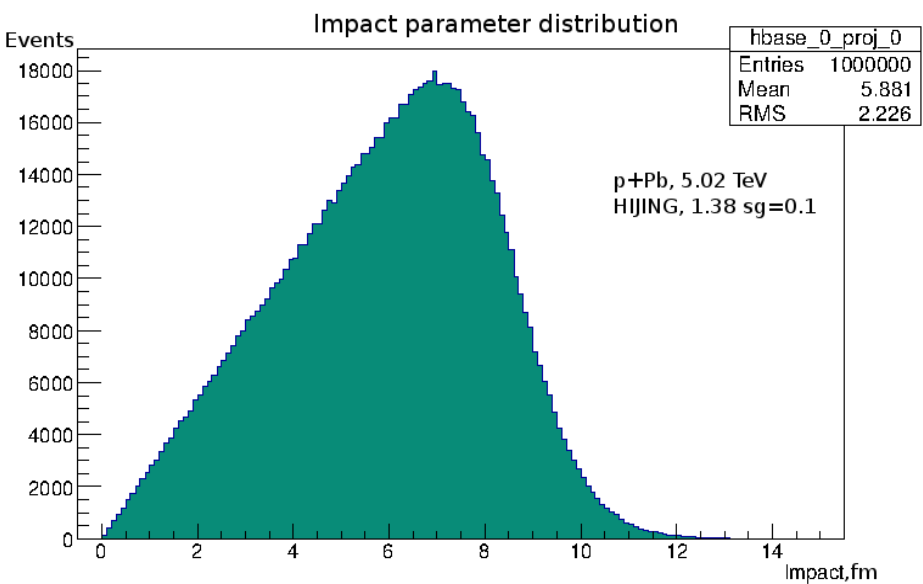
## Impact parameter distribution and different width of impact parameter classes



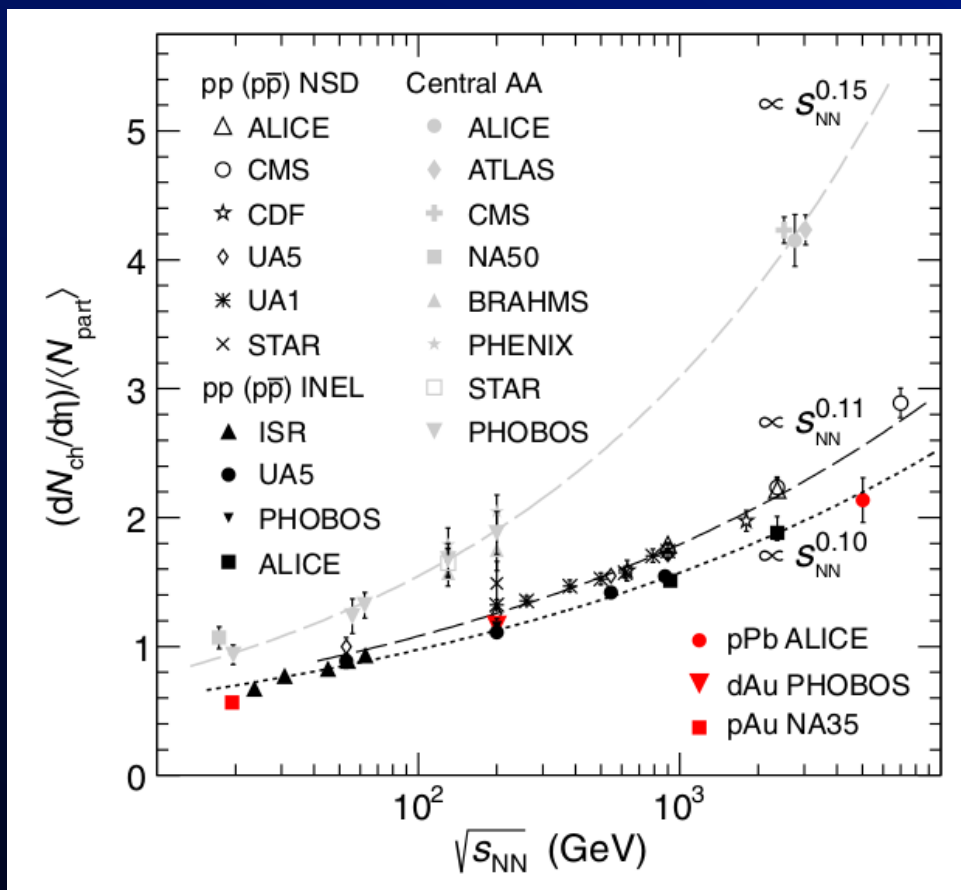
## Number of participants distribution



# Centrality from impact parameter p-Pb



# Normalization of Multiplicity yields



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$$\langle N_{part} \rangle = 7.9 \pm 0.6$$

