

EXTENDED SIEGERT THEOREM IN THE RELATIVISTIC INVESTIGATION OF THE DEUTERON PHOTODISINTEGRATION REACTION

S.B.¹, V. Burov¹, K. Kazakov² and D. Shulga²

(1) *BLTP, Joint Institute for Nuclear Research, Dubna, Russia*

(2) *LTNP, Far Eastern National University, Vladivostok, Russia*

XIX Baldin ISHEPP, October 2, 2008, Dubna

Photodisintegration of the deuteron - motivation:

- breakup reaction, includes effects of the bound state (deuteron), continuum states (np -pair)
- real photon - $q^2 = 0$, investigation of the off-shell behavior of nucleon form factors

Investigations of the deuteron photodisintegration:

- plane-wave relativistic impulse approximation
(K.Yu. Kazakov, S.Eh. Shirmovsky, Phys.Rev.C63:014002,2001)
- effects of negative energy components in deuteron
(K.Yu. Kazakov, D.V. Shulga, Phys.Rev.C65:064002,2002)
- relativistic contribution of the final state interaction
(S.G. Bondarenko, V.V. Burov, K.Yu. Kazakov, D.V. Shulga, Phys.Part.Nucl.Lett.1:178-185,2004)
- effects of the two-particle current by using Siegert theorem
(S.G. Bondarenko, V.V. Burov, K.Yu. Kazakov, D.V. Shulga, *in preparation*)

Let us consider the charge and current operators as a sum of n -particle operators:

$$\hat{\rho} = \sum_{n \geq 1} \hat{\rho}_{[n]}, \quad \hat{\mathbf{j}} = \sum_{n \geq 1} \hat{\mathbf{j}}_{[n]},$$

Using the equation of current conservation in a form

$$\nabla \cdot \hat{\mathbf{j}} + i[\hat{H}, \hat{\rho}] = 0,$$

one obtains the following decomposition on the n -particle operators

$$\nabla \cdot \hat{\mathbf{j}}_{[1]} + i \left[\hat{T}_{[1]}, \hat{\rho}_{[1]} \right] \quad (n = 1)$$

$$+ \nabla \cdot \hat{\mathbf{j}}_{[2]} + i \left[\hat{T}_{[1]}, \hat{\rho}_{[2]} \right] + i \left[\hat{V}_{[2]}, \hat{\rho}_{[1]} \right] \quad (n = 2)$$

+ ...

Applying the Siegert *ansatz* for the two-body system

$$\hat{\rho}_{[2]} = 0$$

one obtain

$$\nabla \cdot \left(\hat{\mathbf{j}}_{[1]} + \hat{\mathbf{j}}_{[2]} \right) + i \left[\hat{T}_{[1]}, \hat{\rho}_{[1]} \right] + i \left[\hat{V}_{[2]}, \hat{\rho}_{[1]} \right] = 0$$

After the Fourier transformation and some algebra the equation

$$\nabla \cdot \hat{\mathbf{j}} + i [\hat{H}, \hat{\rho}_{[1]}] = 0$$

can be rewritten in a limit $\mathbf{q} \rightarrow 0$ as original Siegert theorem

$$\hat{\mathbf{j}}(\mathbf{q} = 0) = i[\hat{H}, \hat{\mathbf{D}}] = \dot{\hat{\mathbf{D}}}$$

with electric dipole moment

$$\mathbf{D} = \sum e_i \mathbf{x}_i.$$

The transversal components are not included into consideration.

