

POSSIBLE DEVELOPMENT of CUMULATIVE PARTICLE EXPERIMENTS



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V.P. Filinova***

Short History



1957 **Leksin G A,**
Azhgirey L S et al

Blokhintsev D I

$P, T=660 \text{ MeV}$
 $P+d \rightarrow p$ in backward
direction,
 $P+He \rightarrow d$

Short-range few-nucleon
correlation flukton

1971 **Baldin A M**
1974 **Stavinskiy V S**

Cumulative effect, quark
structure

1974 - ...

Burov V V, Lukianov V K, Titov A I

Efremov A V

Baldin A A

...

Short-range few-nucleon Frankfurt L L, Strikman M I

correlation



**Direct
measurement of
momentum-
space wave
function squared**

$$\begin{aligned}d^3\sigma/d^3p &\simeq c\sigma_{tot}\psi^2_D(p) \\ E_p d^3\sigma/d^3p &\simeq c\sigma_{tot}E_p\psi^2_D(p) \simeq \\ c\sigma_{tot}\psi^2_{l.c.}\end{aligned}$$

**Cross- section describes knockout of n from d.
Spectator p rushes into detector with speed it
had in d before collision**

Experimental verification

2-nucleon correlation:

Spectrometer EVA

A.Tang et al Phys. Rev. Lett. 90, 042301(2003)

2- and 3-nucleon correlation:

CLAS Collaboration

***K.S. Egiyan et al Phys. Rev. Lett. 96,
082501(2006)***



Formation of quark bag

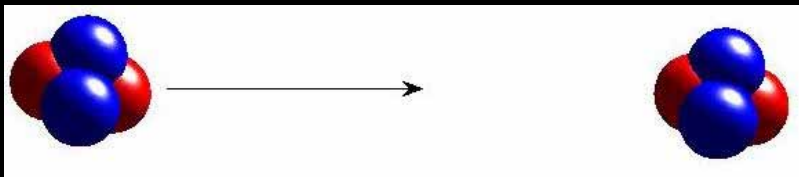


1. Pre-existent quark bag

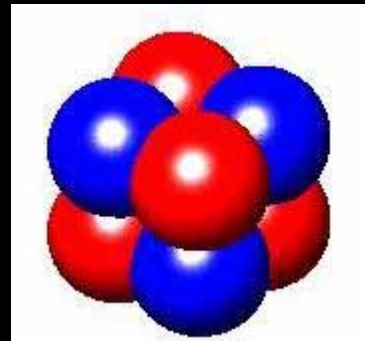
***2. Chiral phase transition
in few-nucleon
systems:***

SRC \rightarrow multibaryon

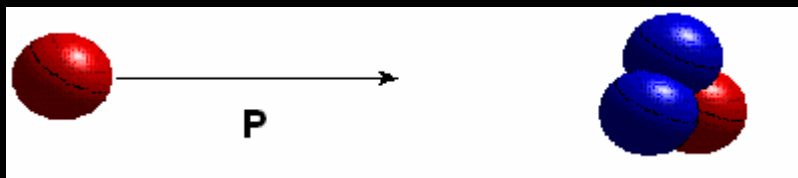
IN:



OUT:



Kinematics



$$M_{MB}^2 = (E - E_{\pi} + M_{SRC})^2 - P_{\pi}^2 - P^2 + 2PP_{\pi} \cos \theta_{\pi}$$

$$M_{MB} = f(M_{SRC})$$

$$M_{SRC} = f^{-1}(M_{MB})$$

Kinematics (continuation)

a priori: $M_{\text{SRC}, \text{min}} = n * 0.94$

Exp. masses of SRC:

$$M_n \geq n$$

GeV

Theor. masses of MB:

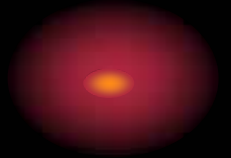
$$M_3^* = 3.62, M_4^* = 4.76, M_5^* = 6.07$$

GeV

Possibility of transition

(p + n-nucleon SRC) →

(n+1) MB + cumulative π



Denominations

1 *monobaryon*

2 *dibaryon*

3 *tribaryon*

4 *tetrabaryon*

5 *pentabaryon*

6 *hexabaryon*

7 *heptabaryon*

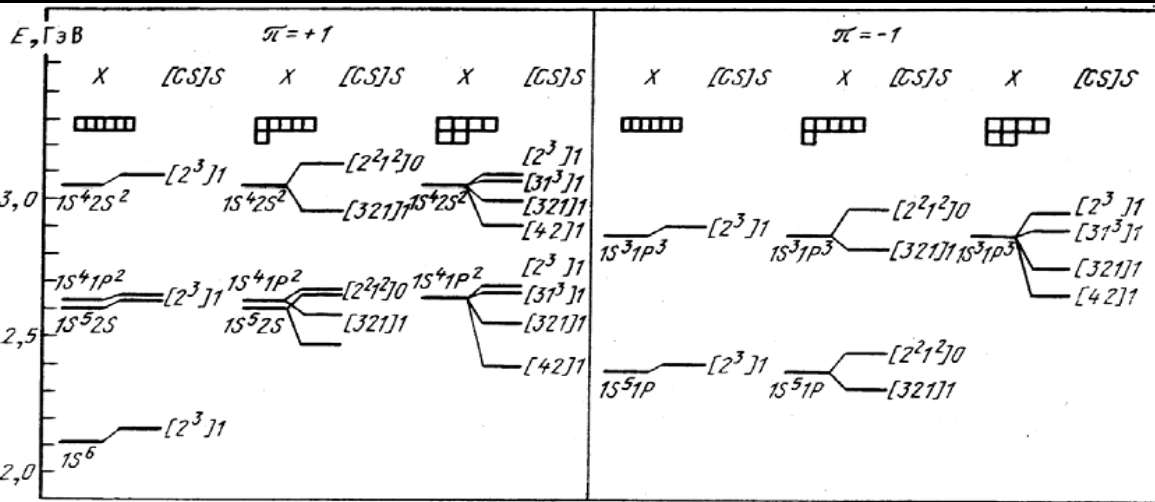
8 *octabaryon*

9 *nonabaryon*

10 *decabaryon*

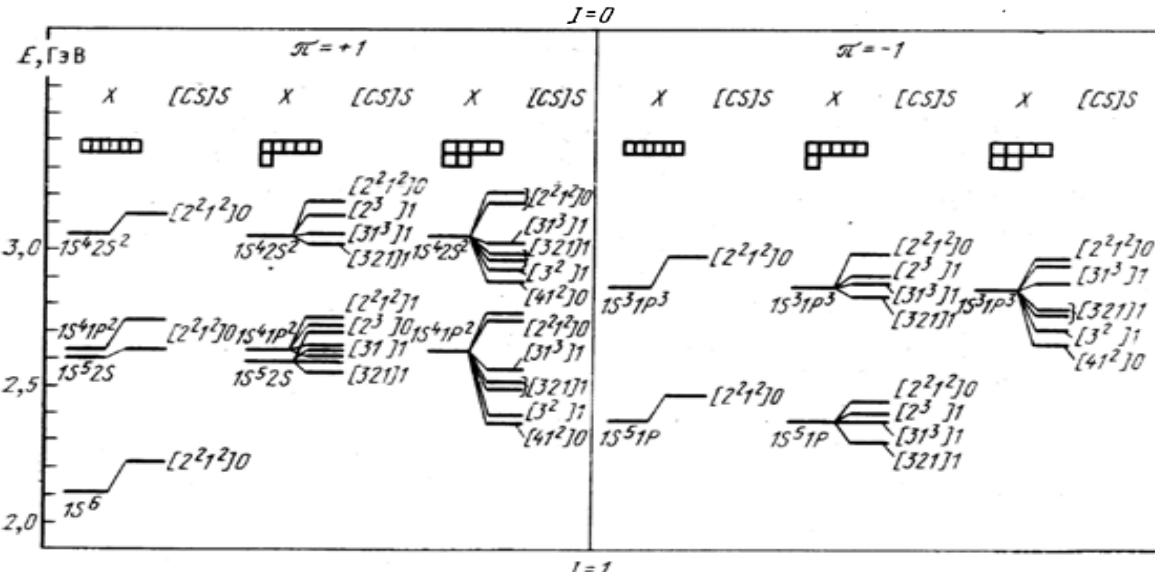


Experimental proposal :



**6-q system,
spectrum in MIT bag
framework**

**Dorkin SM, Reznik BL,
Titov AI,
Yad Fiz 36, 1244 (1982)**



CMM

**Momentum of the trigger
cumulative meson
can be precisely
calculated since
 $M_1=0.94$**

Experimental proposal

CMM

Investigation of dibaryon production in different nuclei (including hydrogen target) may give information on intranuclear pion – nucleus potentials in different nuclei:

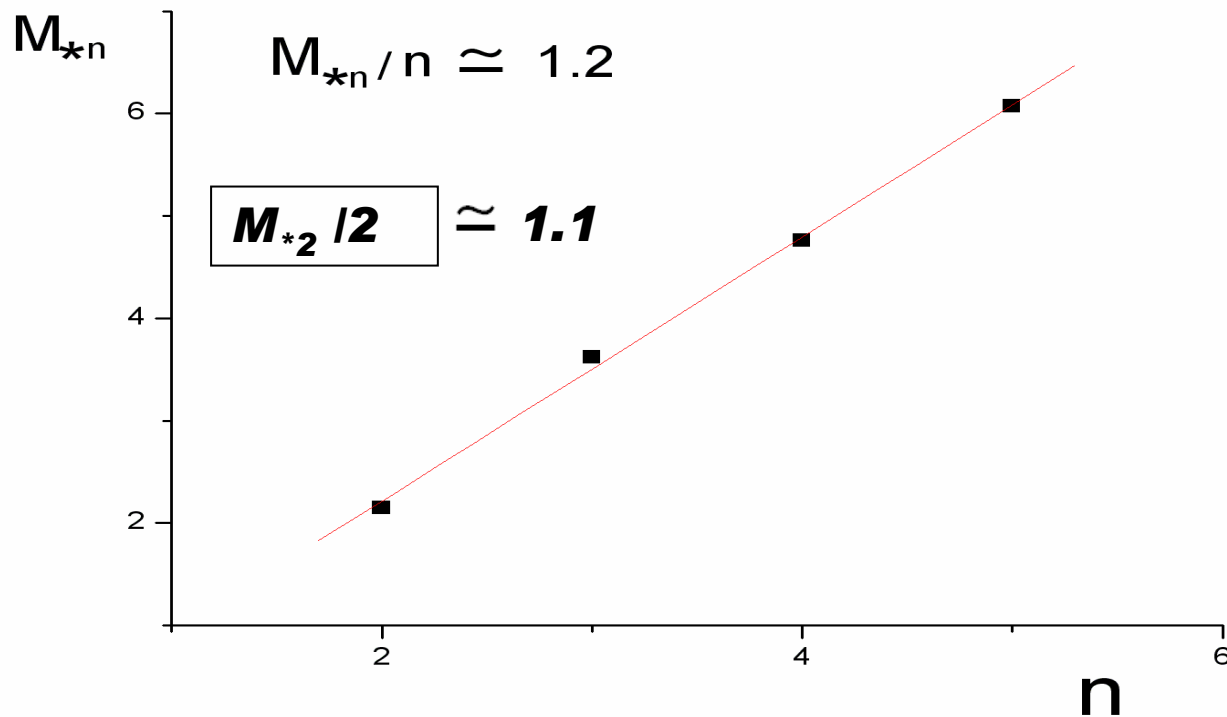
$P + \text{nucleus} \rightarrow \text{dibaryon} + \pi + \dots$

**Alternative explanation:
in-medium effect on dibaryon**



Finite size effects

1. Shell effects : 2—3 %



E. Farhi, R.L. Jaffe, Phys. Rev. D 30, 2379(1984)
J.J. de Swart, Phys. Rev.D 17, 260(1978)
V.K. Lukyanov, A.I. Titov, PEPAN 10, 815(1979)

Finite size effects



2. Surface tension coefficient for quark bag : $70 \text{ MeV}^3 \approx 8,8 \text{ MeV} | \text{Fm}^2$

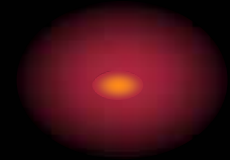
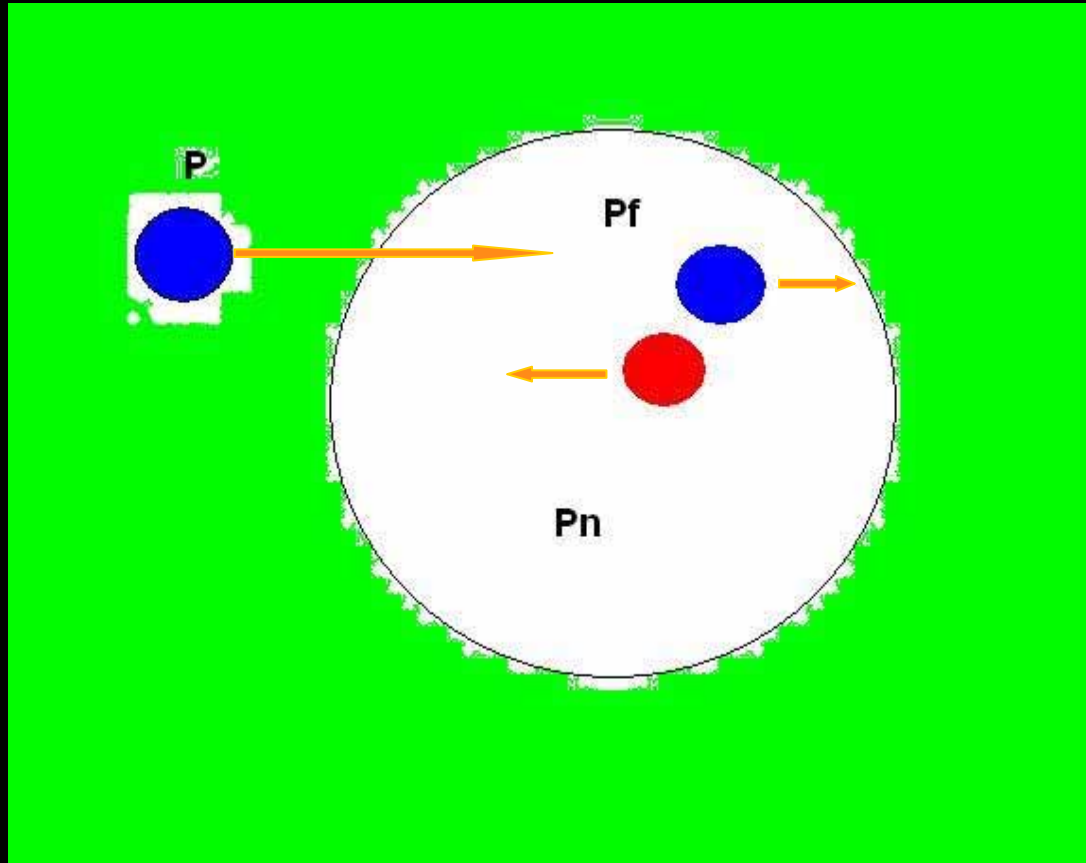
See E. Farhi, R.L. Jaffe, Phys. Rev. D 30, 2379(1984)

