

Study of the reaction $np \rightarrow np\pi^+\pi^-$ at intermediate energies

A.P. Jerusalimov,

Yu.A.Troyan, A.Yu.Troyan, A.V.Belyaev, E.B.Plekhanov

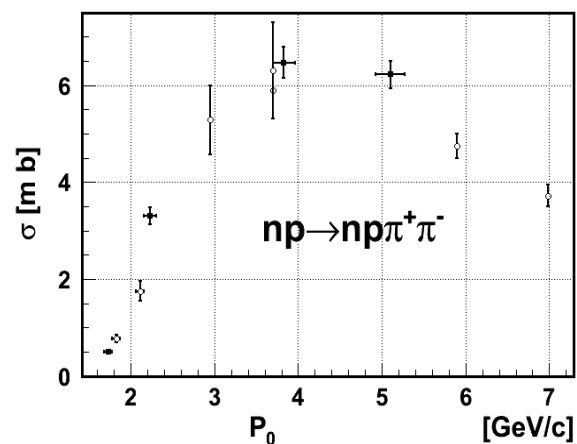
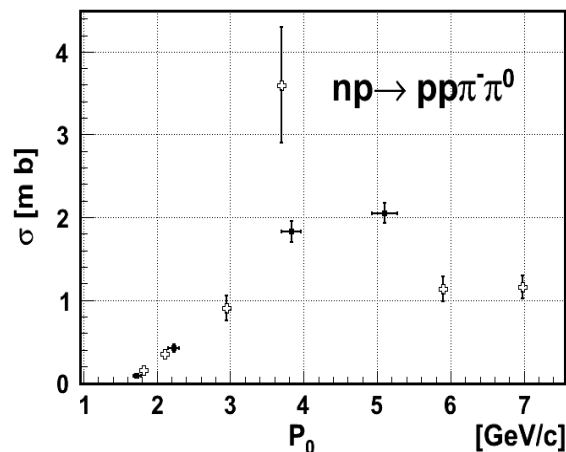
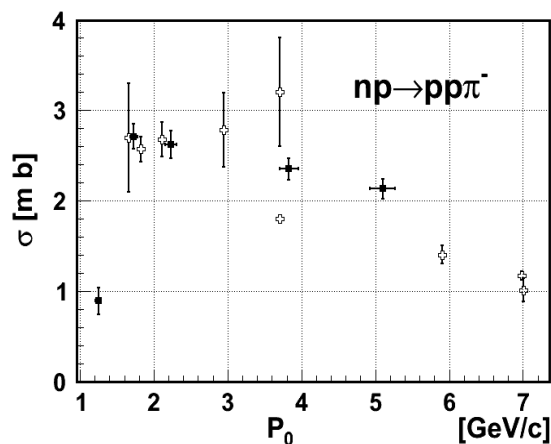
JINR-LHEP, Dubna

Outlook

1. Introduction
 2. The reaction $np \rightarrow np\pi^+\pi^-$ at $P_0 > 3$ GeV/c
 3. The reaction $p\bar{p} \rightarrow p\bar{p}\pi^+\pi^-$ at $P_0 = 7.23$ GeV/c
 4. The reaction $np \rightarrow np\pi^+\pi^-$ at $P_0 < 3$ GeV/c
 5. OPER model and other reactions
 6. Conclusion
- Appendix

1. Introduction: study of inelastic np interactions at accelerator facility of LHEP JINR

- Quasimonochromatic neutron channel: $\delta P \approx 2.5\%$, $P_0 = 1.25; 1.43; 1.73; 2.23; 3.10; 3.83; 4.10$ and 5.20 GeV/c, 4π geometry.
- Cross-sections of inelastic np interactions: (black circles – our data)



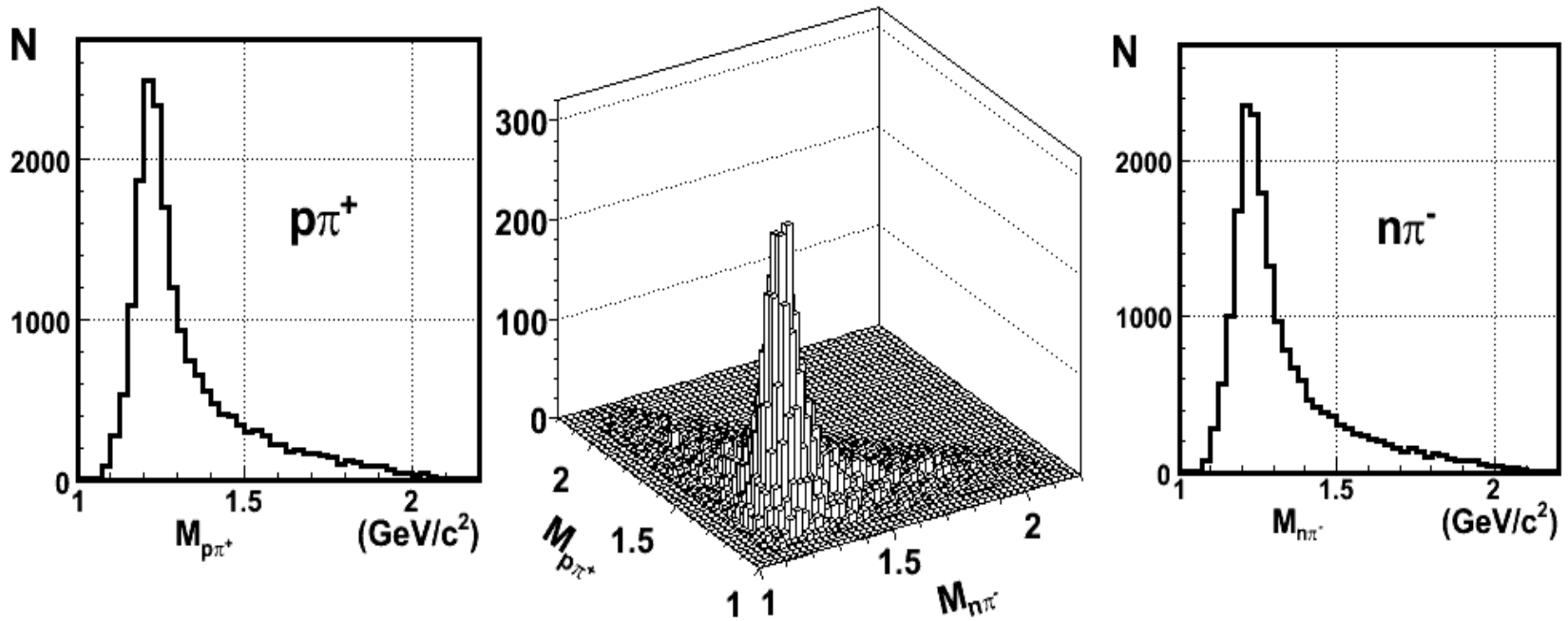
The unique of fullness and precision data are obtained.

It permits to carry out the detailed study of inelastic np interactions in a wide region of energies

2. Reaction $np \rightarrow n\rho\pi^+\pi^-$ at $P_0 > 3$ GeV/c

It is characterized by:

- plentiful production of the Δ resonance ,



- large peripherality of the secondary nucleons

To study the mechanism of the reaction it was chosen the model of **reggeized π -exchange (OPER)**, developed in ITEP
 [L.Ponomarev. Part. and Nucl., v.7(1), pp. 186-248, 1976, JINR, Dubna].