To take into account the transversal components of the current, one need to use the following expression

$$(1 + \mathbf{q} \cdot \nabla_{\mathbf{q}}) \hat{\mathbf{j}}(\mathbf{q}) = -i \nabla_{\mathbf{q}} \hat{\rho}(\mathbf{q}) - 2i \mathbf{q} \times \hat{\boldsymbol{\mu}}(\mathbf{q}).$$

After applying some algebra one can obtain for the current operator

$$\hat{\mathbf{j}}(\mathbf{q}) = \hat{\mathbf{j}}_C(\mathbf{q}) + \hat{\mathbf{j}}_M(\mathbf{q}),$$

where the generalized electric dipole and magnetic moments are introduced

$$\hat{\mathbf{j}}_C(\mathbf{q}) = i[\hat{H}, \hat{\mathbf{D}}(\mathbf{q})] \qquad \hat{\mathbf{j}}_M(\mathbf{q}) = -i \mathbf{q} \times \hat{\mathbf{M}}(\mathbf{q})$$

$$\hat{\mathbf{D}}(\mathbf{q}) = -i \int_0^1 \frac{d\lambda}{\lambda} \nabla_{\mathbf{q}} \hat{\rho}_{(1)}(\lambda \mathbf{q}) \qquad \hat{\mathbf{M}}(\mathbf{q}) = -i \int_0^1 d\lambda \nabla_{\mathbf{q}} \times \hat{\mathbf{j}}_{(1)}(\lambda \mathbf{q})$$

This is the extended Siegert theorem.

To find expression for the amplitude of the deuteron photodisintegration

$$\langle \mathbf{P}_f, f | \hat{S} | \mathbf{P}_i, i \rangle = \hat{A}^\mu(P_f - P_i) \langle \mathbf{P}_f, f | \hat{j}^\mu(\mathbf{0}) | \mathbf{P}_i, i \rangle,$$

with

$$\hat{A}^\mu(P_f - P_i) = \int d^4x e^{i(P_f - P_i) \cdot x} \hat{A}^\mu(x)$$

Using Foldy identity for the Fourier transformed expressions

$$\int d^3R e^{i\mathbf{K}\mathbf{R}} \mathbf{j}(\mathbf{R}) =$$
$$- \int d^3R \int_0^1 d\lambda [e^{i\lambda\mathbf{K}\mathbf{R}} \mathbf{R} (\nabla \cdot \mathbf{j}(\mathbf{R})) + i\lambda e^{i\lambda\mathbf{K}\mathbf{R}} \mathbf{K} \times (\mathbf{R} \times \mathbf{j}(\mathbf{R}))],$$

the amplitude becomes

$$\langle \mathbf{P}_f, f | \hat{S} | \mathbf{P}_i, i \rangle = (2\pi)^4 \delta^{(4)}(P_f - P_i - q) T_{fi}$$

with

$$T_{fi} = -\langle 0_\gamma | \hat{\mathbf{E}}(0) | 1_\gamma^q \rangle \cdot \mathbf{D}_{fi}(\mathbf{K}) - \langle 0_\gamma | \hat{\mathbf{H}}(0) | 1_\gamma^q \rangle \times \mathbf{M}_{fi}(\mathbf{K}),$$

and photon matrix elements

$$\langle 0_\gamma | \hat{\mathbf{E}}(0) | 1_\gamma^q \rangle = \frac{i}{\sqrt{2E_\gamma}} (E_\gamma \boldsymbol{\varepsilon} - \mathbf{q} \varepsilon_0),$$

$$\langle 0_\gamma | \hat{\mathbf{H}}(0) | 1_\gamma^q \rangle = \frac{i}{\sqrt{2E_\gamma}} \mathbf{q} \times \boldsymbol{\varepsilon}.$$

The generalized electric dipole and magnetic moments are introduced in terms of matrix elements of 1-particle current

$$\hat{\mathbf{D}}(\mathbf{q}) = -i \int_0^1 \frac{d\lambda}{\lambda} \nabla_{\mathbf{q}} \langle \mathbf{P}_i + \lambda \mathbf{q}, f | \hat{\rho}_{(1)}(0) | \mathbf{P}_i, i \rangle,$$

$$\hat{\mathbf{M}}(\mathbf{q}) = -i \int_0^1 d\lambda \nabla_{\mathbf{q}} \times \langle \mathbf{P}_i + \lambda \mathbf{q}, f | \hat{\mathbf{j}}_{(1)}(0) | \mathbf{P}_i, i \rangle.$$