For M_3^* this gives 2–3 % correction given $R \approx 0.8 \text{ Fm}$

**Estimation of Casimir energy in chiral bag model,
see L. Vepstas, A.D. Jackson, Phys. Rep. 187, 109(1990)
gives the same**

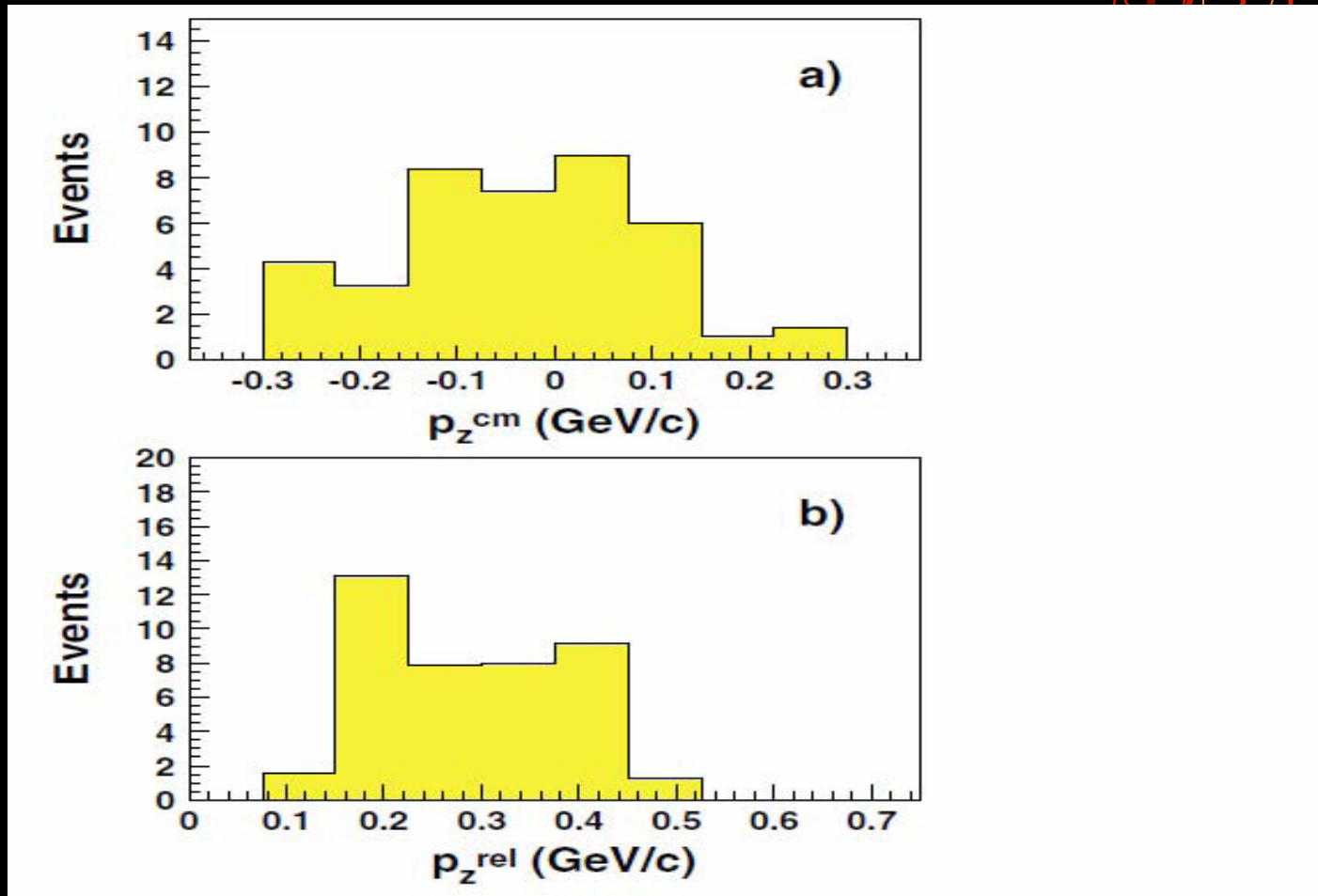
3. Coulomb repulsion : less 0.2 %

Experiment at BNL with EVA spectrometer

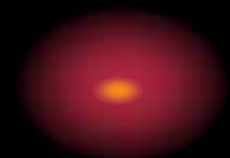


J. Aclander et al Phys. Lett. B 453, 211 (1999)
A. Tang et al Phys. Rev. Lett. 90, 042301 (2003)

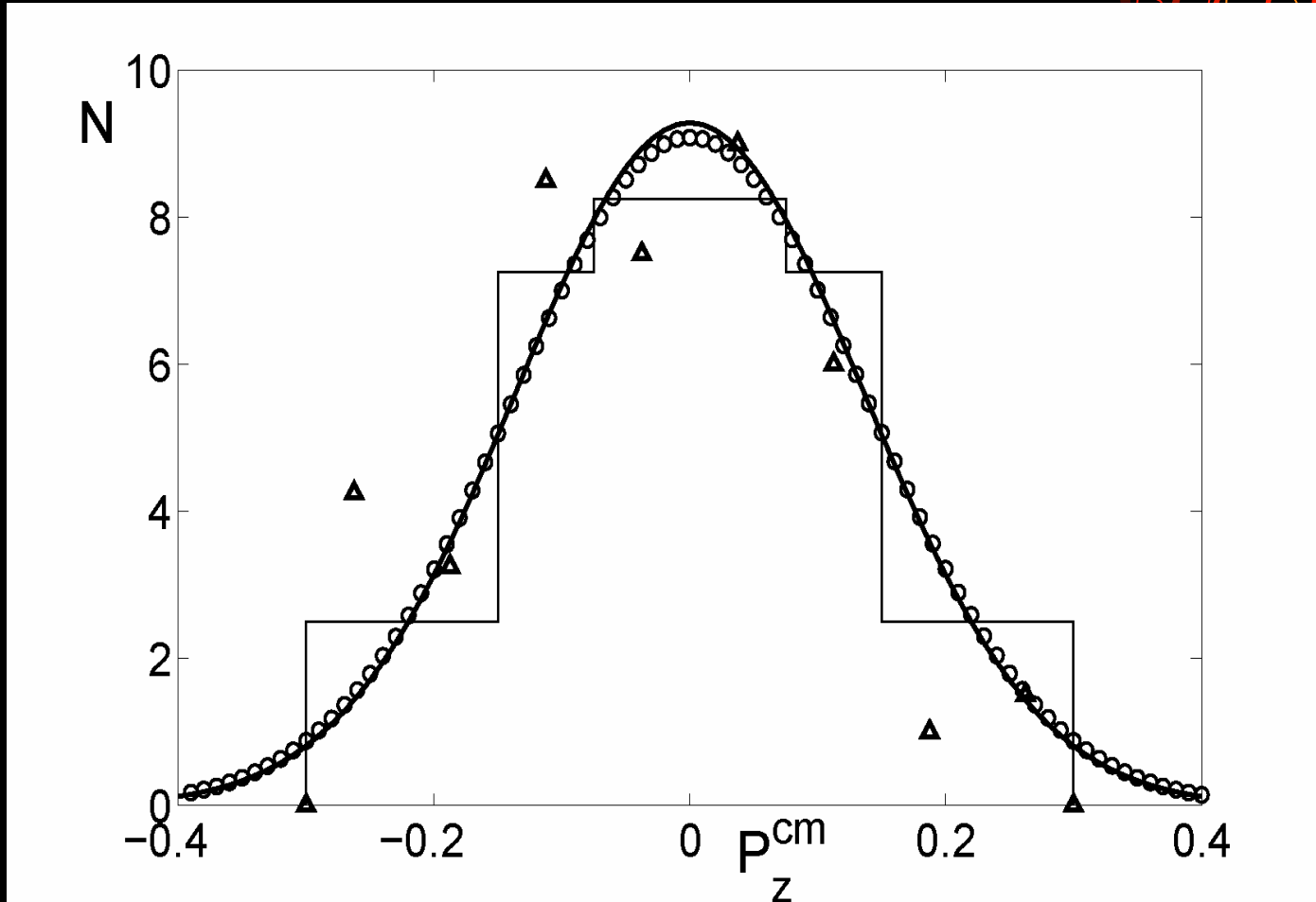
Experimental evidence for 2-nucleon SRC