The advantages of OPER model are:

- **small number of free parameters (3 in our case),**
- **wide region of the described energies (2 ÷ 200 GeV),**
- **calculated values are automatically normalized to the reaction cross-section.**

The following main diagrams correspond to the reaction $np \rightarrow np\pi^+\pi^-$ within the framework of OPER model:

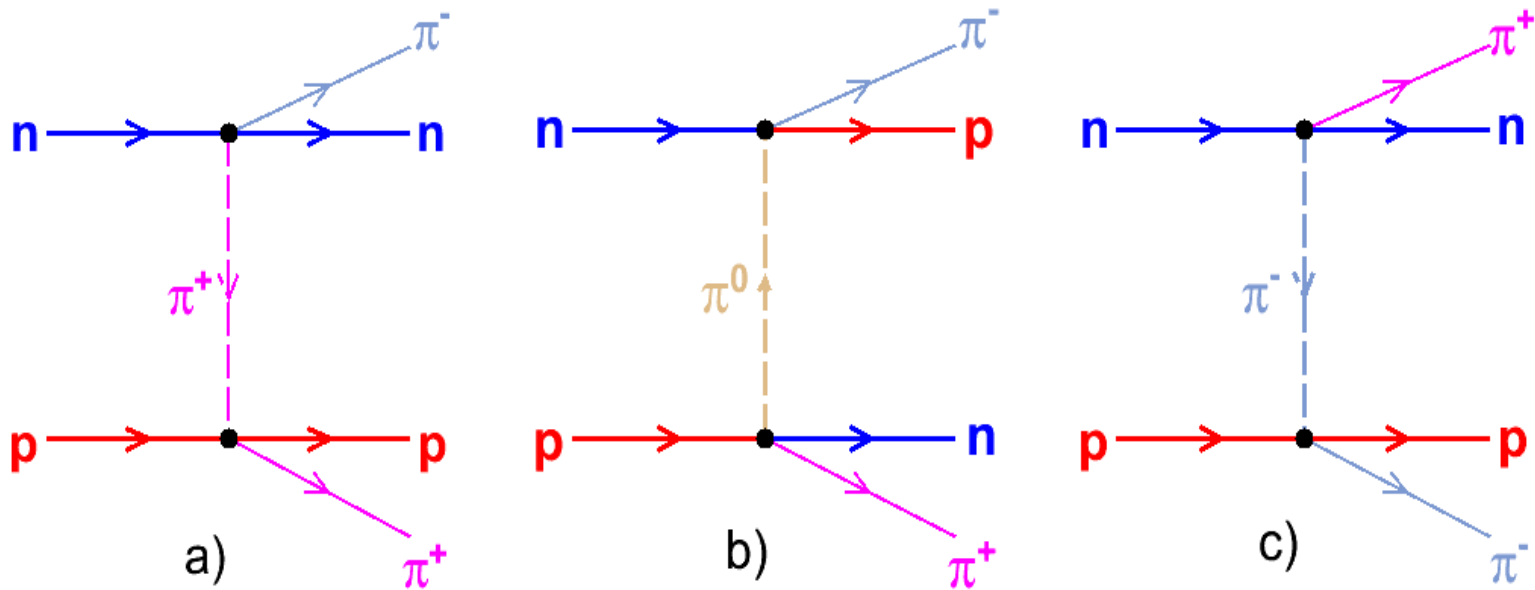


Fig.1

Matrix element for the diagrams 1a ,1b и 1c is written in the following form:

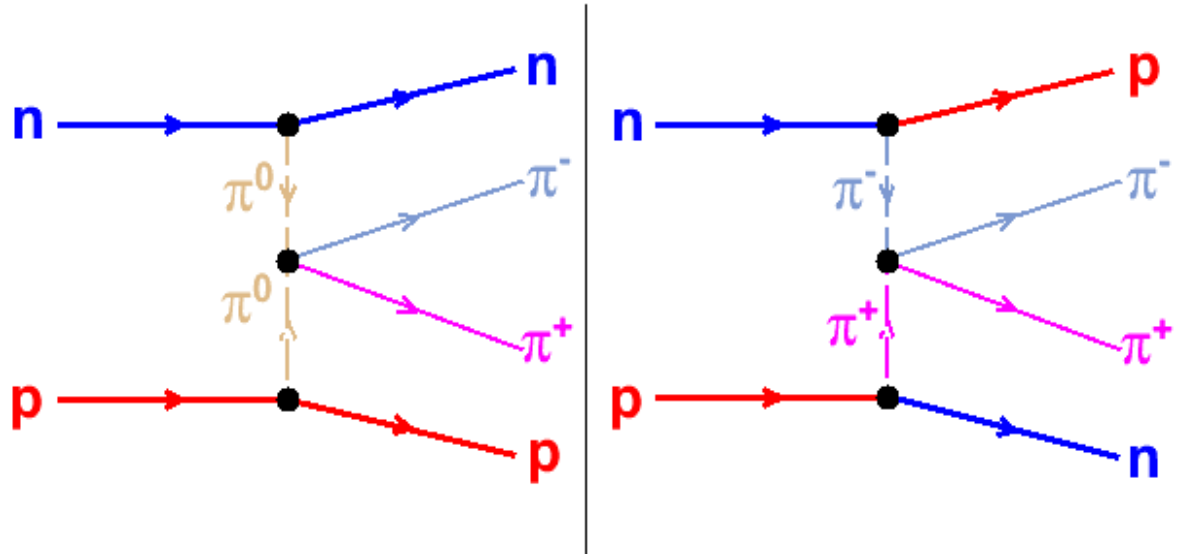
$$M_1 = T_{\pi N \rightarrow \pi N} \cdot F_2 \cdot T_{\pi N \rightarrow \pi N} / (t - m_\pi^2),$$

where $T_{\pi N \rightarrow \pi N}$ – amplitude of elastic $\pi N \rightarrow \pi N$ scattering off mass shell,
 F_2 – form-factor, going away off mass shell of $T_{\pi N \rightarrow \pi N}$ amplitudes,
 $1 / (t - m_\pi^2)$ – π -meson propagator.

The data of elastic $\pi N \rightarrow \pi N$ were taken from *PWA* [R.A. Arndt et al. *IJMP* **A18(3)**, 2003, p. 449]

The analysis shows, that interference between diagrams 1a ,1b и 1c is negligible
 [A.P. Jerusalimov et al. *JINR Rapid Communications*, v.35(2) pp.21-26, 1989, JINR, Dubna].

The study has shown that it is not necessary to take into account the contribution of the «hanged» diagrams into the reaction cross-sections at $P_0 < 10$ GeV/c



It was shown in [G.W. van Appeldorn et al, NP B156 (1979),pp. 110-125] that the use of some specific cuts permits to select the kinematic region of the reaction $np \rightarrow n\rho\pi^+\pi^-$ in which the contribution of the diagrams **1a**, **1b** и **1c** consists up to 95 % at $P_0 > 3$ GeV/c.