Finally

$$T_{fi} = \frac{-1}{\sqrt{2E_\gamma}} \left[E_\gamma \int_0^1 \frac{d\lambda}{\lambda} (\boldsymbol{\varepsilon} \cdot \nabla_{\mathbf{q}}) \rho_{(1)}(\lambda \mathbf{q}) + \int_0^1 d\lambda (\mathbf{q} \times \boldsymbol{\varepsilon}) \cdot (\nabla_{\mathbf{q}} \times \mathbf{j}_{(1)}(\lambda \mathbf{q})) \right]$$

$$\begin{aligned}
j_{\mu}^{(1)}(\mathbf{q}) &= \langle \mathbf{K} + \lambda \mathbf{q}, f | \hat{j}_{\mu}(0) | \mathbf{K}, i \rangle = \\
&= Sp \left\{ \bar{\chi}_{S m_S}^{(0)}(\mathbf{p}) \Gamma_{\mu}^{(1)}(q_{\lambda}) \Lambda_{\lambda \mathbf{q}} G^{(1)} \left(\mathcal{L}_{\lambda \mathbf{q}}^{-1} \left(\frac{K - q_{\lambda}}{2} + p \right) \right) \right. \\
&\quad \left. \Gamma_{m_d} \left(\mathcal{L}_{\lambda \mathbf{q}}^{-1} \left(p - \frac{q_{\lambda}}{2} \right); K^{(0)} \right) \Lambda_{\lambda \mathbf{q}}^{-1} \right\} \\
&+ (-1)^{I+1} Sp \left\{ \bar{\chi}_{S m_S}^{(0)}(-\mathbf{p}) \Gamma_{\mu}^{(2)}(q_{\lambda}) \Lambda_{\lambda \mathbf{q}} G^{(2)} \left(\mathcal{L}_{\lambda \mathbf{q}}^{-1} \left(\frac{K - q_{\lambda}}{2} - p \right) \right) \right. \\
&\quad \left. \Gamma_{m_d} \left(\mathcal{L}_{\lambda \mathbf{q}}^{-1} \left(-p - \frac{q_{\lambda}}{2} \right); K^{(0)} \right) \Lambda_{\lambda \mathbf{q}}^{-1} \right\}
\end{aligned}$$

Here $\mathcal{L}_{\mathbf{q}}^{\pm 1}$ corresponds to Lorentz transformation from the center of mass system to the laboratory system:

$$k_0 = \frac{1}{M_d} (E_d k'_0 \mp \mathbf{q} \cdot \mathbf{k}') \quad \mathbf{k} = \mathbf{k}' + \frac{\mathbf{q}}{M_d} \left(\frac{\mathbf{q} \cdot \mathbf{k}'}{M_d + E_d} \mp k'_0 \right),$$

and BS vertex functions for the deuteron are transformed as

$$\Lambda^{\pm 1} = \sqrt{\frac{E_d + M_d}{2M_d}} \left(1 \mp \frac{\gamma^0 \boldsymbol{\gamma} \cdot \mathbf{q}}{E_d + M_d} \right)$$