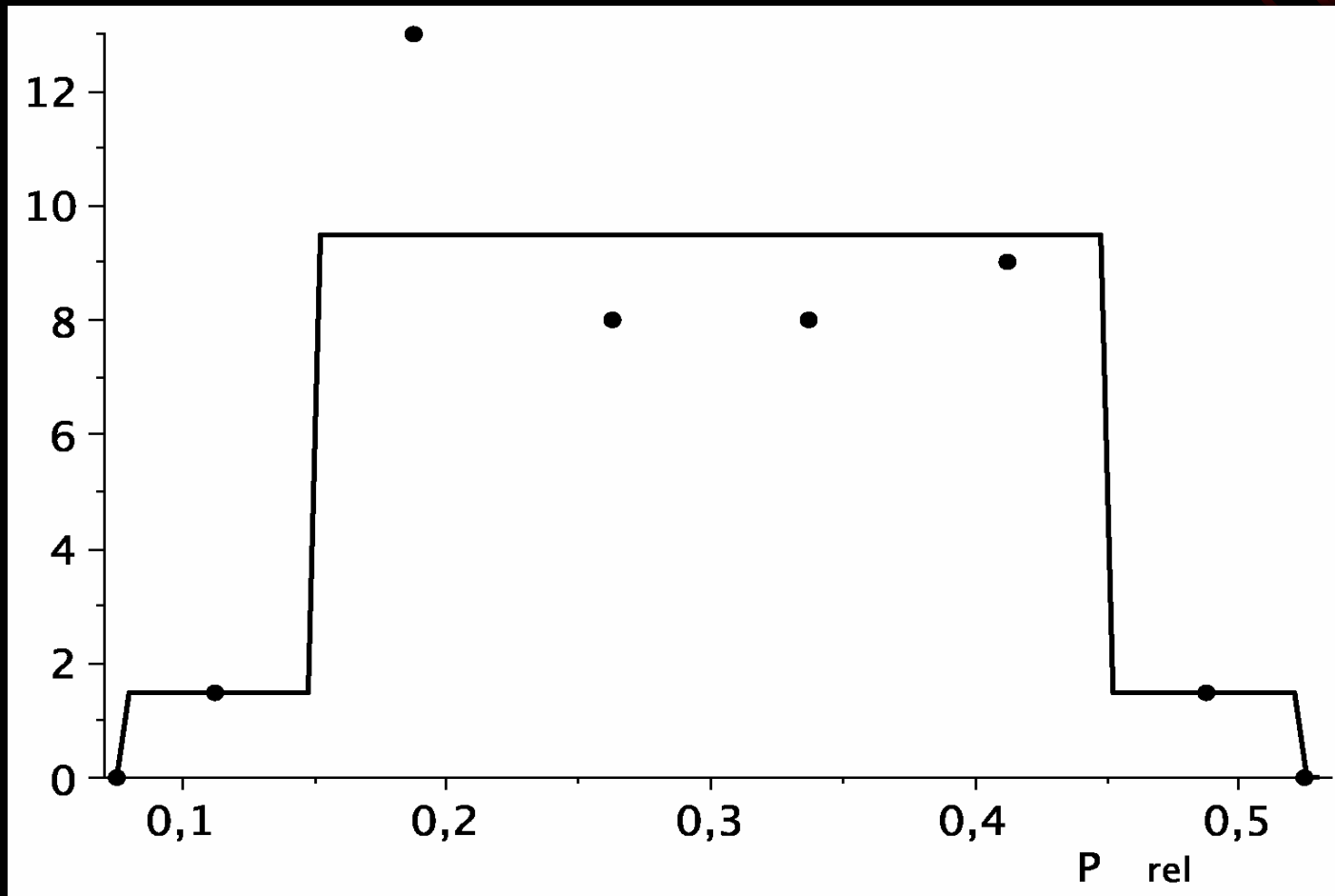
CM motion in longitudinal direction



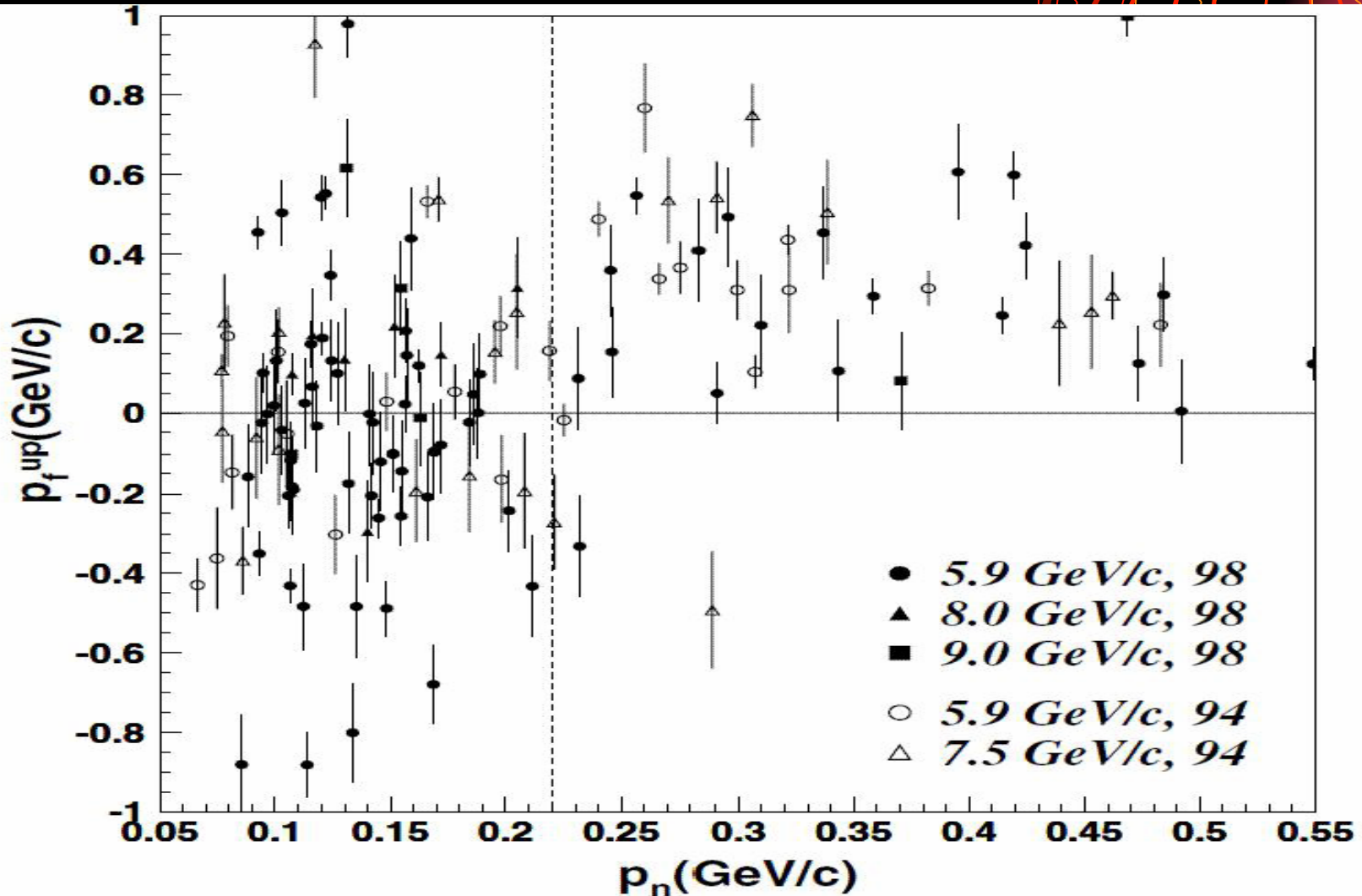
$\Sigma = 0.14$



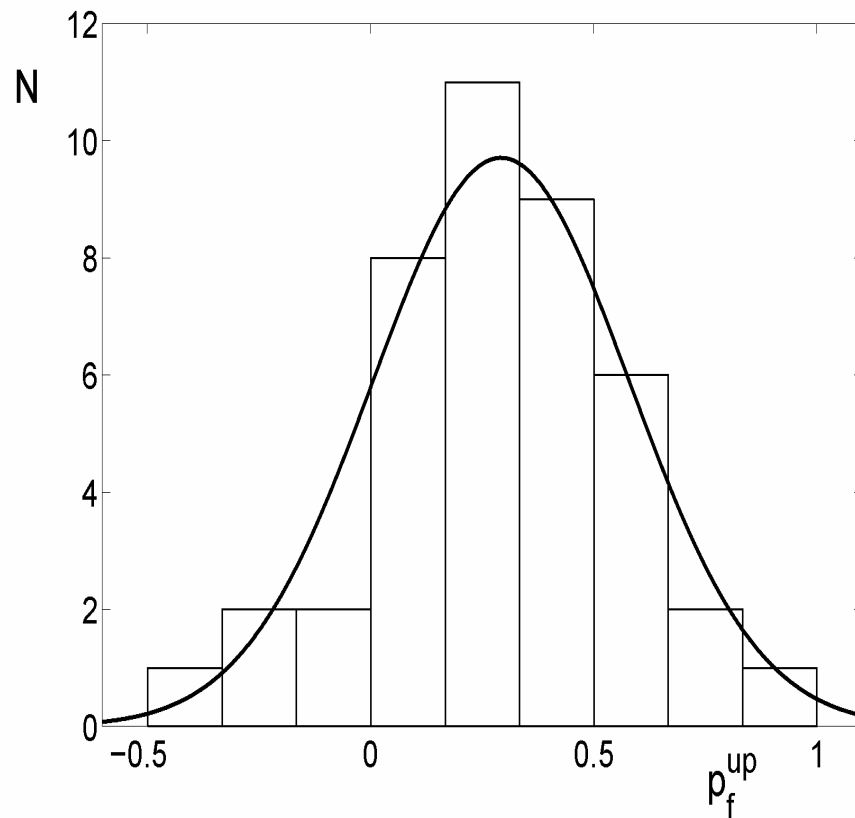
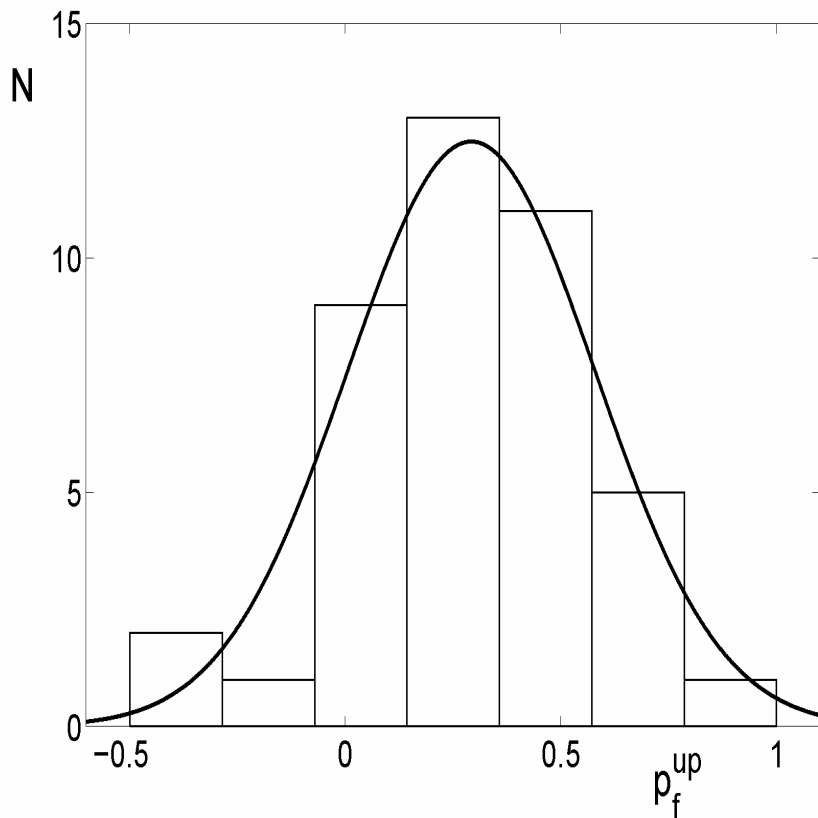
Relative motion in longitudinal direction



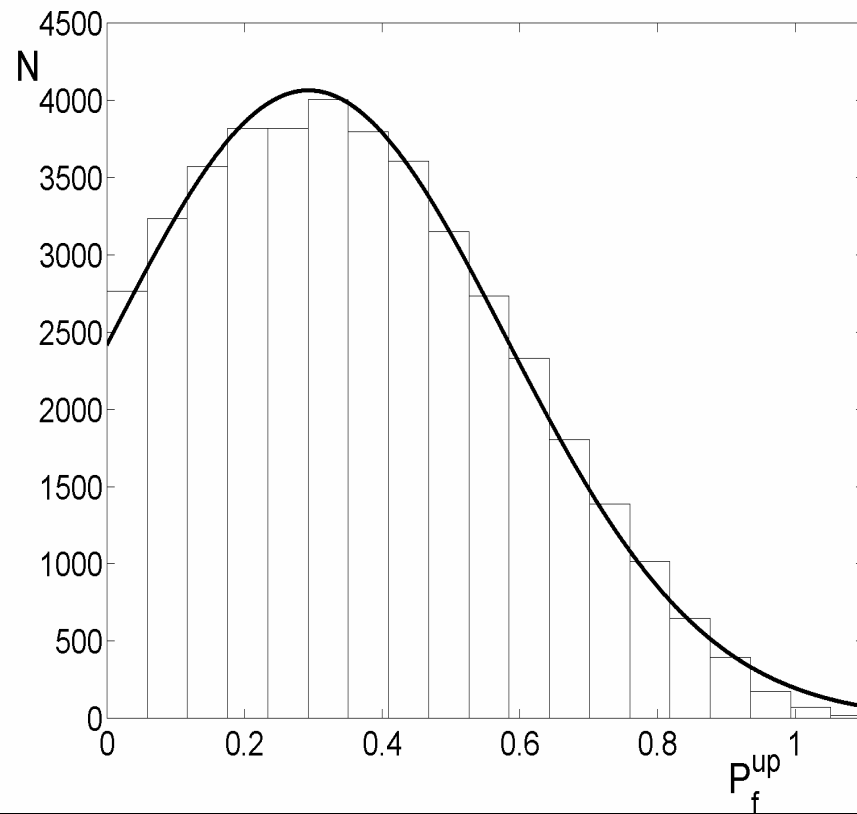
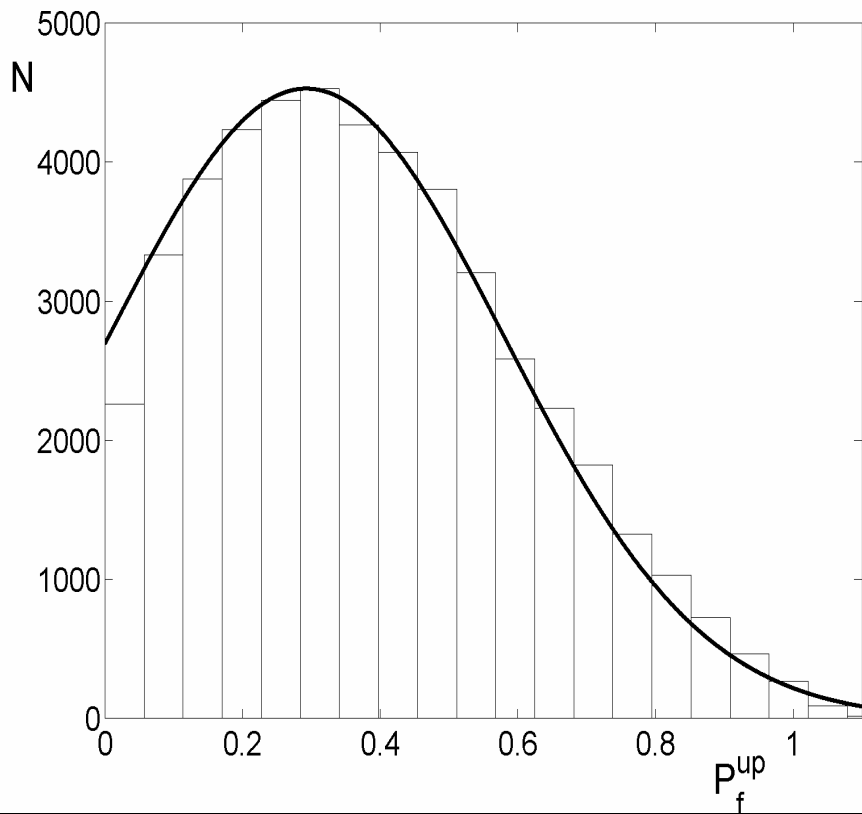
Motion in transversal direction



Distributions of P_x



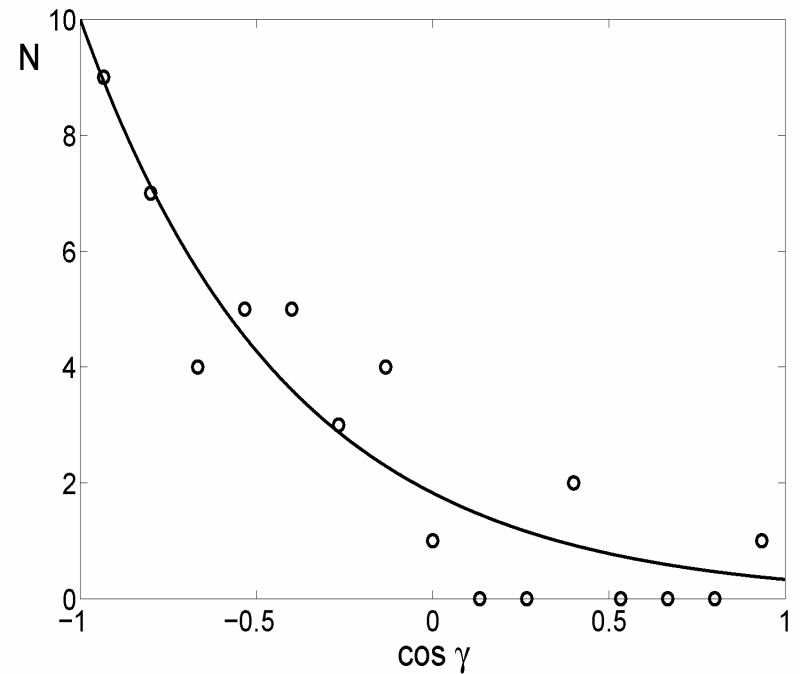
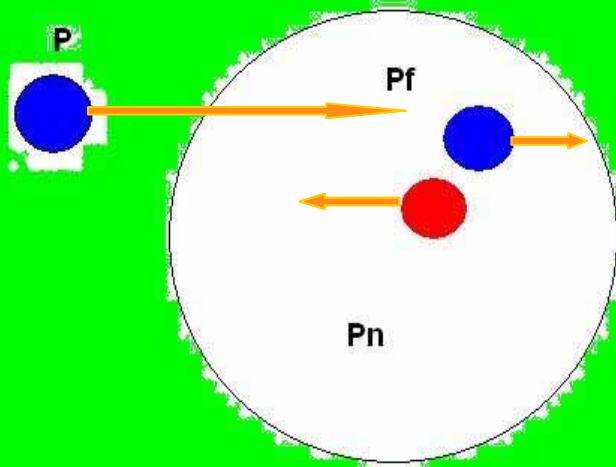
Summation of relative and CM motion