Fig.2 shows some distributions for the reaction $np \rightarrow n\rho\pi^+\pi^-$ for this region at $P_0 = 5.20$ GeV/c (blue curves – results of calculations using OPER model)

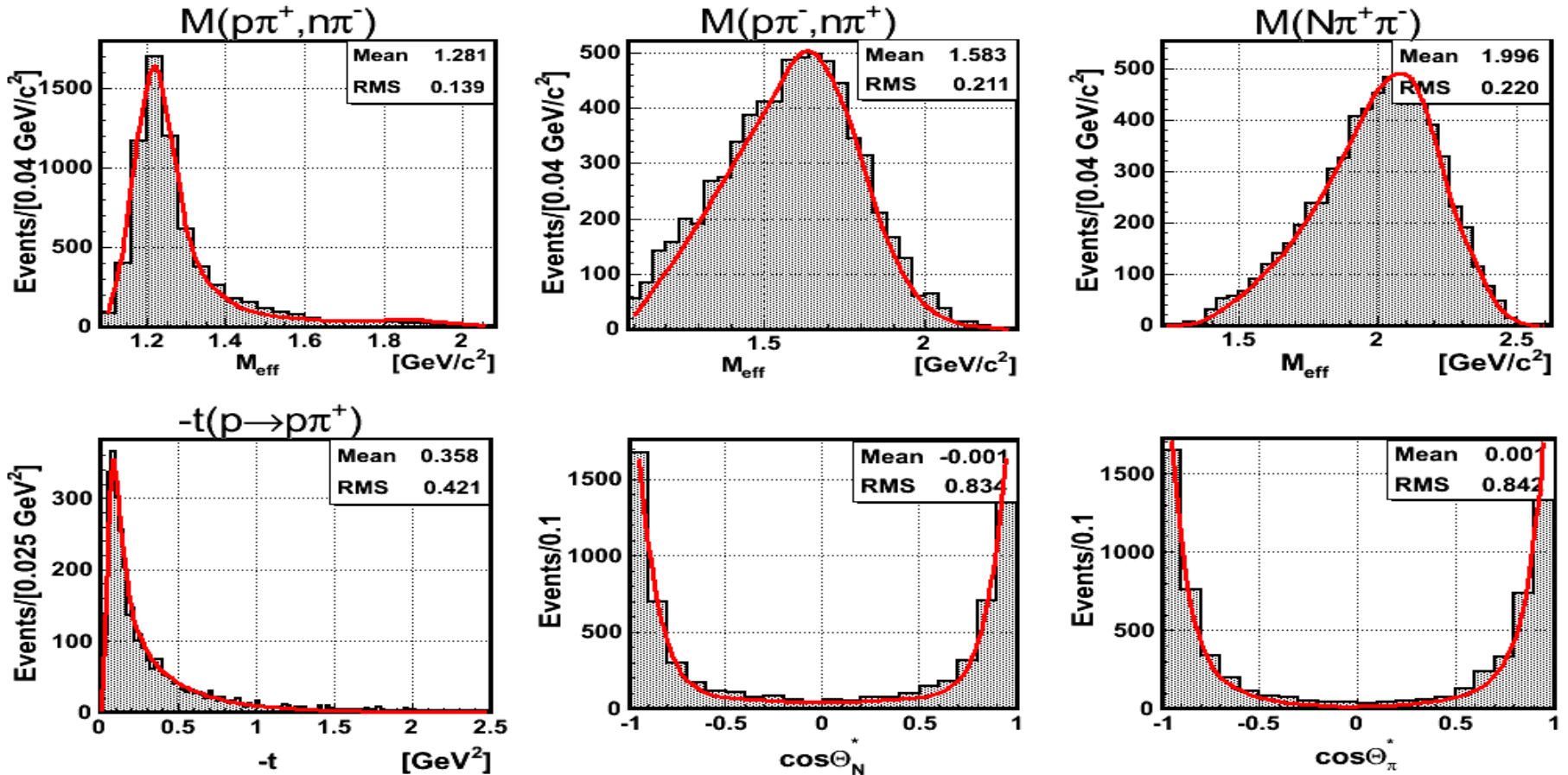


Fig. 2

But the diagrams shown in Fig.1 are insufficient to describe totally the characteristics of the reaction $n p \rightarrow n p \pi^+ \pi^-$. It is necessary to take into account the diagrams of the following type:

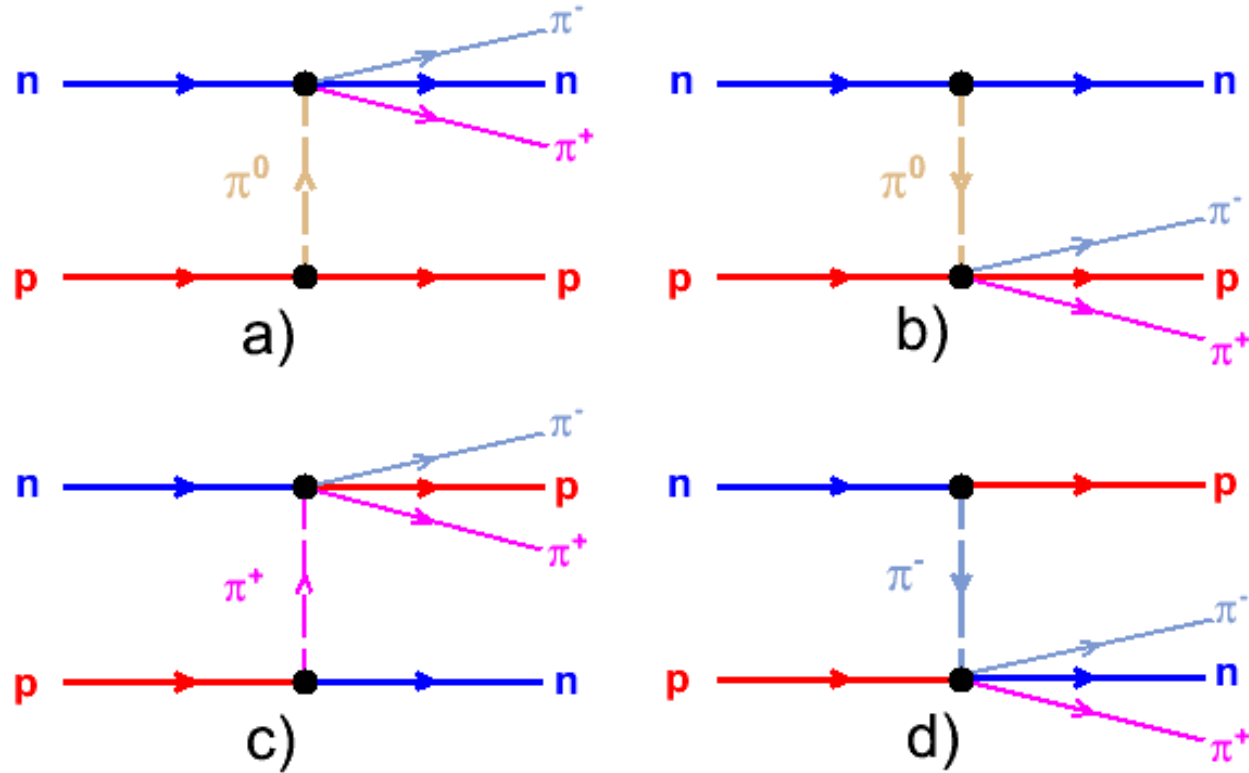


Fig. 3

the matrix element for which is written in the following form:

$$M_3 = G u(q_N) \gamma_5 u(Q_N) \cdot \mathbf{F}_1 \cdot T_{\pi N \rightarrow \pi \pi N} / (t - m_\pi^2),$$

where $T_{\pi N \rightarrow \pi \pi N}$ - off mass shell amplitudes of inelastic $\pi N \rightarrow \pi \pi N$ scattering that are known much worse than $T_{\pi N \rightarrow \pi N}$ amplitudes.

Therefore it is necessary to do a parametrization of the inelastic $\pi N \rightarrow \pi \pi N$ scattering (see [Appendix](#)).