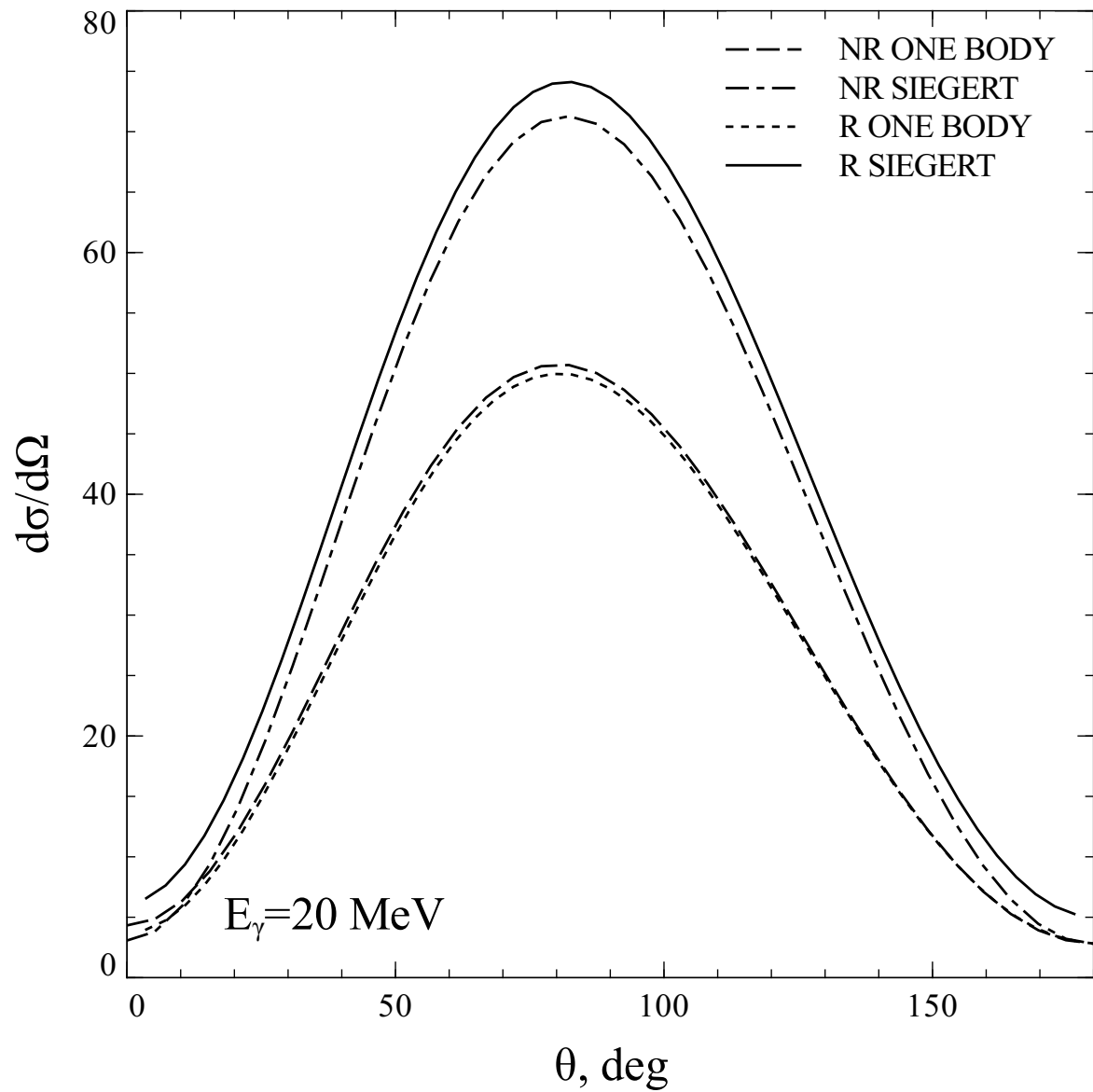
BS amplitude for the np -pair

$$\chi_{Sm_s}^{(0)}(p_f, P_{f(0)}) = \sum_{m_1 m_2} C_{\frac{1}{2}m_1 \frac{1}{2}m_2}^{Sm_s} u_{m_1}^{(1)}(\hat{\mathbf{p}}) u_{m_2}^{(2)}(-\hat{\mathbf{p}}).$$