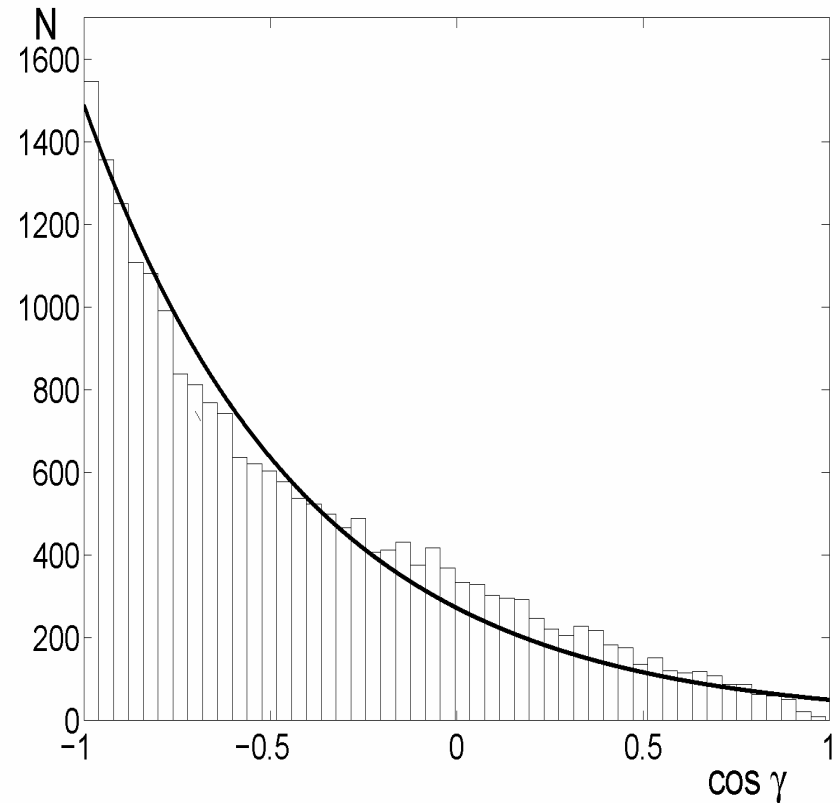
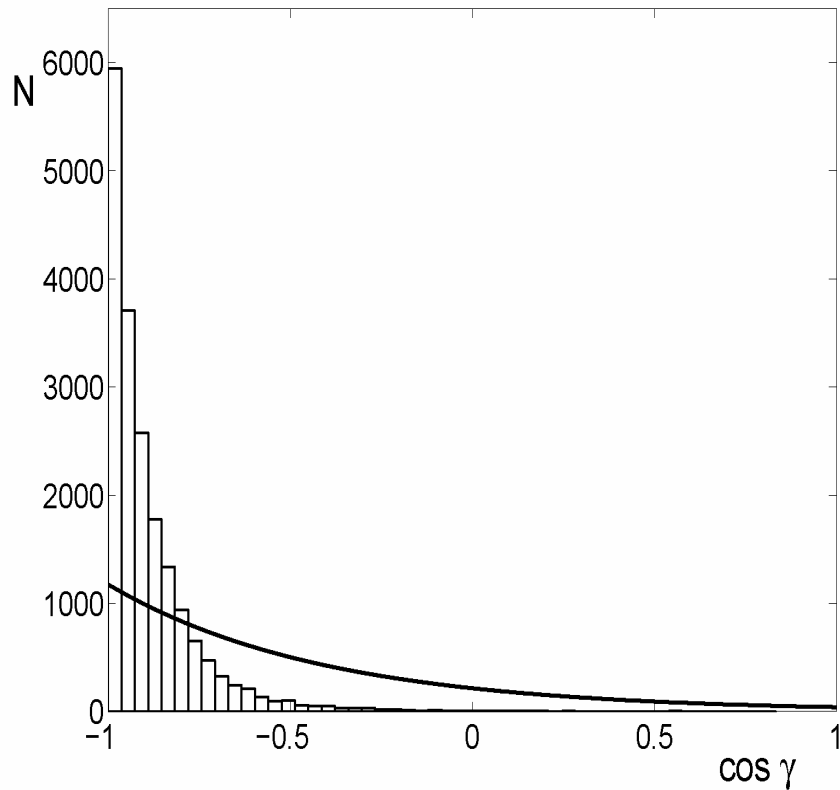
1. $\Sigma^{\text{cm}}=0.136, \Sigma^{\text{rel}}=0.586$

2. $\Sigma^{\text{cm}}=0.570, \Sigma^{\text{rel}}=0.212$

Model of quasi-elastic knockout



Recognition of CM motion

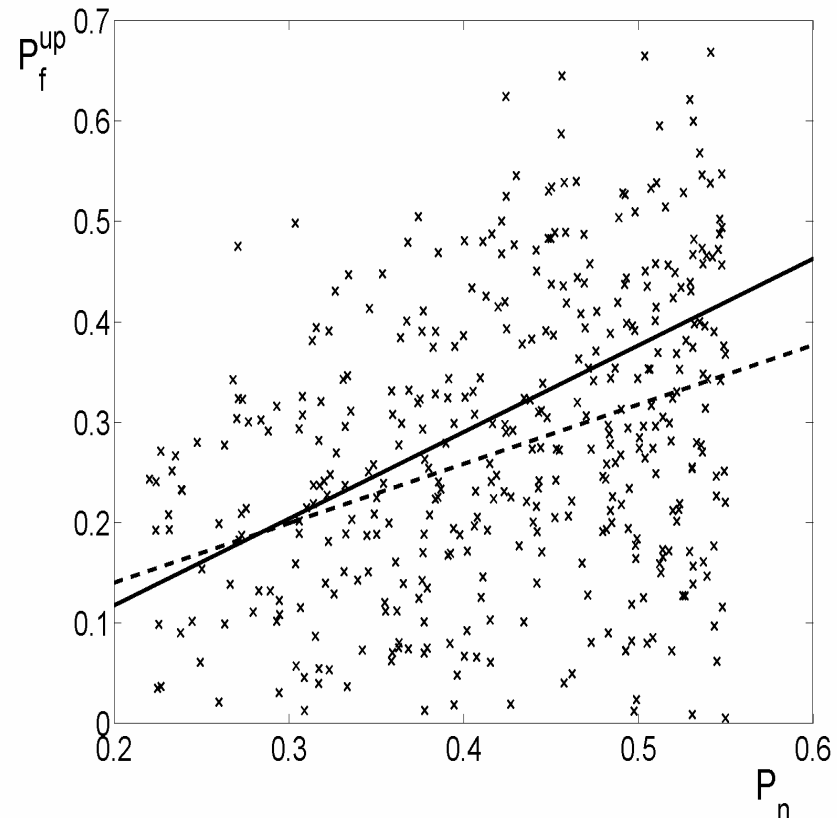
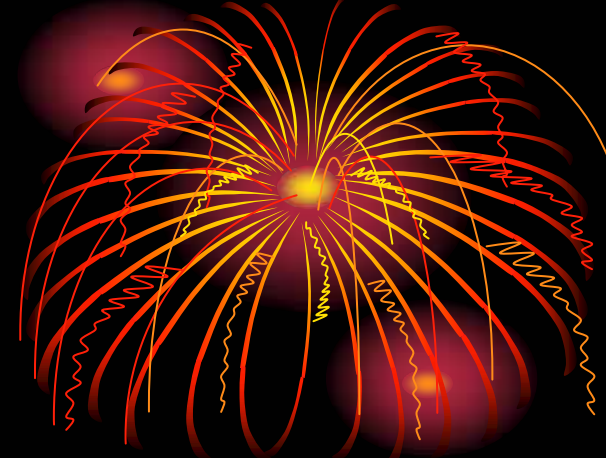


1. $\Sigma^{cm}=0.136, \Sigma^{rel}=0.586$

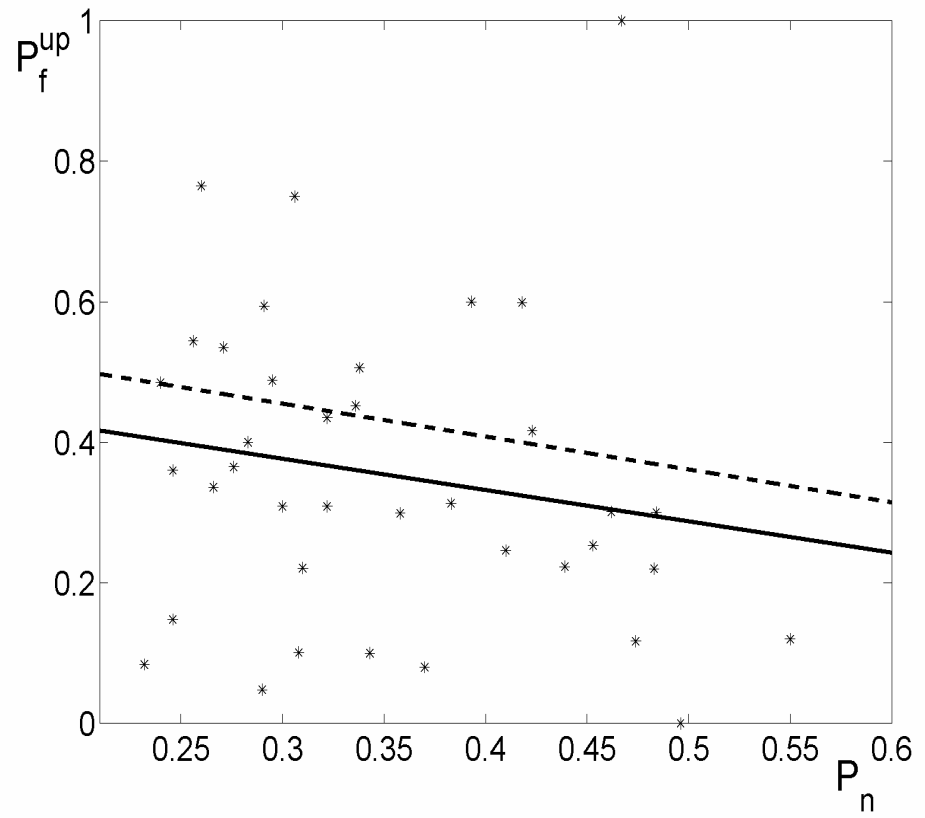
2. $\Sigma^{cm}=0.570, \Sigma^{rel}=0.212$

Additional evidence: correlation analysis

J. Aclander et al Phys. Lett. B 453, 211 (1999)



1. $\Sigma^{\text{cm}}=0.136$, $\Sigma^{\text{rel}}=0.586$



2. $\Sigma^{\text{cm}}=0.570$, $\Sigma^{\text{rel}}=0.212$

Reason for difference

Linear regression :

$$\langle p_f^{up}(p_n) \rangle = \langle p_f^{up} \rangle + \rho_{fn}^{\text{exp}} \frac{\sum_n^{up} f}{\sum_n^{\text{exp}}} (p_n - \langle p_n^{\text{exp}} \rangle)$$

The difference is due to the initial approximation of P_f^{up} distribution

Theoretical and experimental parameters \sum_n agree without special fitting, as well as correlation coefficients