It permits to get a good description of the experimental characteristics of the reaction $n p \rightarrow n p \pi^+ \pi^-$ at $P_0=5.20$ GeV/c (Fig. 5) taking into account OPER diagrams shown in Fig.1 and Fig.3 :

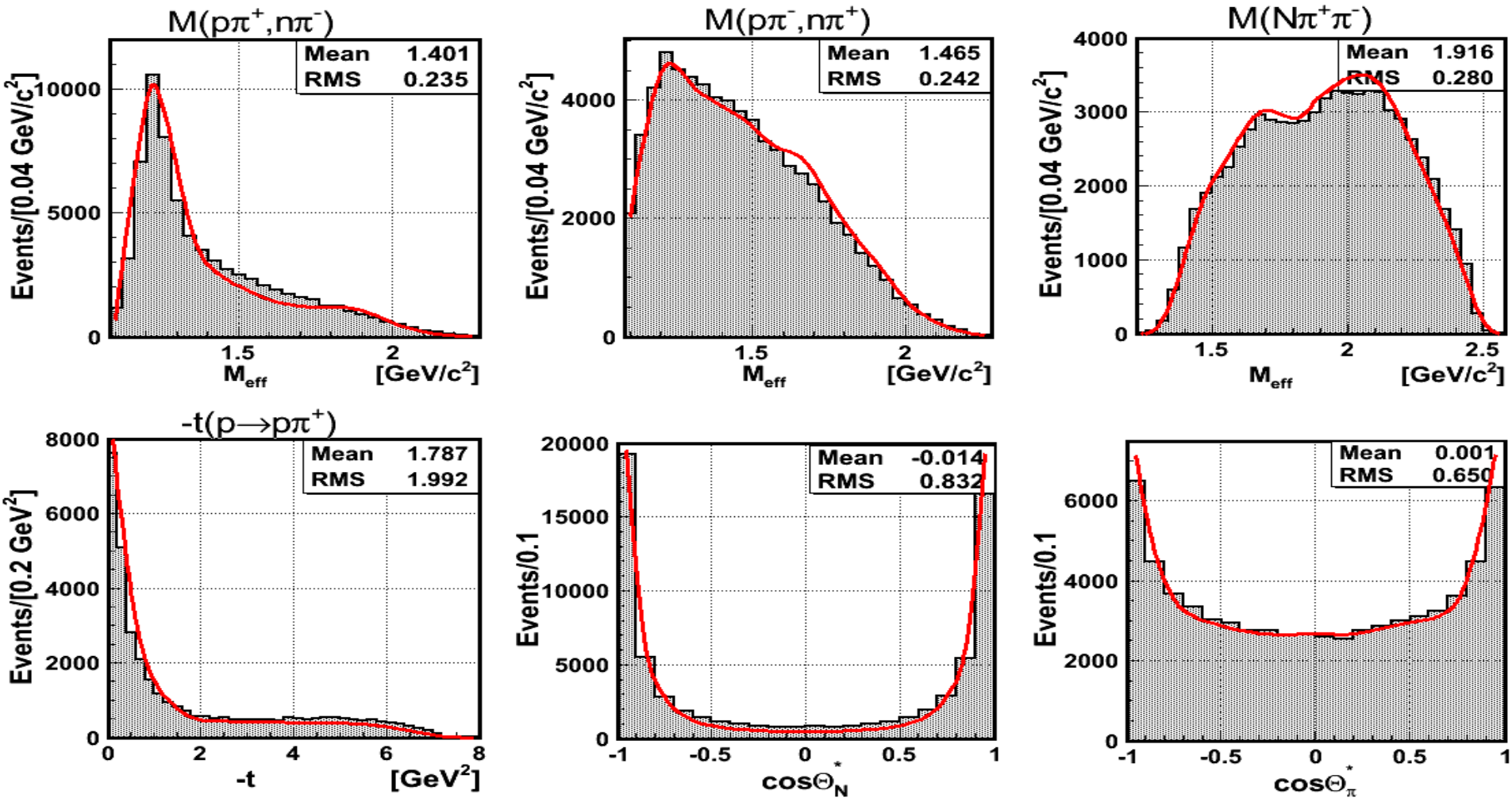
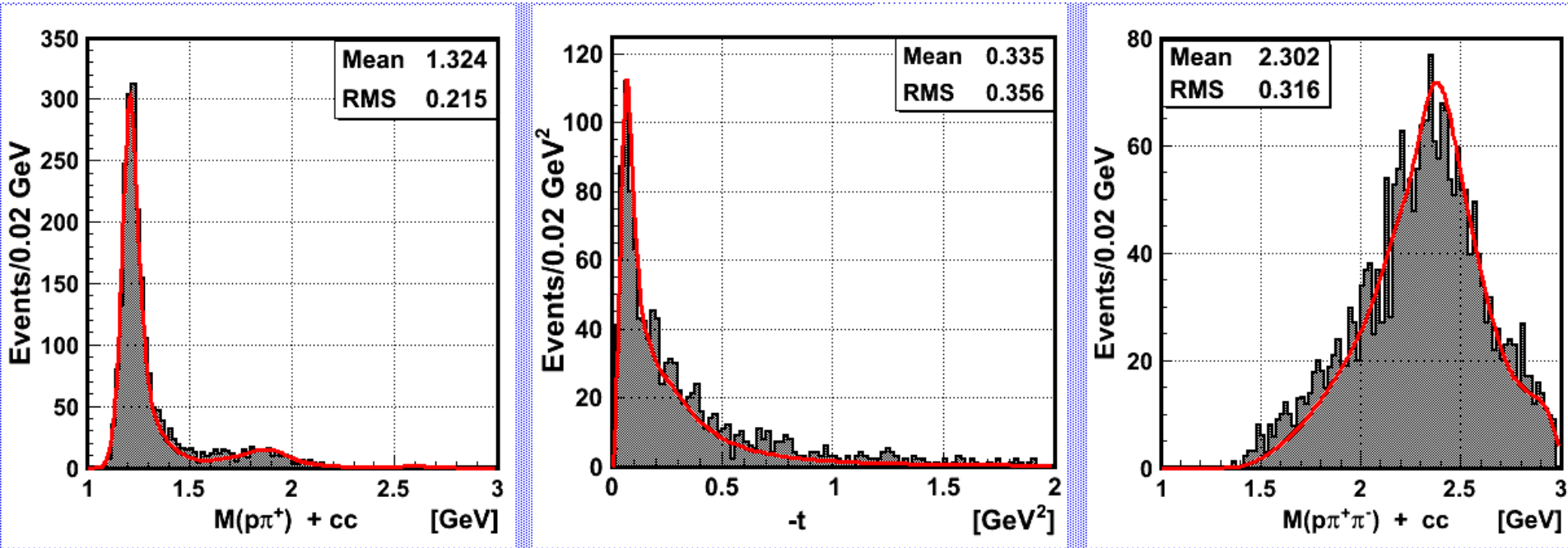


Fig. 4

3. Reaction $\bar{p} p \rightarrow \bar{p} p \pi^+ \pi^-$ at $P_0 = 7.23 \text{ GeV}/c$

Using OPER model we try to describe the experimental distributions from the reaction
 $\bar{p} p \rightarrow \bar{p} p \pi^+ \pi^-$ at $P_0 = 7.23 \text{ GeV}/c$