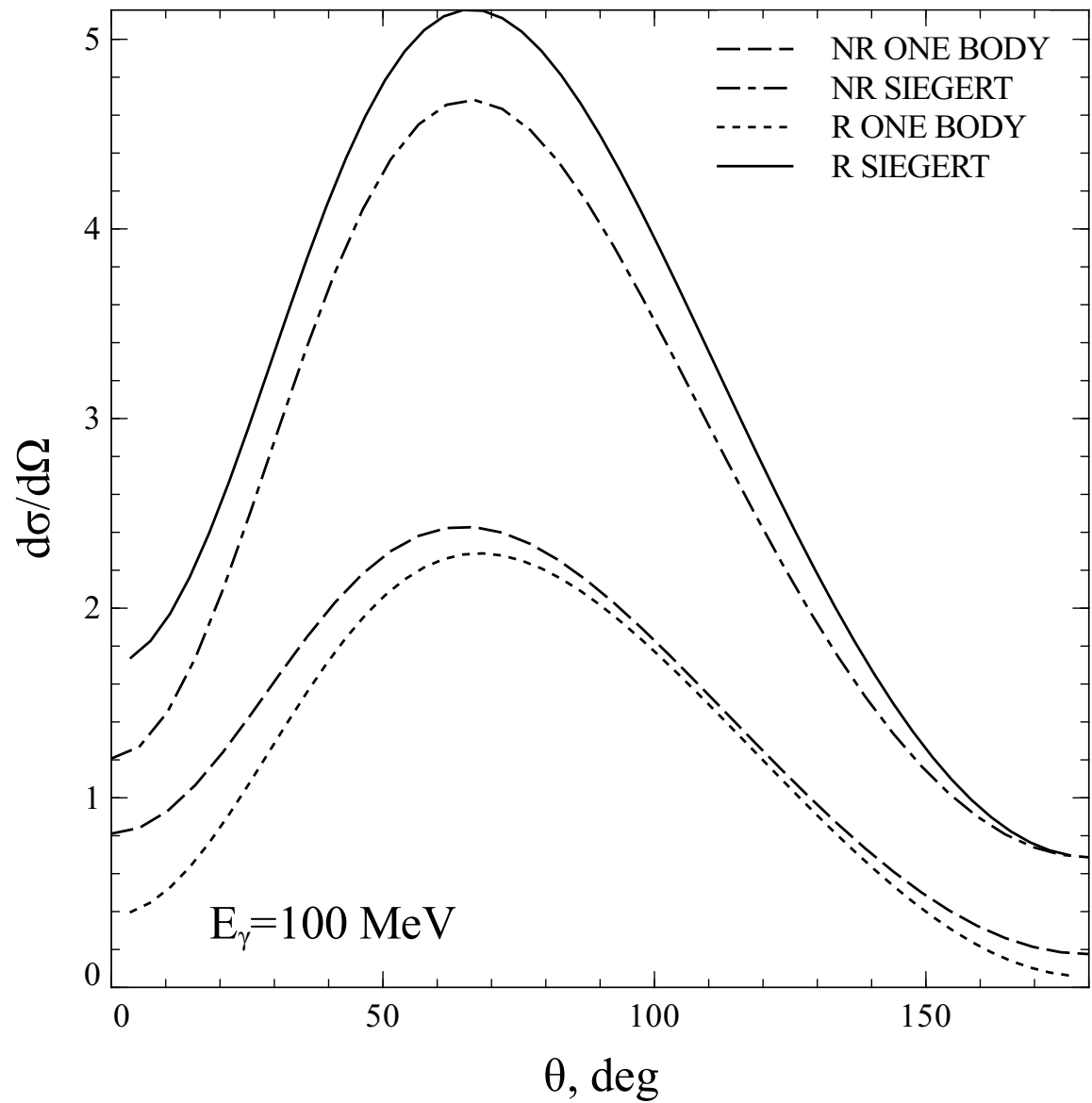
The deuteron BS vertex function $\Gamma_{m_d}(k, K_i)$ calculated by using the Graz II kernel separable kernel.