Summary of our study of EVA results

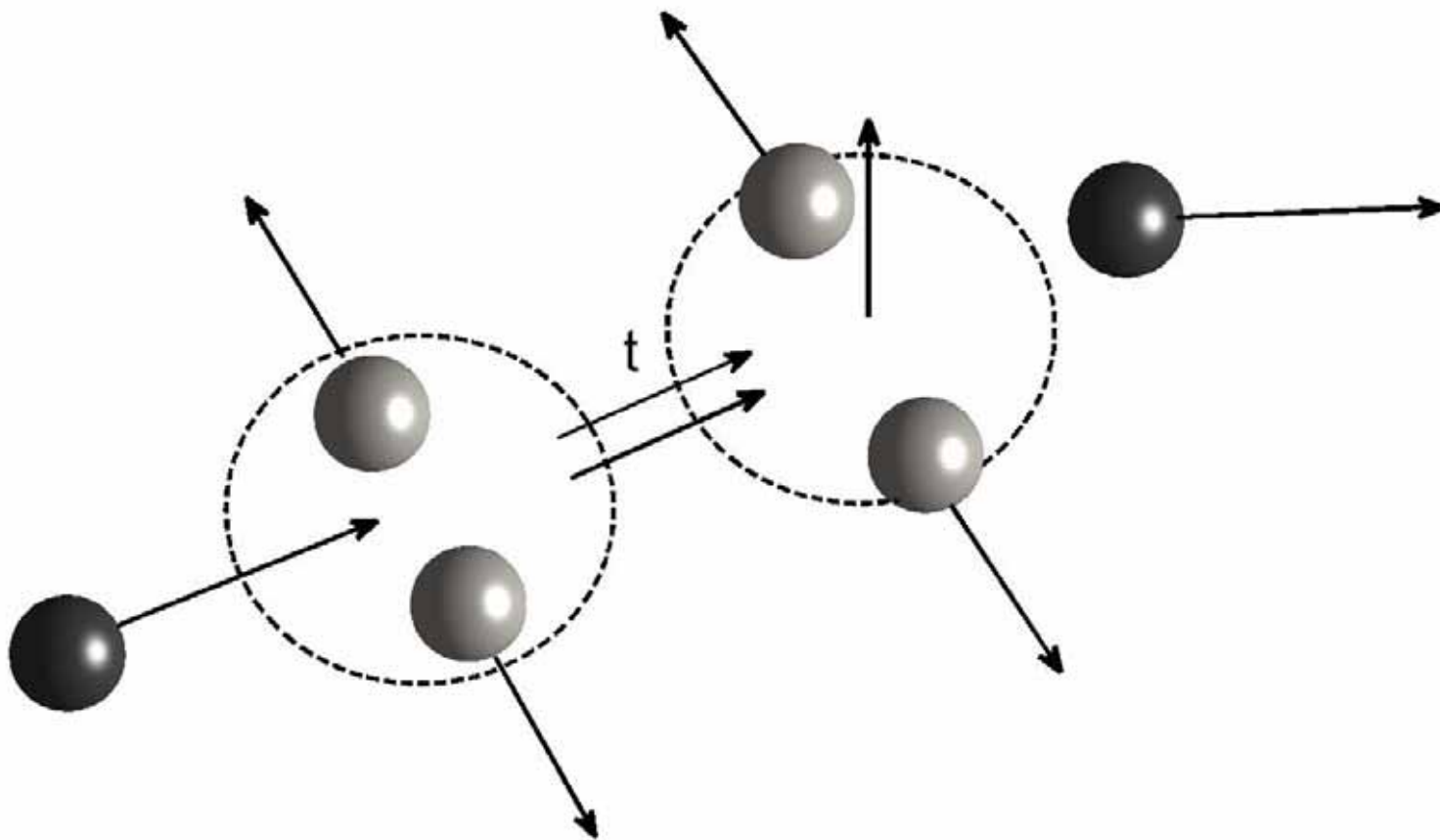


***1 We confirm EVA results for
momentum distributions of SRC,
 P^{cm} and P^{rel} , along z axis***

***2 EVA results permit also to
establish distributions for P^{cm}
and P^{rel} along the transversal
directions***

***3 Distributions P^{cm}_z , P^{rel}_z and
 P^{cm}_x , P^{rel}_x are very different***

Evident, but wrong explanation



Beyond the quasi-elastic knockout



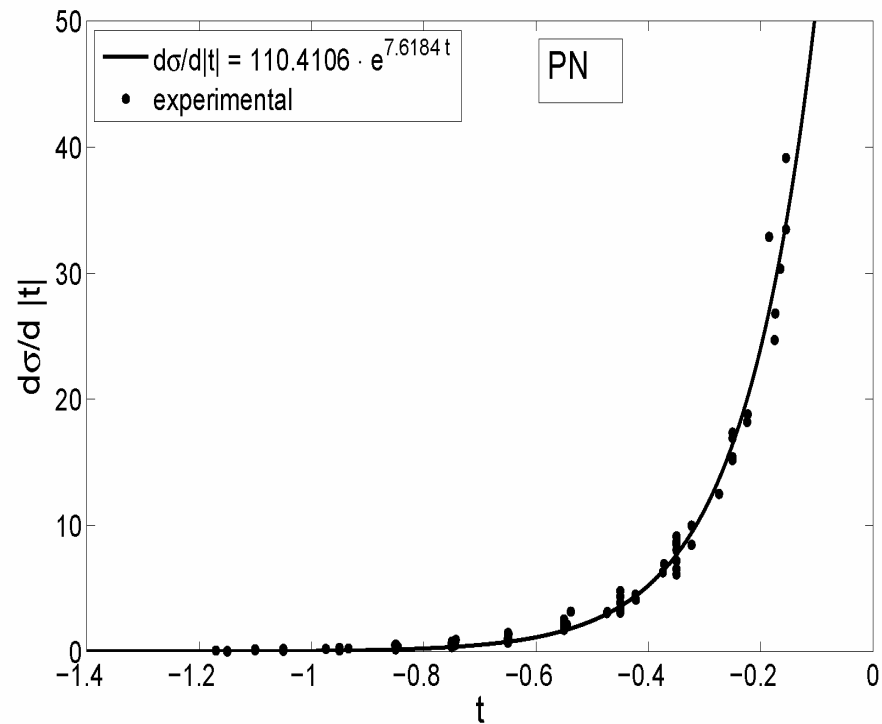
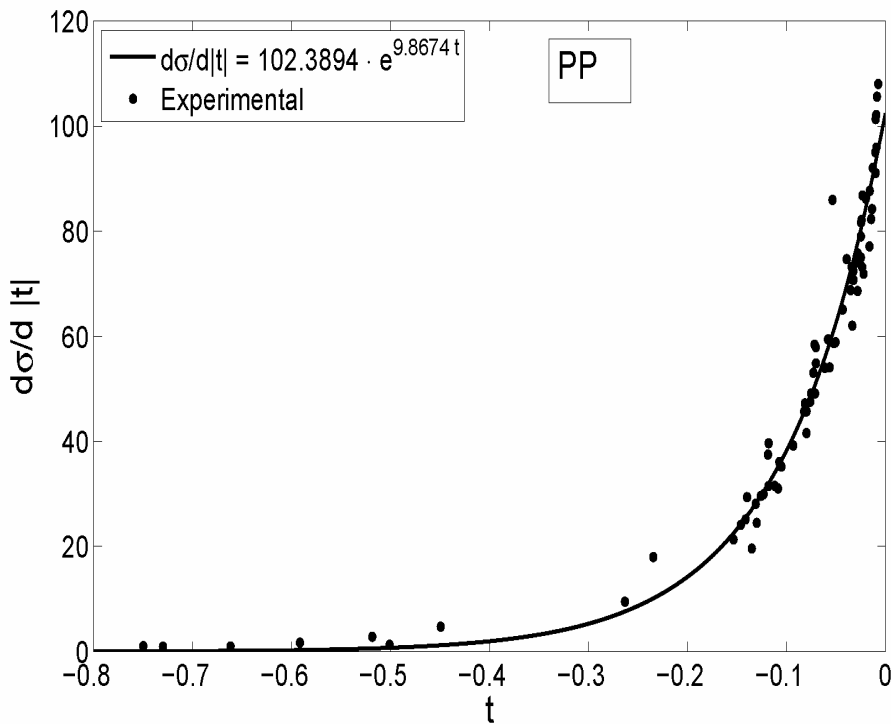
$$\vec{p}_0 + \vec{p}_{p,f} + \vec{p}_{n,b} = \vec{p}_1 + \vec{p}_2 + \vec{p}_n + \Delta\vec{p}$$

$$\vec{p}_f \equiv \vec{p}_1 + \vec{p}_2 - \vec{p}_0 = \vec{p}_{p,f} + \vec{p}_{n,b} - \vec{p}_n - \Delta\vec{p}$$

$$\vec{p}^{cm} \equiv \vec{p}_f + \vec{p}_n = \vec{p}_{p,f} + \vec{p}_{n,b} - \Delta\vec{p}$$

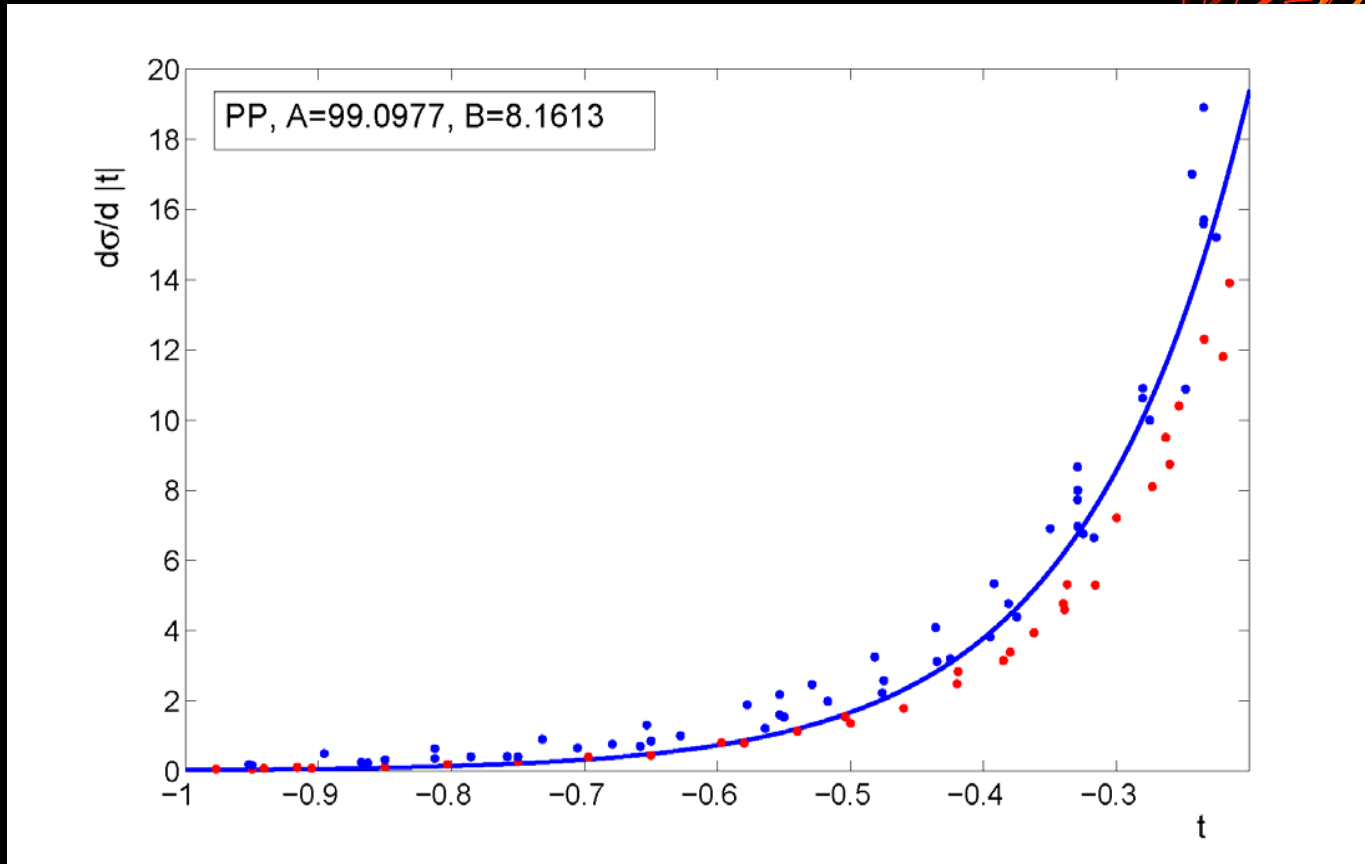


May ΔP arise from elastic scattering of projectile ?



Compilation exp data from the LANDOLT - BÉRSTEIN tables

t- and s- dependence



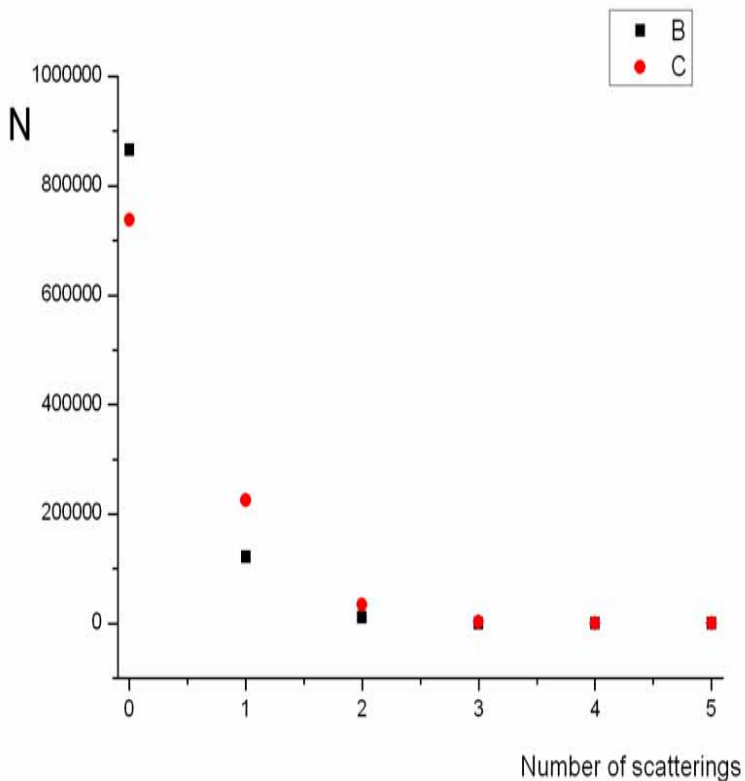
Experimental data from the LANDOLT – BÉRSTEIN compilations

Main suggestions of simulation program

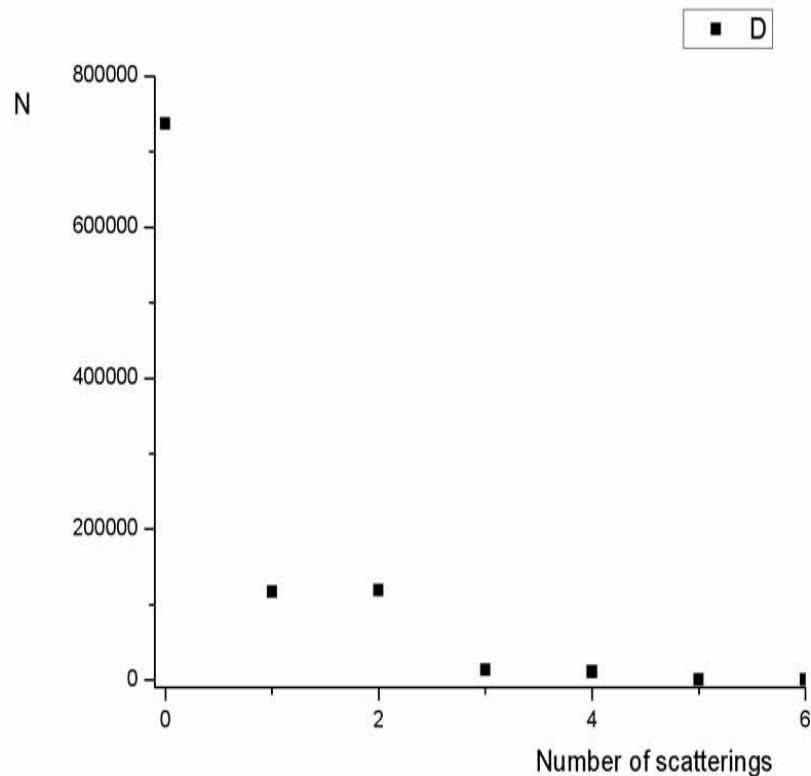


- 1. Nuclear density ρ : Woods-Sakson shape, $r_N \approx 0.2 \text{ Fm}$, $E_{N,bind} = .006$**
- 2. Probability to find 2-nucleon SRC is $\sim \rho^2$**
- 3. Respect for the Pauli principle with $P_{\text{Fermi}} = 0.22 \text{ GeV} / c$**
- 4. There were no π -mesons accompanying secondary nucleons in the final state**
- 5. Only elastic scattering of projectile before and after collision with SRC is taken into account (main contribution to P_{tr})**

How often scatterings take place ?