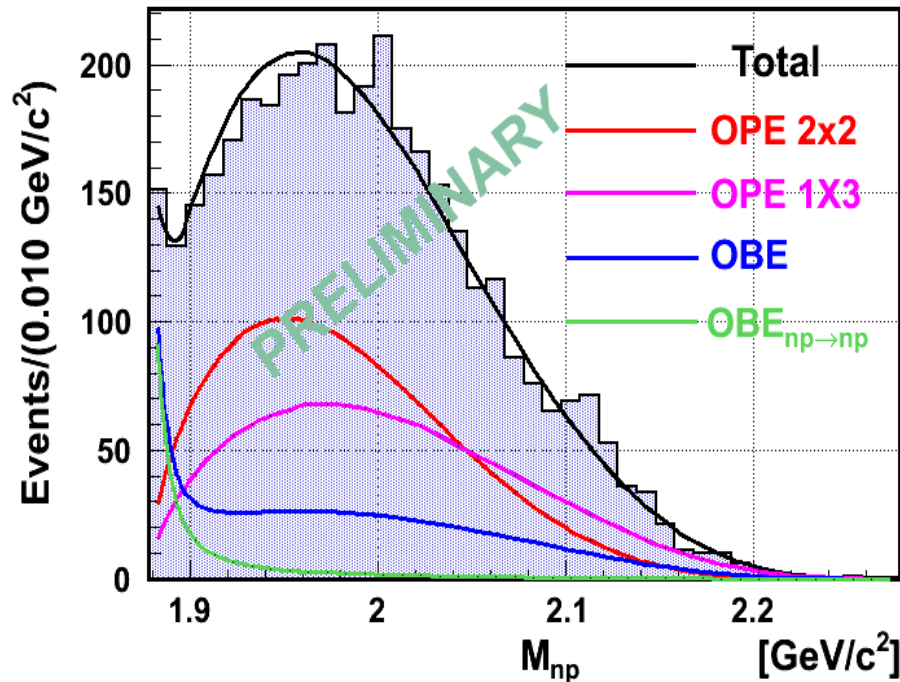
[G.W. van Appeldorn et al, NP B156 (1979), pp. 110-125]



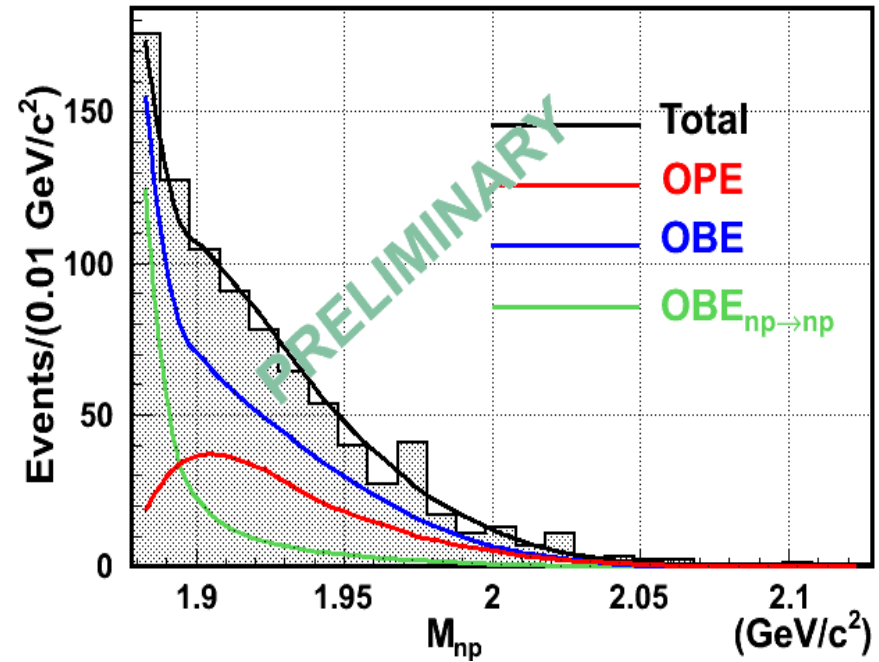
It is observed a good agreement between experimental data and theory.

4. Reaction $np \rightarrow n\pi^+ \pi^-$ at $P_0 < 3$ GeV/c

The study of effective mass spectra of np – combinations at $P_0=1.73$ and 2.23 GeV/c shows the clear peak close the threshold ($M_{np}=m_n+m_p$) that can not be described within the framework of OPER-model c using the diagrams 1a, 1b, 1c, 3a, 3b, 3c и 3d.



$P_0 = 2.23$ GeV/c



$P_0 = 1.73$ GeV/c

The model of Regge poles with baryon exchange and nonlinear trajectories, suggested in [A.B. Kaydalov and A.F. Nilov. *YaF*, v.41(3),pp. 768-776, 1985 ; *YaF*, v.52(6), pp. 1683-1696, 1990] was used to describe these features.

The following diagrams of one baryon exchange (OBE) were taken into account within the framework of this model:

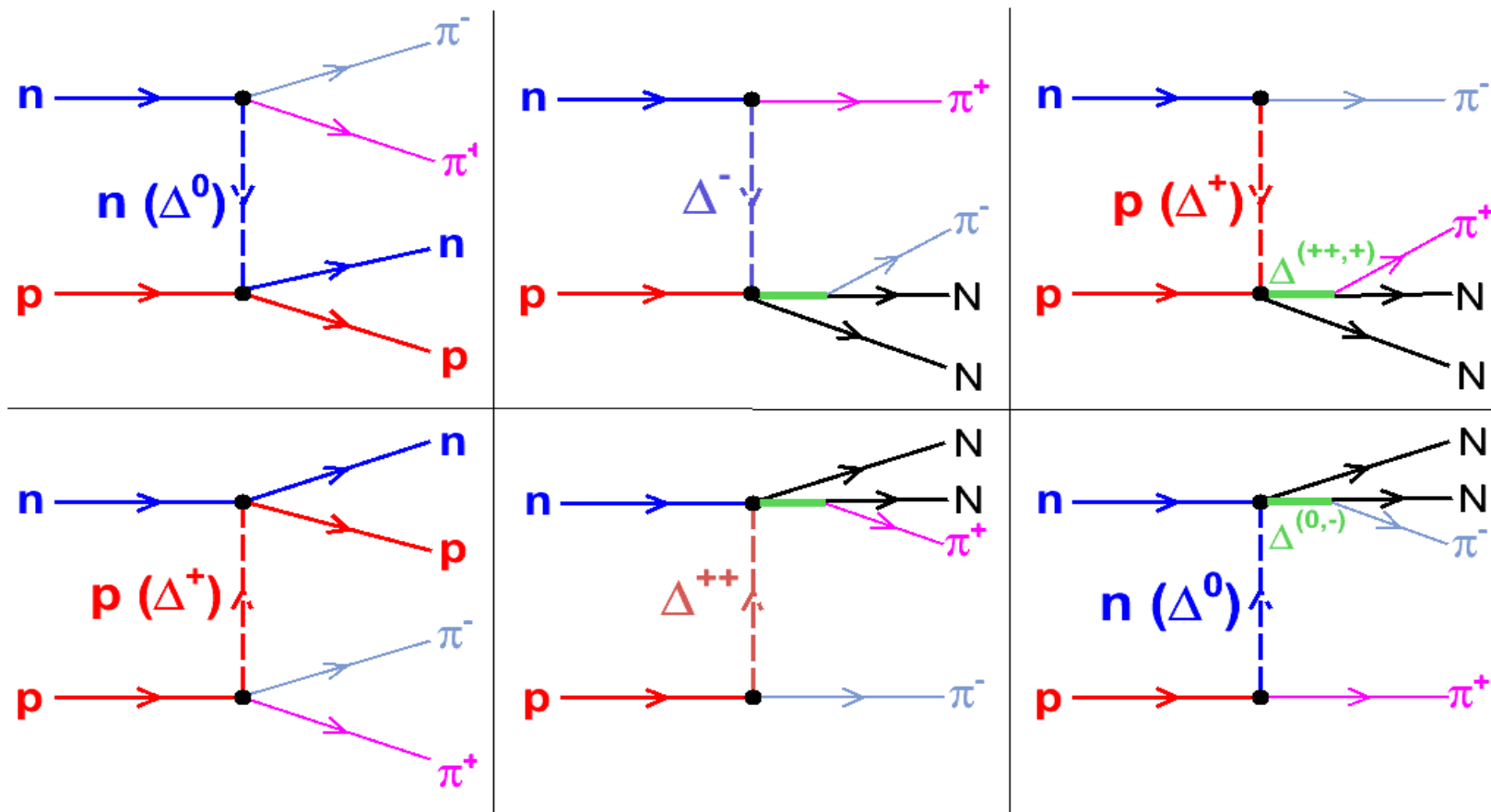
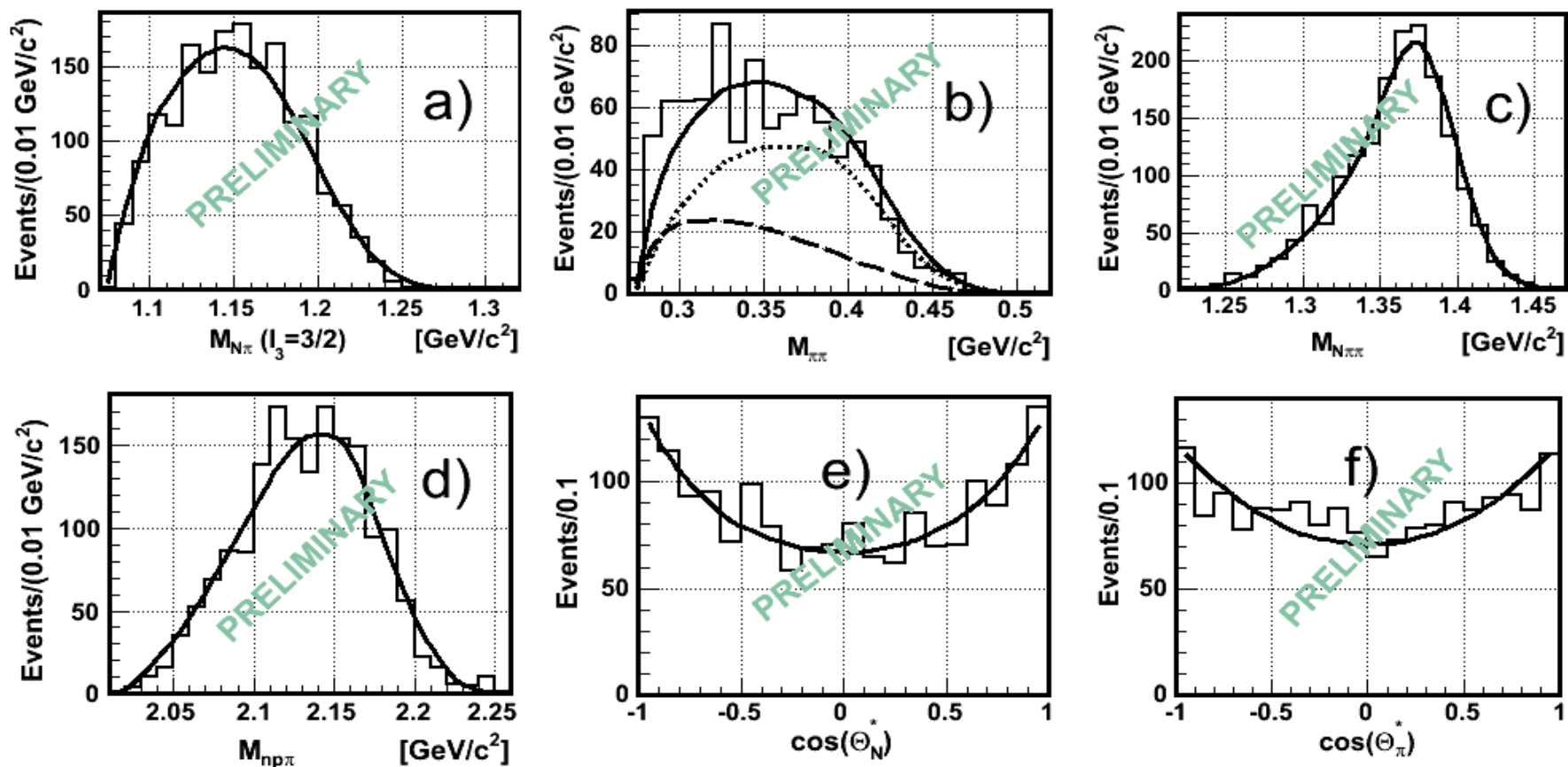


Fig. 6

The vertex function of elastic $\mathbf{np} \rightarrow \mathbf{np}$ scattering was calculated using the data from [NN and ND interactions – a compilation. UCRL-20000 NN, august 1970].

The vertex functions of $\Delta\mathbf{N} \rightarrow \mathbf{np}$, $\mathbf{NN} \rightarrow \Delta\mathbf{N}$ и $\Delta\mathbf{N} \rightarrow \Delta\mathbf{N}$ scattering were calculated corresponding to [В.С. Барашенков и Б.Ф. Костенко. 4-84-761, JINR, Dubna, 1984]. In result one can get the good description of the experimental distribution from the reaction $\mathbf{np} \rightarrow \mathbf{np}\pi^+\pi^-$ at $P_0=1.73$ and 2.23 GeV/c.



$P_0 = 1,73$ ГэВ/с

5. OPER model and other reactions

The other reactions of **np** interactions are scheduled to study by means of OPER model:

- **np** \rightarrow **pp** π^- vertex functions **1 x 2**
- **np** \rightarrow **pp** $\pi^- \pi^0$ vertex functions **2 x 2** and **1 x 3**
- **np** \rightarrow **pp** $\pi^+ \pi^- \pi^-$ vertex functions **2 x 3**
- **np** \rightarrow **pp** $\pi^+ \pi^- \pi^- \pi^0$ vertex functions **3 x 3**
- **np** \rightarrow **np** $\pi^+ \pi^+ \pi^- \pi^-$ vertex functions **3 x 3**

Similar reactions of **pp** -, **pbap** p - and **π N** - interactions also can be described by OPER model.

The following reactions were simulated for HADES experiment:

$$\mathbf{pp} \rightarrow \mathbf{pp} \pi^+ \pi^- \text{ at } T_{\text{kin}}=3.5 \text{ GeV}$$

$$\mathbf{np} \rightarrow \mathbf{np} \pi^+ \pi^- \text{ at } T_{\text{kin}}=1.25 \text{ GeV}$$

$$\mathbf{np} \rightarrow \mathbf{np} e^+ e^- \text{ at } T_{\text{kin}}=1.25 \text{ GeV} \quad \text{with vertex function of } \mathbf{\pi N} \rightarrow \mathbf{N} e^+ e^-$$

Since the **$\pi N \rightarrow \pi N$** and **$\pi N \rightarrow \pi \pi N$** vertex functions are taken in helicity representation it seems to be perspective to use OPER model for description of the reaction with polarized particles.

6. Conclusion

Reaction $np \rightarrow n p \pi^+ \pi^-$ at $\underline{P_0 > 3 \text{ GeV/c}}$ is characterized by the plentiful production of the Δ resonance and the large peripherality of the secondary particles. The experimental data are successfully described by the further development of OPER – model.

However at $\underline{P_0 < 3 \text{ GeV/c}}$ it is necessary to take into account another mechanism of the reaction (such as OBE).

OPER – model permits to describe another $N(\bar{N})\text{-}N$ reactions with the production of some π -mesons.

The further development of OPER – model can be very promising to describe the production of e^+e^- -pairs in hadronic interactions.

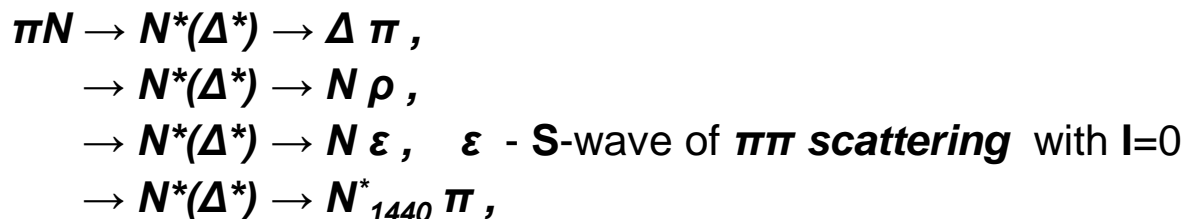
OPER – model can be used as an effective tool to simulate various reactions of hadronic interactions.