From Glauber model

Sg	$\langle N_{part} \rangle$	$\langle Mult \rangle$
0	7.265	99.06
0.1	6.536	78.1
0.2	5.454	48.26
0.28	3.981	30.92

HIJING 1.38

Number of participants is depended on models



No straight forward treatment of experimental data on multiplicity, based on normalization to  $N_{part}$

\* See details in T. Drozhzhova, G. Feofilov, V. Kovalenko, A. Seryakov. PoS (QFTHEP 2013) 053, 2013



# Summary and Conclusions:

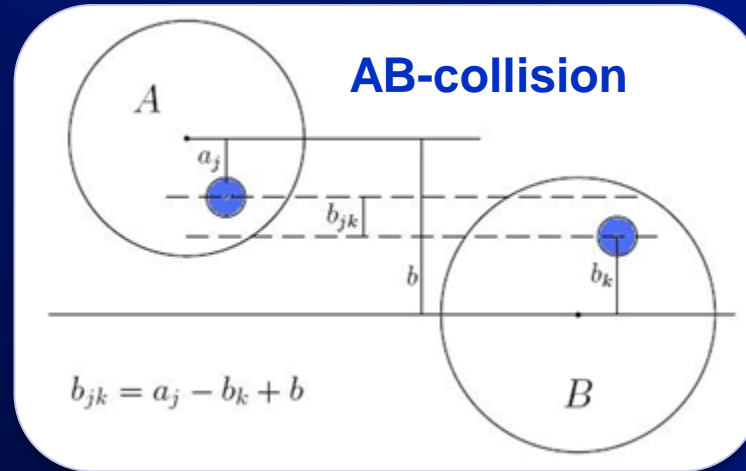
- The method of centrality evaluation initially developed for ion-ion collisions was applied for p+Pb
- Large fluctuations of number of participants in multiplicity classes make dividing of the events in classes according to  $N_{part}$  problematically
- Model dependence of  $N_{part}$  makes questionable normalization of multiplicity yields to  $N_{part}$

- Back-up slides

# MC Glauber model

Pb-Pb

$$\sqrt{s_{NN}} = 2.76 \text{ TeV}$$



- Nucleons are meant as black disks here

Nuclear density

Woods-Saxon distribution:

$$\rho(r) = \rho_0 \left\{ 1 + \exp\left(\frac{r - R_A}{a}\right) \right\}^{-1}$$

where:  $R_A = R_0 \cdot A^{\frac{1}{3}}$  - nuclear radius,  
 $R_0 = 1.07 \text{ fm}$   
 $a = 0.545 \text{ fm}$

# Multiplicity in Glauber model

Poisson distribution of multiplicity in one event

$M_c$  - multiplicity in one event  
 $N_{str}$  - number of quark-gluon stings

$$P(M_c) = e^{-\rho} \frac{\rho^{M_c}}{M_c!}$$

$$\langle M_c \rangle = \rho,$$

$$\rho = m_f \cdot N_{str}(\beta)$$

$m_f$  - multiplicity from one string

$\Delta y$  - rapidity window

$$m_f = \Delta y \cdot \omega$$

Particle multiplicity is proportional to number of produced strings, which is proportional to participants' number  $N_{AB}(\beta)$  and collisions' number  $N_c(\beta)$

$$N_{str}(\beta) = x N_{str}^{NN} N_c(\beta) + (1 - x) N_{AB}(\beta)$$

$$N_{str}^{NN} = 2.56 - 0.478 \ln E + 0.084 (\ln E)^2$$

$$x \in [0, 1]$$

$N_{str}^{NN}$  - number of strings in nucleon-nucleon collision (pp)

$E$  - energy per colliding nucleon pair, GeV