**Scattering of 0 and 1 particles.
Effective anticorrelation**

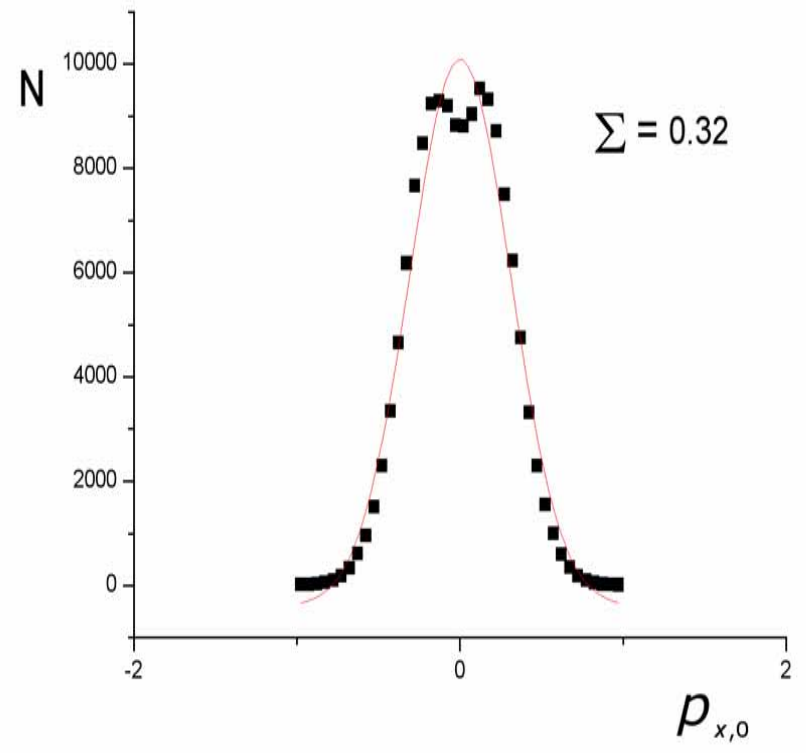
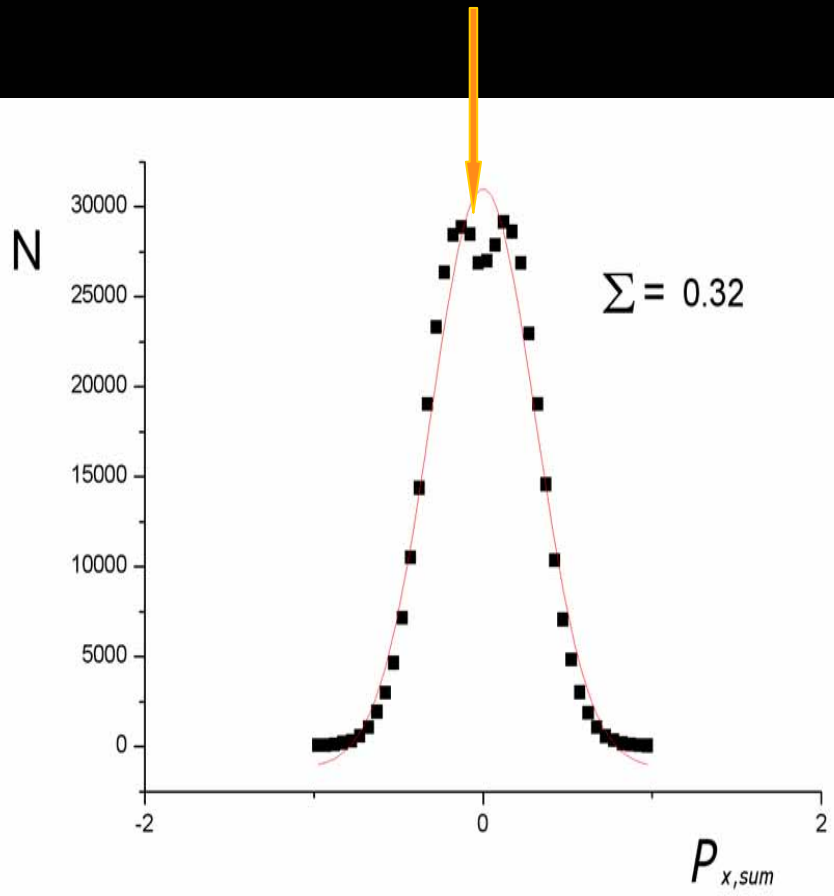


**Scattering at least one of them.
Events without additional scattering
dominate : $P_0 = 0.74$**

Contribution of additional scattering to P_{tr}



Depression due to the Pauli principle



Is this enough ?



$$\left\langle (\xi_1 - \langle \xi_1 \rangle)^2 + (\xi_2 - \langle \xi_2 \rangle)^2 \right\rangle = \Sigma_1^2 + \Sigma_2^2 + 2\rho_{12}\Sigma_1\Sigma_2$$

$$\rho_{12} = 0$$

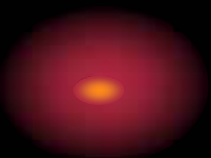
$$\Sigma_{sum} = \sqrt{\Sigma_1^2 + \Sigma_2^2} = \sqrt{\Sigma_{cm,z}^2 + \Sigma_{scatt}^2} = \sqrt{0.14^2 + 0.32^2} = 0.35 < 0.57$$

No! Even in the case $P_0=0$!

Summary of our study of intranuclear scattering



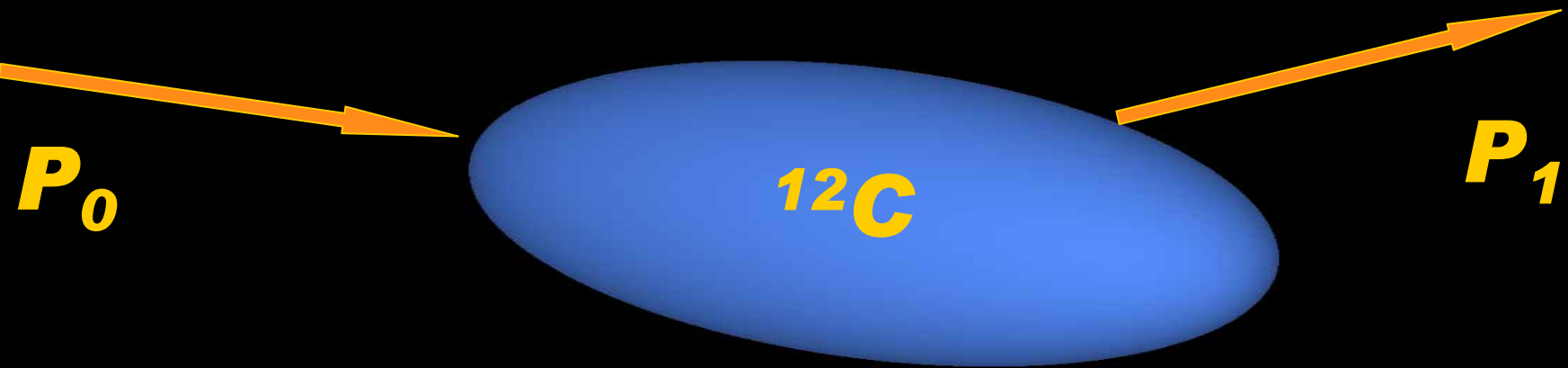
Contribution of the intranuclear scattering is insufficient for description of the observed motion of SRC along the transversal direction



More intensive Fermi motion ?



Nuclear states squeezed in transversal direction



Unconsidered possibilities:



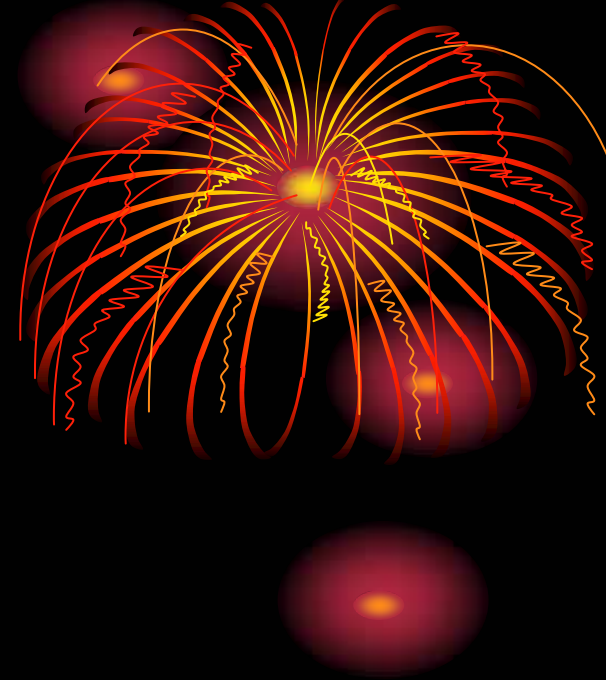
- 1) Experimental mistake: there were missing (lost) π - mesons in each relevant experimental event***
- 2) Theoretical mistake: colour anti - transparency was observed (instead of expected colour transparency)***

Possible wave function of ^{12}C

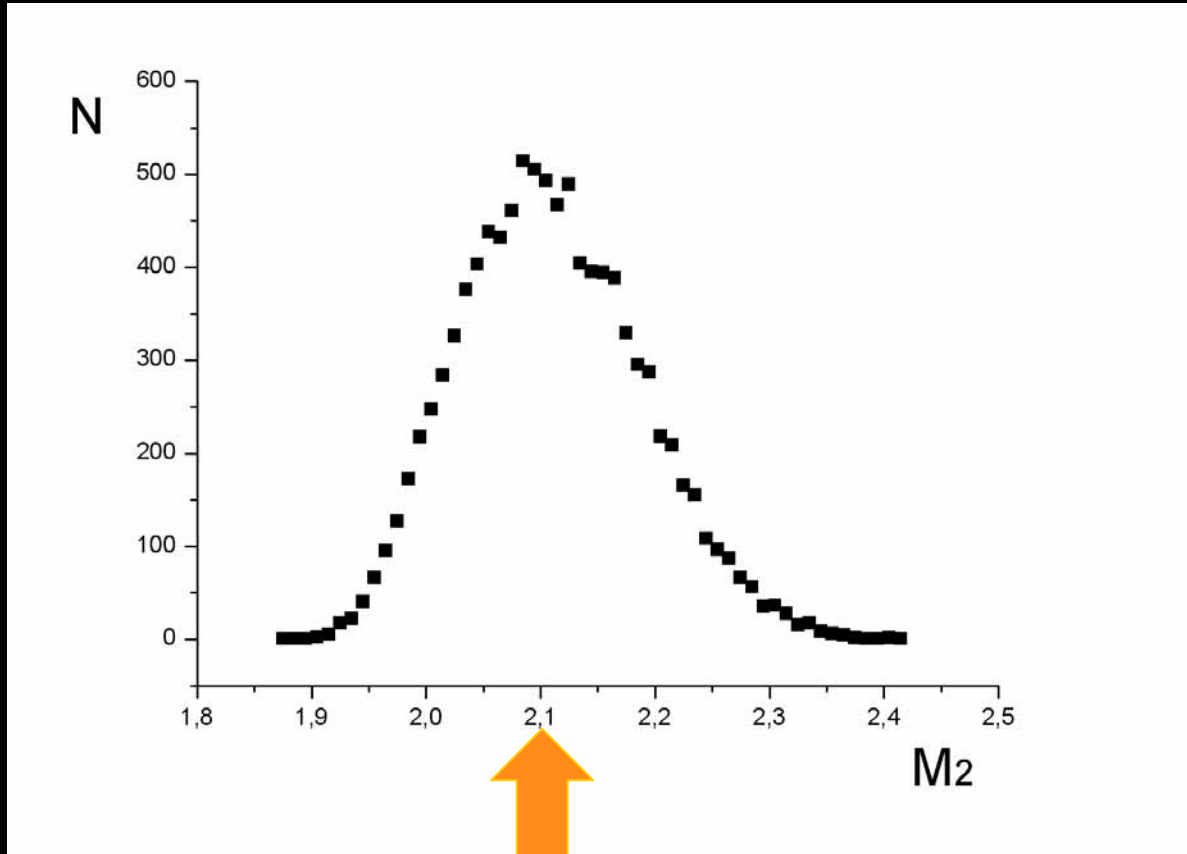
$$|\Psi\rangle = \dots + \alpha |\Psi_{\perp}\rangle \otimes |\Psi_{\parallel}\rangle$$

Independent measurement of transversal size (large momentum transfer) and longitudinal size (low momentum transfer)

SRC appears only inside a squeezed state of nucleus ?

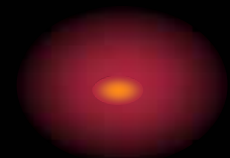
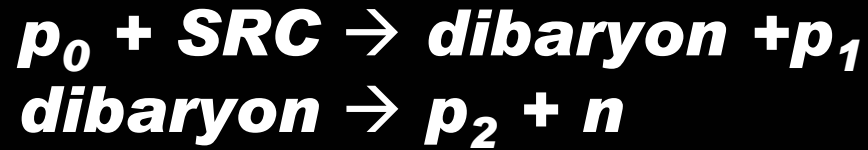