Appendix: Parametrization of $\pi N \rightarrow \pi \pi N$ reactions

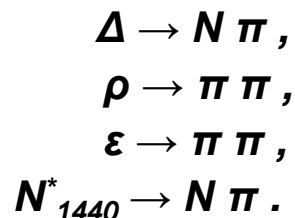
Within the framework of **Generalized Isobar Model (GIM)**

[D.J. Herndon et al. PR D11, 3165 (1975); D.M.Manley and E.M. Saleski, PR D45, 4002 (1992)]

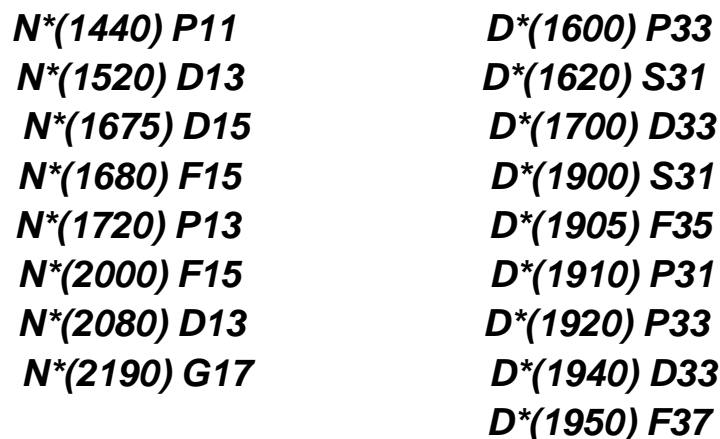
$\pi N \rightarrow \pi \pi N$ reactions are described as quasi-two body ones:



with the consequent
decays :



The parameters
of the following
resonances
(**** and ***)
were taken
from **RPP**



The spin and
isospin relations
were taken
account

For quasi two-body reactions like $\mathbf{a} + \mathbf{b} \rightarrow \mathbf{c} + \mathbf{d}$

$$\begin{aligned} \pi N &\rightarrow N^*(\Delta^*) \rightarrow \Delta \pi, \\ &\rightarrow N^*(\Delta^*) \rightarrow N \rho, \\ &\rightarrow N^*(\Delta^*) \rightarrow N \varepsilon, \\ &\rightarrow N^*(\Delta^*) \rightarrow N_{1440}^* \pi, \end{aligned}$$

one can write

$$d\sigma = \frac{1}{(2S_a + 1)(2S_b + 1)} \left(\frac{2\pi}{p} \right)^2 \sum_{\lambda_i} |\langle \lambda_d \lambda_c | T | \lambda_b \lambda_a \rangle|^2 \times dPS$$

where

$$\langle \lambda_d \lambda_c | T | \lambda_b \lambda_a \rangle = \frac{1}{4\pi} \sum_j (2j + 1) \langle \lambda_d \lambda_c | T_j | \lambda_b \lambda_a \rangle e^{i(\lambda - \mu)\varphi} d_{\lambda\mu}^j(\vartheta)$$

$\lambda = \lambda_a - \lambda_b$, $\mu = \lambda_c - \lambda_d$ – helicity variables, $d_{\lambda\mu}^j(\vartheta)$ – rotation matrixes.

The polarization components of the particles \mathbf{c} and \mathbf{d} from the reaction $\mathbf{a} + \mathbf{b} \rightarrow \mathbf{c} + \mathbf{d}$ is suitable to express through the elements of the spin density matrix (for example, for particle \mathbf{d}):

$$\rho_{mm'}^d = \frac{1}{N} \sum_{\lambda_c \lambda_b \lambda_a} \langle m' \lambda_c | T | \lambda_b \lambda_a \rangle^* \langle m \lambda_c | T | \lambda_b \lambda_a \rangle$$

where

$$N = \sum_{m \lambda_c \lambda_b \lambda_a} |\langle m \lambda_c | T | \lambda_b \lambda_a \rangle|^2$$

normalization factor for $\text{Sp}\rho=1$.

Example:

$$\pi + N \rightarrow N^*_{1680} \rightarrow \Delta + \pi \rightarrow (N + \pi) + \pi$$

$$\langle \lambda_{\Delta} | T | \lambda_N \rangle = C_{3,0;\frac{1}{2},-\lambda_{\Delta}}^{\frac{5}{2},-\lambda_N} C_{1,0;\frac{3}{2},-\lambda_{\Delta}}^{\frac{5}{2},-\lambda_{\Delta}} d_{-\lambda_N,\lambda_{\Delta}}^{\frac{5}{2}}(\vartheta) \times R_J$$

R_J is taken in Breit-Wigner form

Then it is easy to get the angular distribution of Δ (in CMS):

$$\frac{d\sigma(s, t)}{d\Omega} \sim (1 + 2\cos^2\vartheta_{\Delta}) |R_J|^2 = (1 + 2\cos^2\vartheta_{\Delta}) BW(\sqrt{s}, M_R, \Gamma_R)$$

If particle \mathbf{d} is unstable: $\mathbf{d} \rightarrow \alpha + \beta$ ($\mathbf{d} \rightarrow \Delta + \pi$)

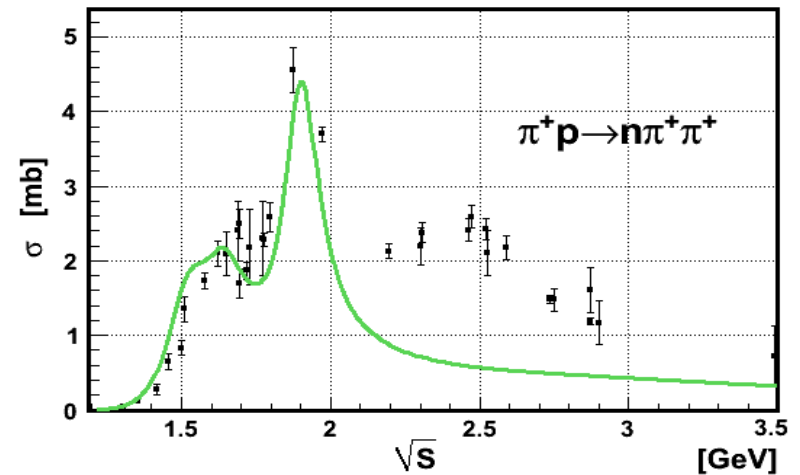
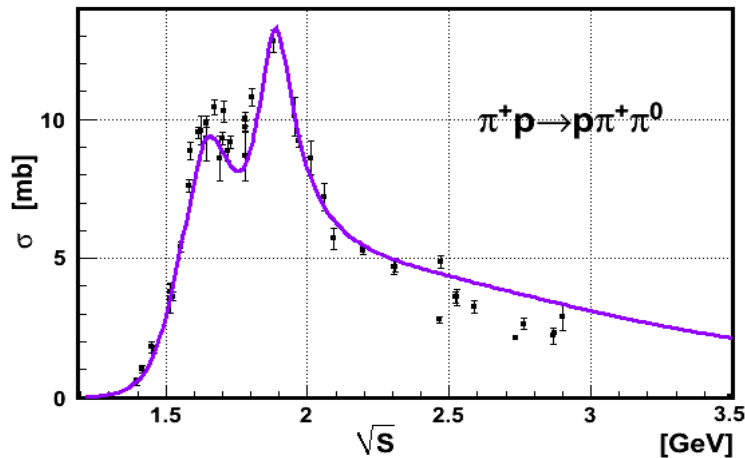
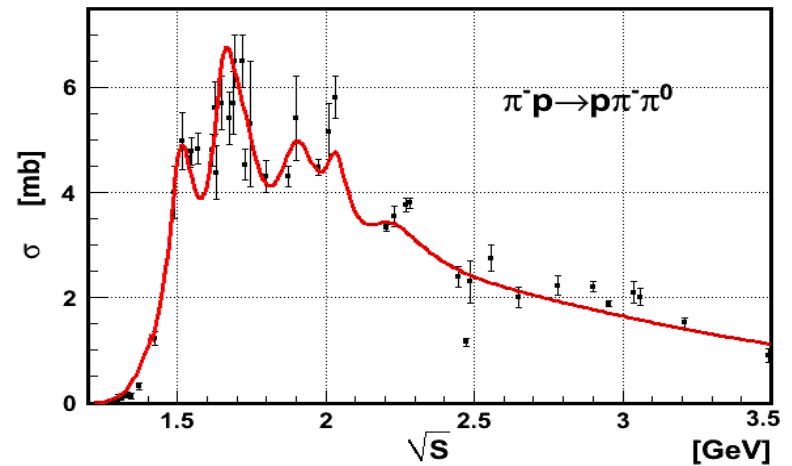
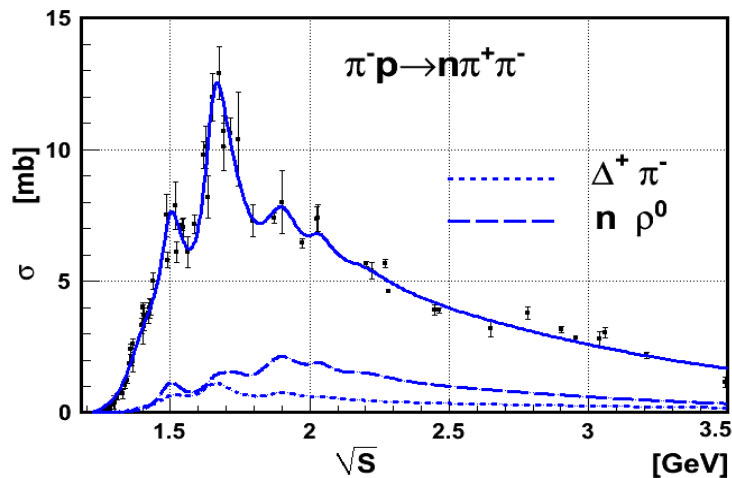
then in the rest system of the particle \mathbf{d} ($\mathbf{d} \rightarrow \Delta + \pi$)

$$W_{\Delta}(\vartheta, \varphi) = \frac{3}{4\pi} \left\{ \rho_{33} \sin^2 \vartheta + \frac{1}{3} \rho_{11} (1 + 3 \cos^2 \vartheta) - \frac{2}{\sqrt{3}} \text{Re} \rho_{3-1} \sin^2 \vartheta \cos 2\varphi - \frac{2}{\sqrt{3}} \text{Re} \rho_{31} \sin 2\vartheta \cos \varphi \right\}$$

is the normalized angular distribution of the decay products.

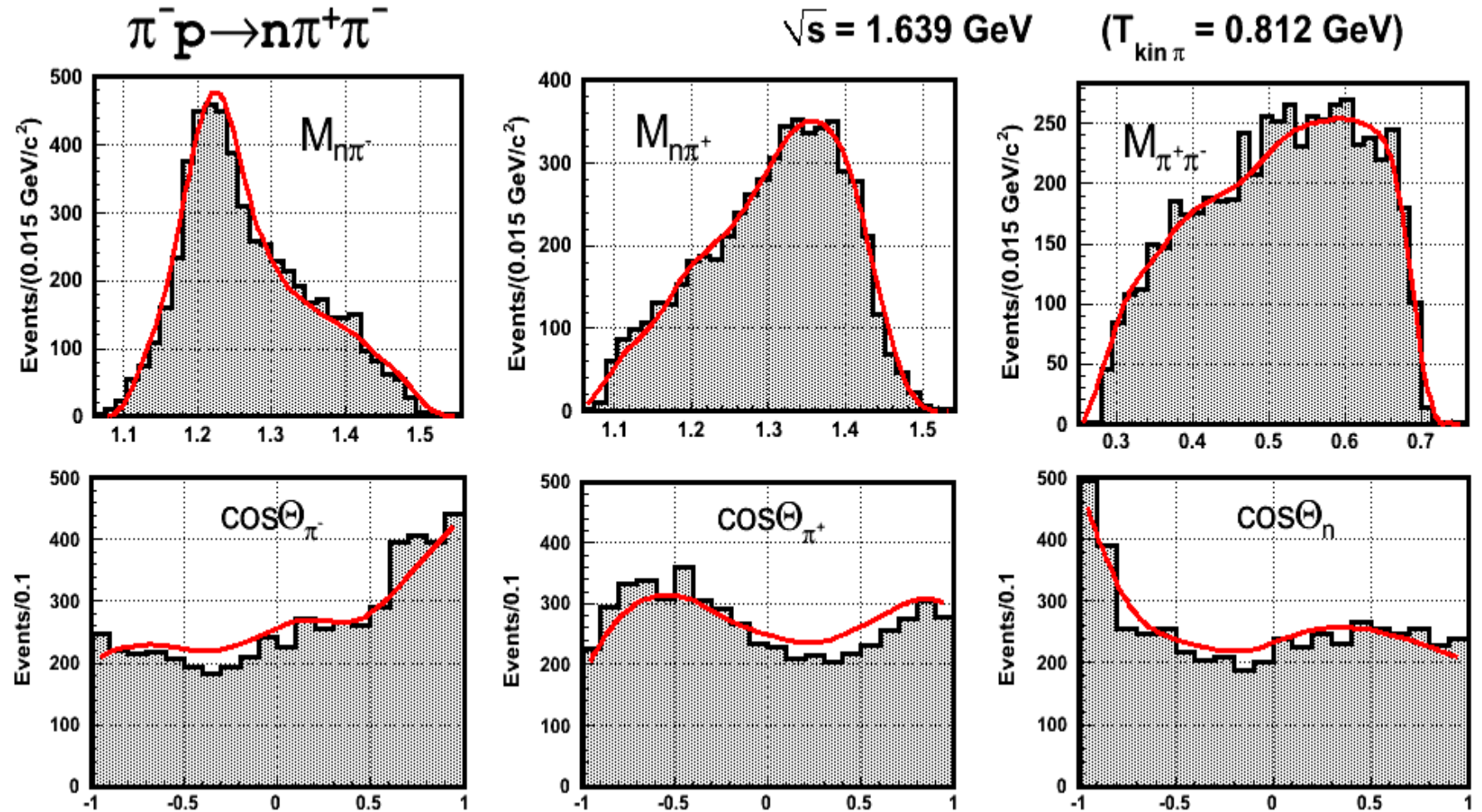
Comparison with experimental data

The following cross-sections were calculated using **GIM** :



One can see a satisfactory description of cross-sections, except $\pi^+ p \rightarrow n \pi^+ \pi^+$
Maybe it is necessary to put into **GIM** S-wave of $\pi^+ \pi^+$ scattering with $l=2$.

Some distributions of the reaction $\pi^- p \rightarrow n \pi^+ \pi^-$ were calculated at various energies to study a quality of the application of GIM :



[J. Dolbeau et al. NP B78, 233(1974)]

It is observed a good agreement between experimental data and theory.