Mass distribution

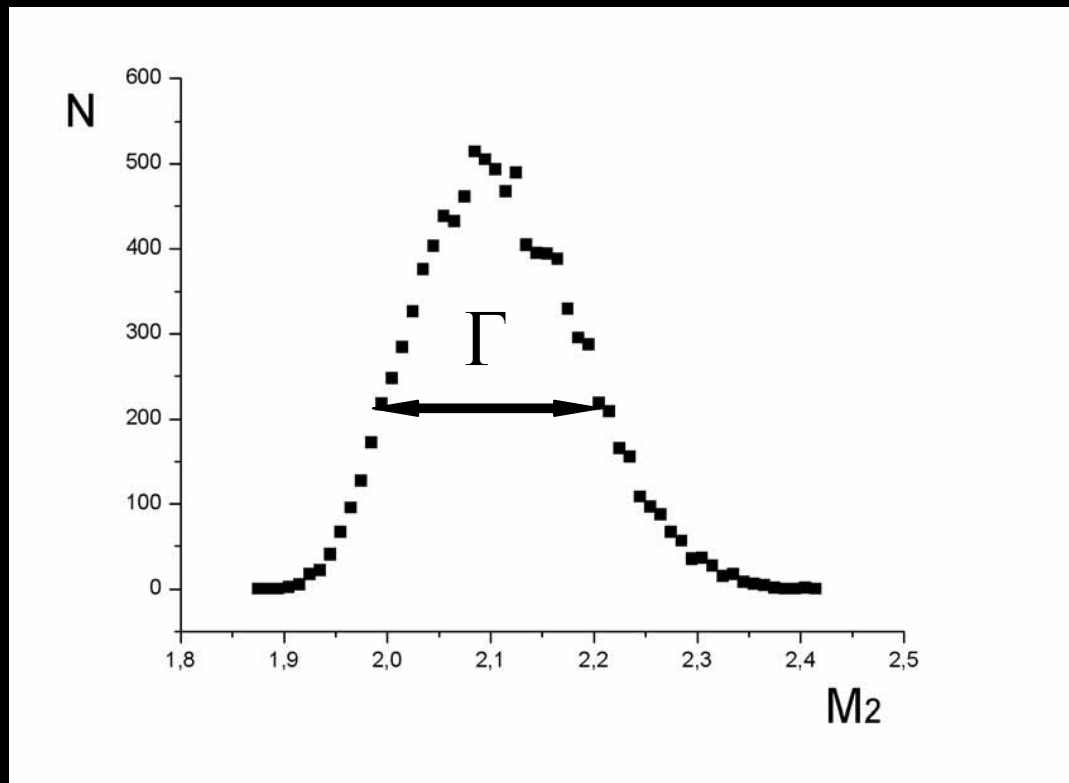


Most probable mass of SRC measured with EVA spectrometer

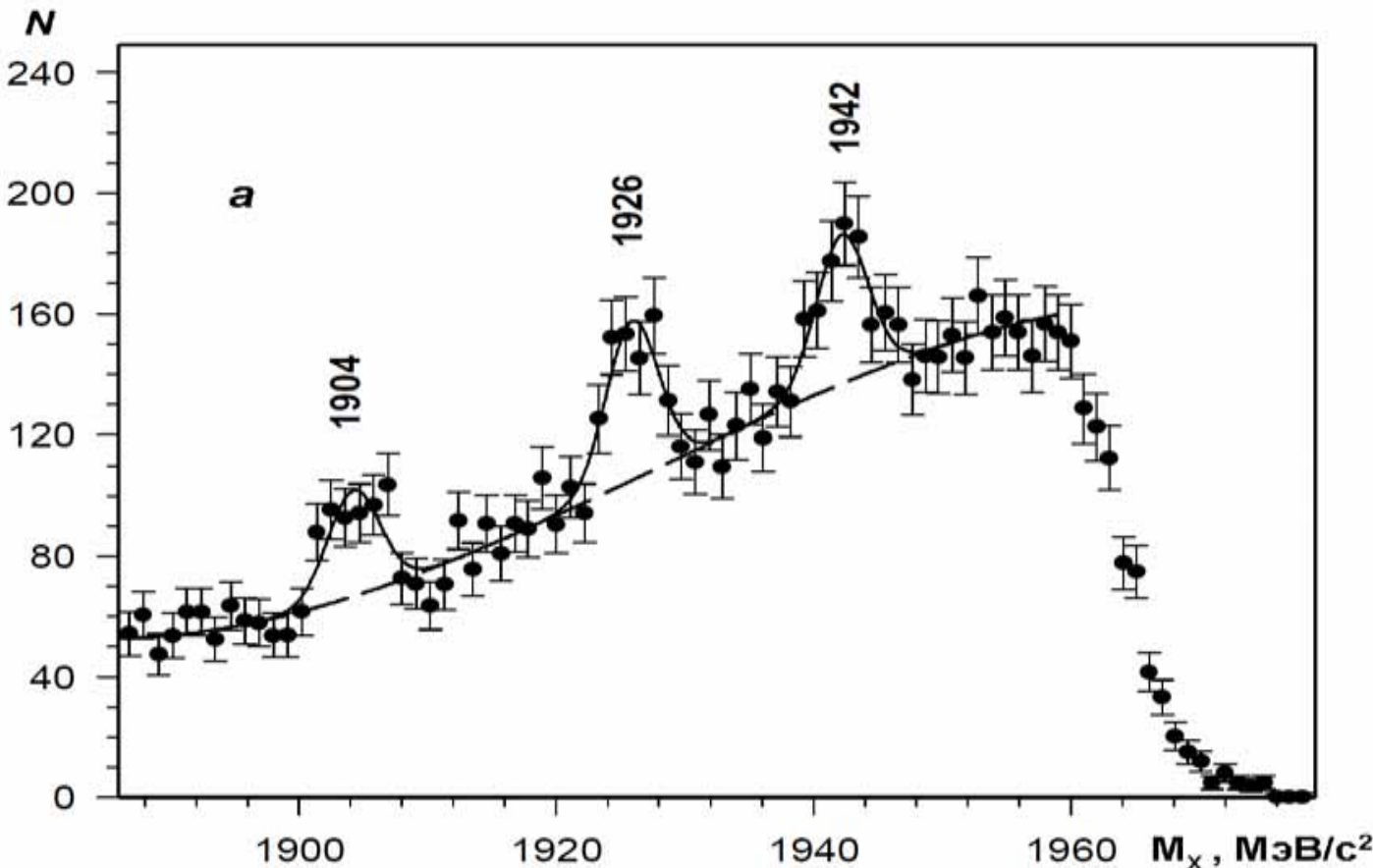
May it be dibaryon production ?



$$M_{\text{dibaryon}} \approx 2.15$$



Experimental proposal: to increase resolution

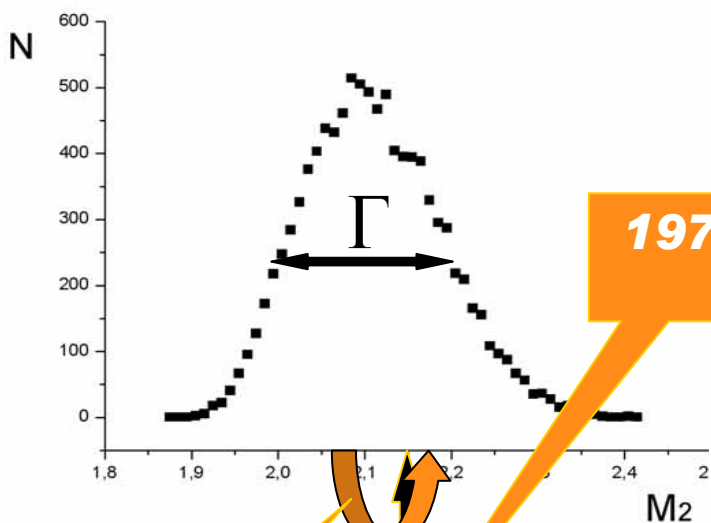


$p d \rightarrow p + p X$

**Method:
invariant mass
 M_{pX} spectra**

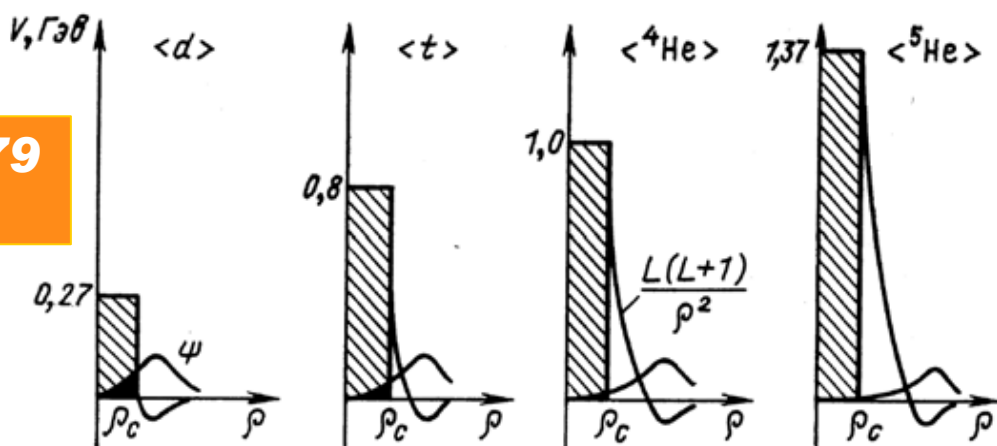
***LV Fil'kov et al (Lebedev Institute + JINR)
Baldin ISHEPP XV, 2000***

May it be flucton existing before interaction?



1979

Lukyanov, Titov, PEPAN 1979



1984

Burov, Lukyanov, Titov, PEPAN 1984

$M_2 = 0.208 - 0.218$

**How created and
pre-existing MB may be
discriminated ?**



CNM versus CMM

$p_0 + \text{SRC} \rightarrow \text{dibaryon} + p_1$

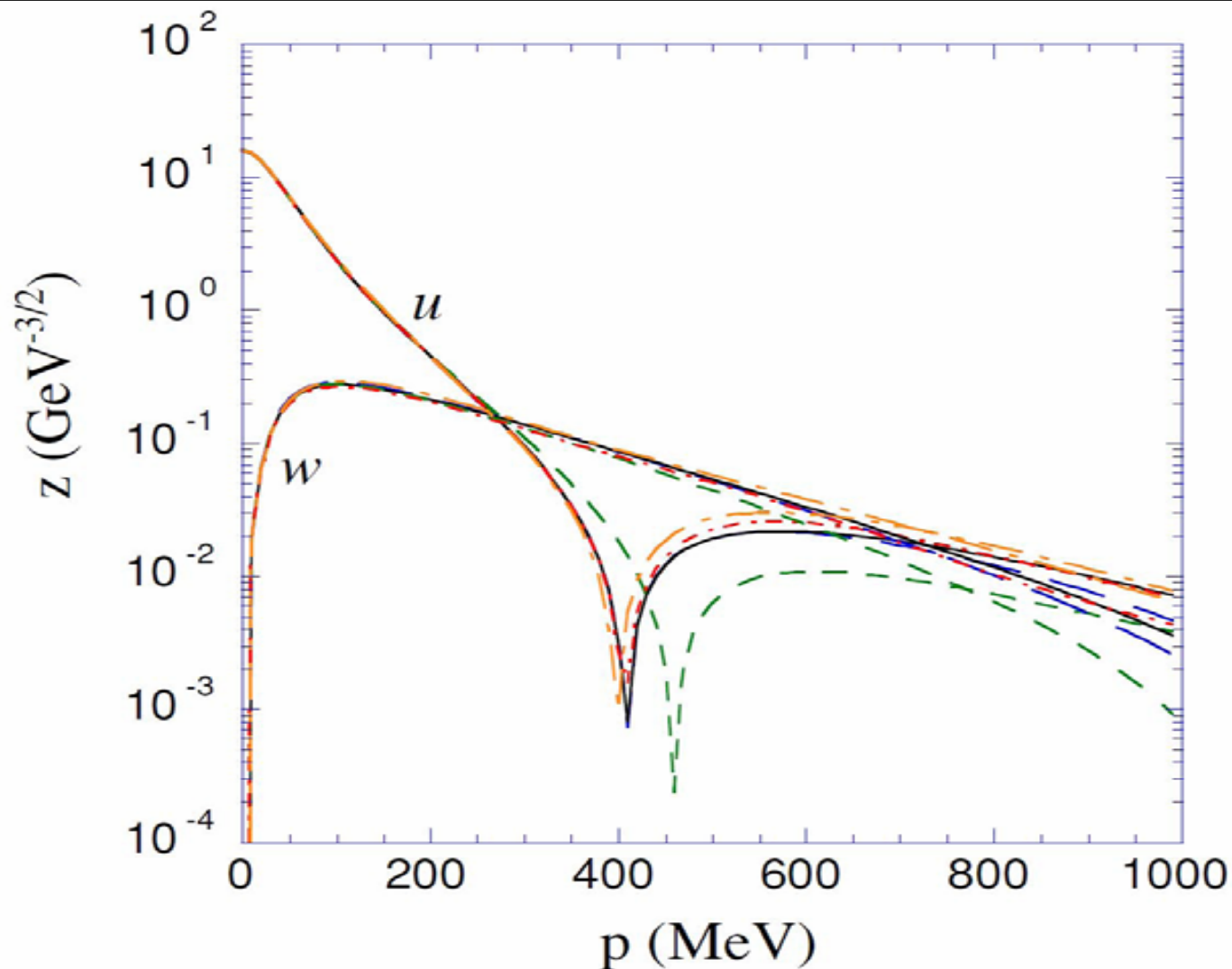
$\text{dibaryon} \rightarrow p_2 + n$

**Measurement of the projectile
particle momentum transfer**

$p_1 - p_0$

May it be SRC ?

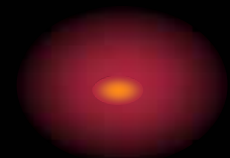
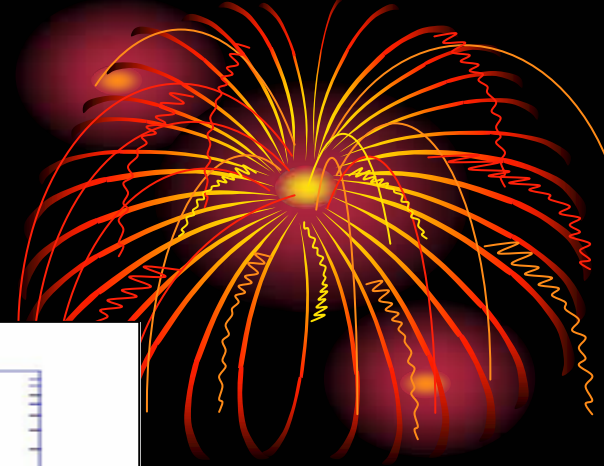
R. Gilman, F. Gross, J Phys G 28 (2002) R37



$P_S = 0.24$

$P_D = 0.76$

$0.45 < P < 1.1$

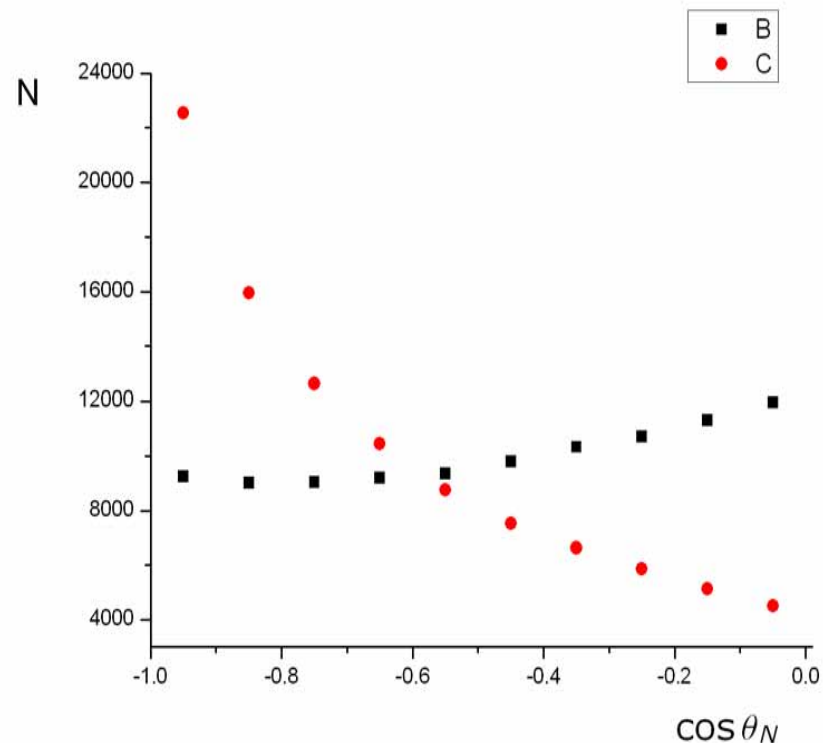
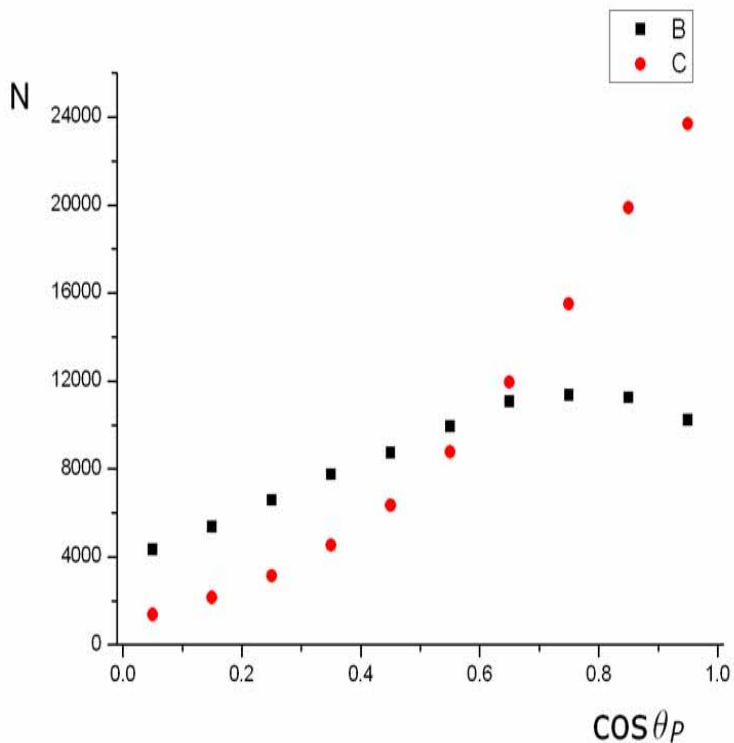


May it be SRC ?

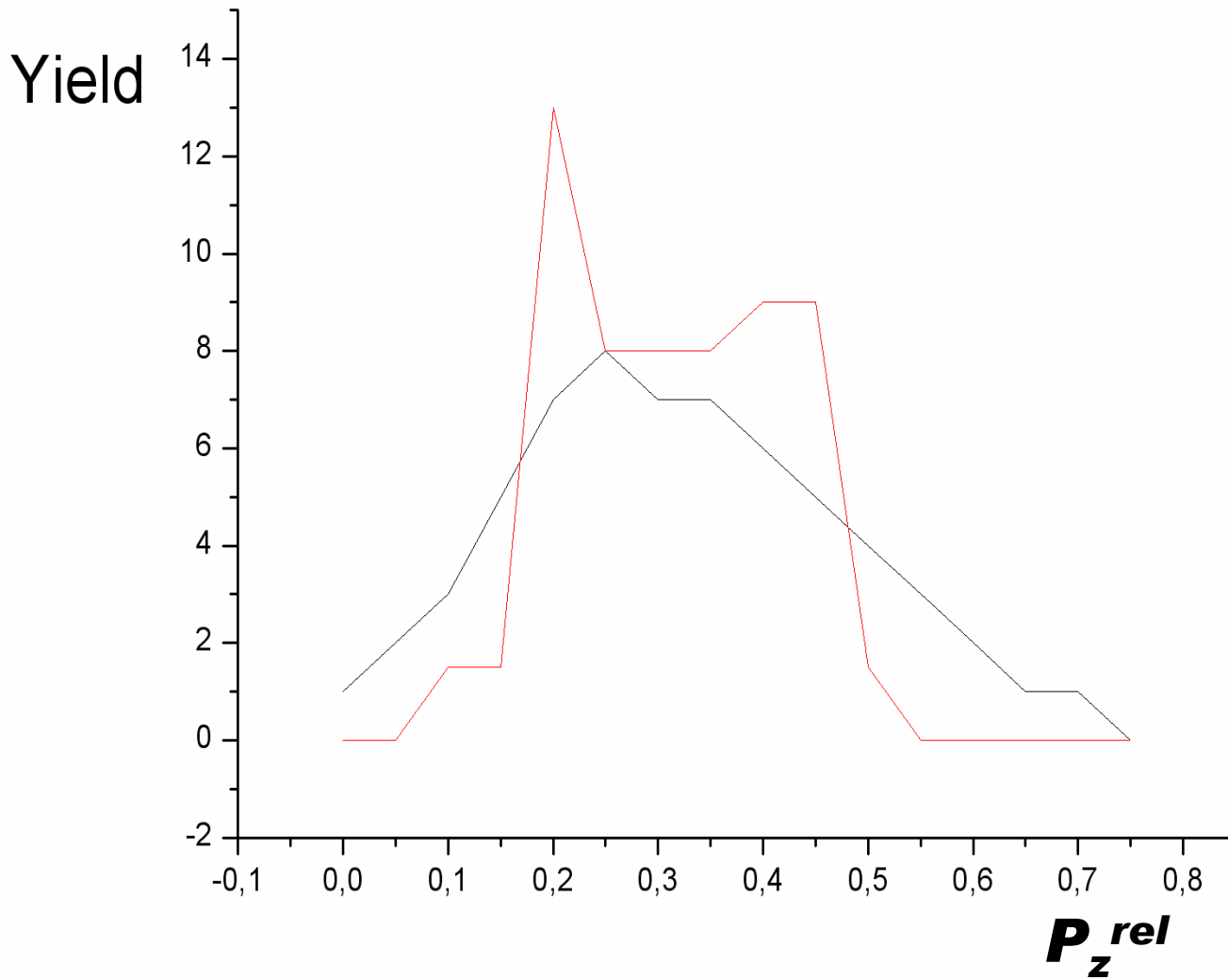
Influence of quark counting rules

$$d\sigma/d\Omega = (s - 4m^2)(4\pi)^{-1} d\sigma/dt$$

$$d\sigma/dt \sim s^{-9}$$




May it be SRC ?



**Experimental cut-offs:
Neutron moves downward and backward,
 $0.05 < P_n < 0.55$ GeV**

Probability for tails to be cut ≈ 0.84

Experimental proposal : knockout or creation of MB



Cumulative particle is nucleon

**Search for 6 – q bag : to improve
statistics in an experiment of
EVA type for the purpose
of to refine P_z^{rel} distribution**

Toward true cumulative effect



P_p	SRC	EXP
0.715	$0.33 \pm 4\%$	$0.33 \pm 10\%$
0.888	$0.12 \pm 6\%$	$0.06 \pm 10\%$
1.026	$0.031 \pm 12\%$	$0.012 \pm 10\%$

EVA:

$$P_n < 0.55$$

ITEPh :

$$0.58 < P_p < 2.215$$

S.V.Boyarinov et al Yad. Fiz. 57, 1452(1994)

Signature of N N fusion

P+Be,

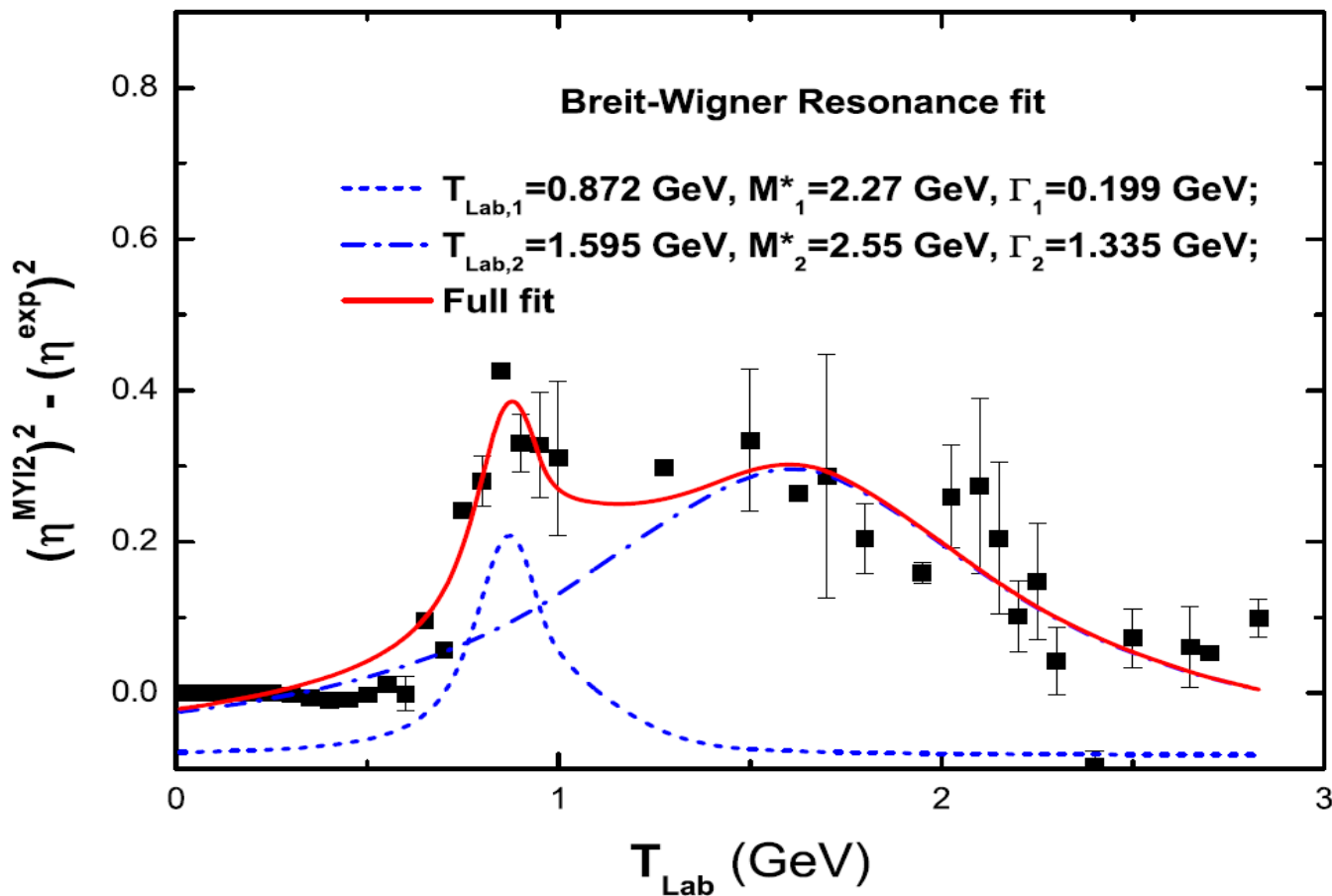
$$\Theta_p = 97^\circ$$

Covariant Bethe – Salpeter approach

S. G. Bondarenko et al Nucl Phys A 848, 75 (2010)

MY6 model

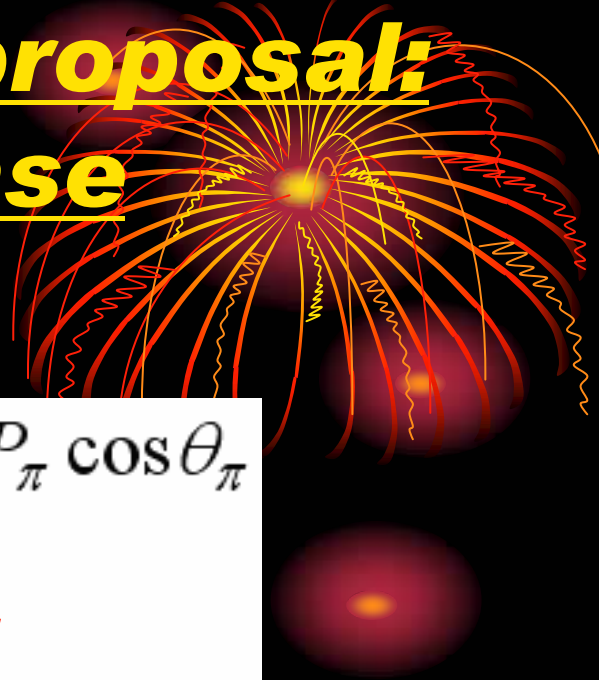
Experimental proposal



SG Bondarenko,
VV Burov,
EP Rogochaya
PL B705(2011)264

**Search for 2.27 and 2.55 GeV resonances
in CMM experiments**
 $p+p \rightarrow (\text{quasi}) \text{ dibaryon} + \pi$

The main experimental proposal: registration of chiral phase transition



$$M_{MB}^2 = (E - E_\pi + M_{SRC})^2 - P_\pi^2 - P^2 + 2PP_\pi \cos \theta_\pi$$

$$M_{MB} = f(M_{SRC})$$

$$M_{SRC} = f^{-1}(M_{MB})$$

CMM

**Either SRC or q-bag
model is true**



$$\theta_\pi = 119^\circ:$$

$$P_\pi = 1.008$$

$$\theta_\pi = 97^\circ:$$

$$P_\pi = 1.285$$

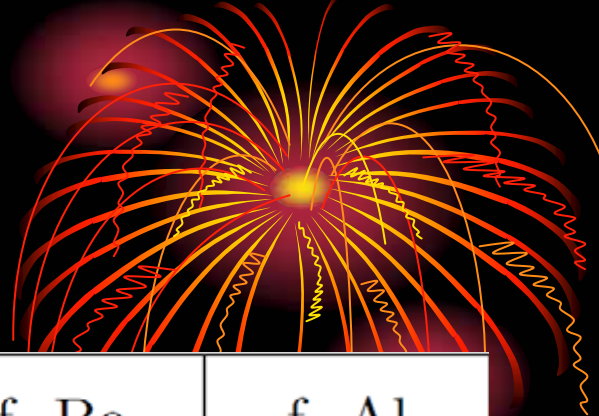
**Resolution is desirable to
be high**



$$M_3^* = 3.62, M_4^* = 4.76, M_5^* = 6.07$$

+ account for $E_{\pi,bind} \approx 0.025$

Feasibility



$P_{\pi}, /c$	f, Be	f, Al
0.873	$1.65 \cdot 10^{-4}$	$4.61 \cdot 10^{-4}$
0.979	$2.47 \cdot 10^{-5}$	$8.62 \cdot 10^{-5}$
1.077	$3.72 \cdot 10^{-6}$	$1.72 \cdot 10^{-5}$
1.293	$6.23 \cdot 10^{-8}$	$3.56 \cdot 10^{-7}$
1.402	$8.21 \cdot 10^{-9}$	$5.32 \cdot 10^{-8}$
1.512	$7.94 \cdot 10^{-10}$	$4.95 \cdot 10^{-9}$
1.619		$1.03 \cdot 10^{-9}$

$P_{\pi}, /c$	f, Be	f, Al
1.192	$1.95 \cdot 10^{-5}$	$7.09 \cdot 10^{-5}$
1.370	$1.20 \cdot 10^{-6}$	$6.34 \cdot 10^{-6}$
1.523	$9.36 \cdot 10^{-8}$	$6.37 \cdot 10^{-7}$
1.635	$1.40 \cdot 10^{-8}$	$1.26 \cdot 10^{-7}$
1.790	$1.21 \cdot 10^{-9}$	$1.42 \cdot 10^{-8}$

$\text{mb} \cdot \text{GeV}^{-2} \cdot \text{c}^3 \cdot \text{sr}^{-1} \cdot \text{nucleon}^{-1}$

S.V.Boyarinov et al., Yad. Fiz. 46,1472(1987); 57, 1452(1994)

Last experimental proposal



CMM may also be applied to double cumulative processes for search of heavy multibaryons

Cumulative π -meson may be replaced by cumulative K-meson to create strange MB