The γNN electromagnetic vertex is in on-mass-shell form

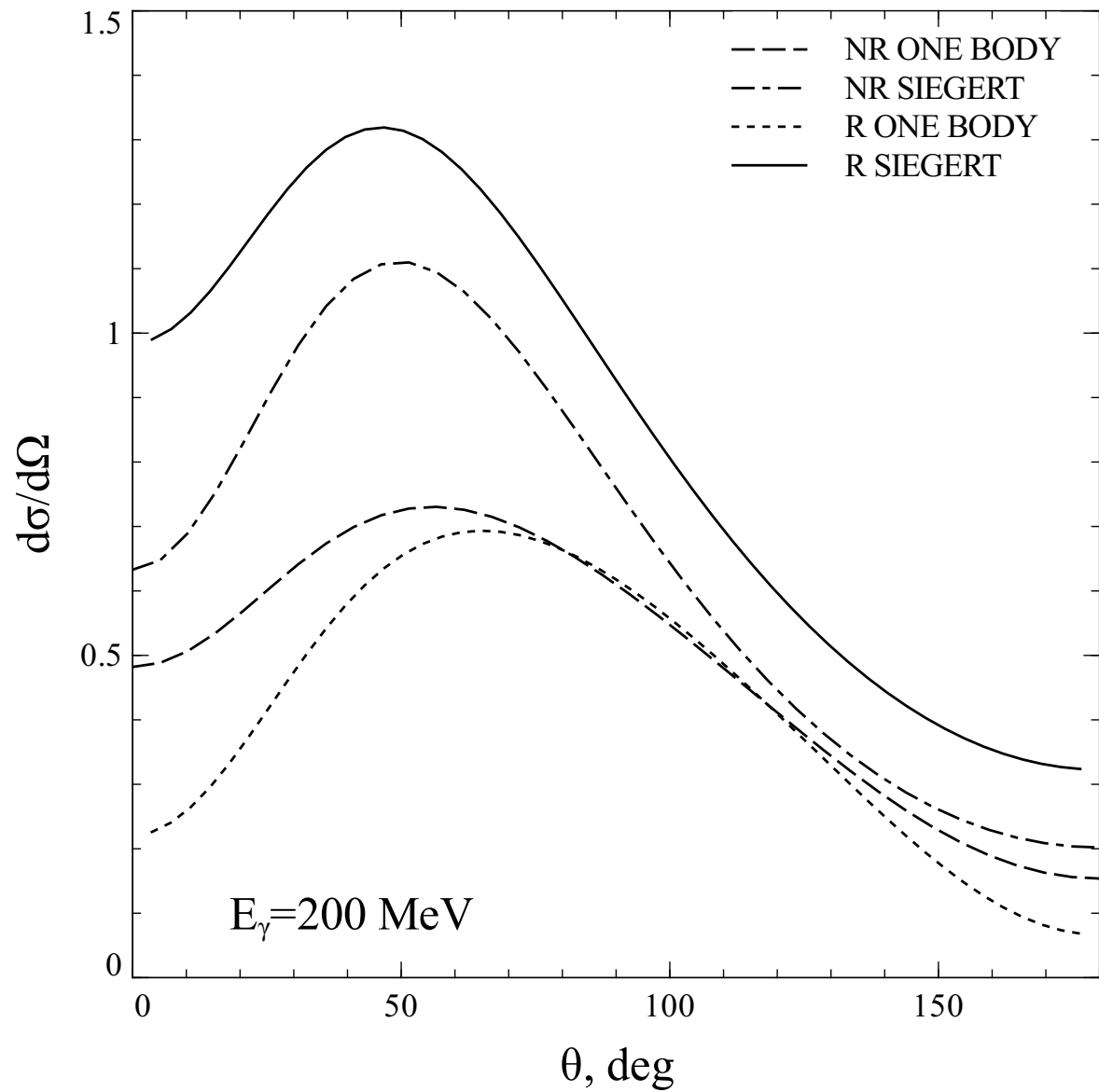
$$\Gamma_{\mu}^{(1,2)} = \gamma_{\mu}^{(1,2)} F_1^{(1,2)} - 1/4m(\gamma_{\mu} \hat{q} - \hat{q} \gamma_{\mu})^{(1,2)} F_2^{(1,2)}.$$



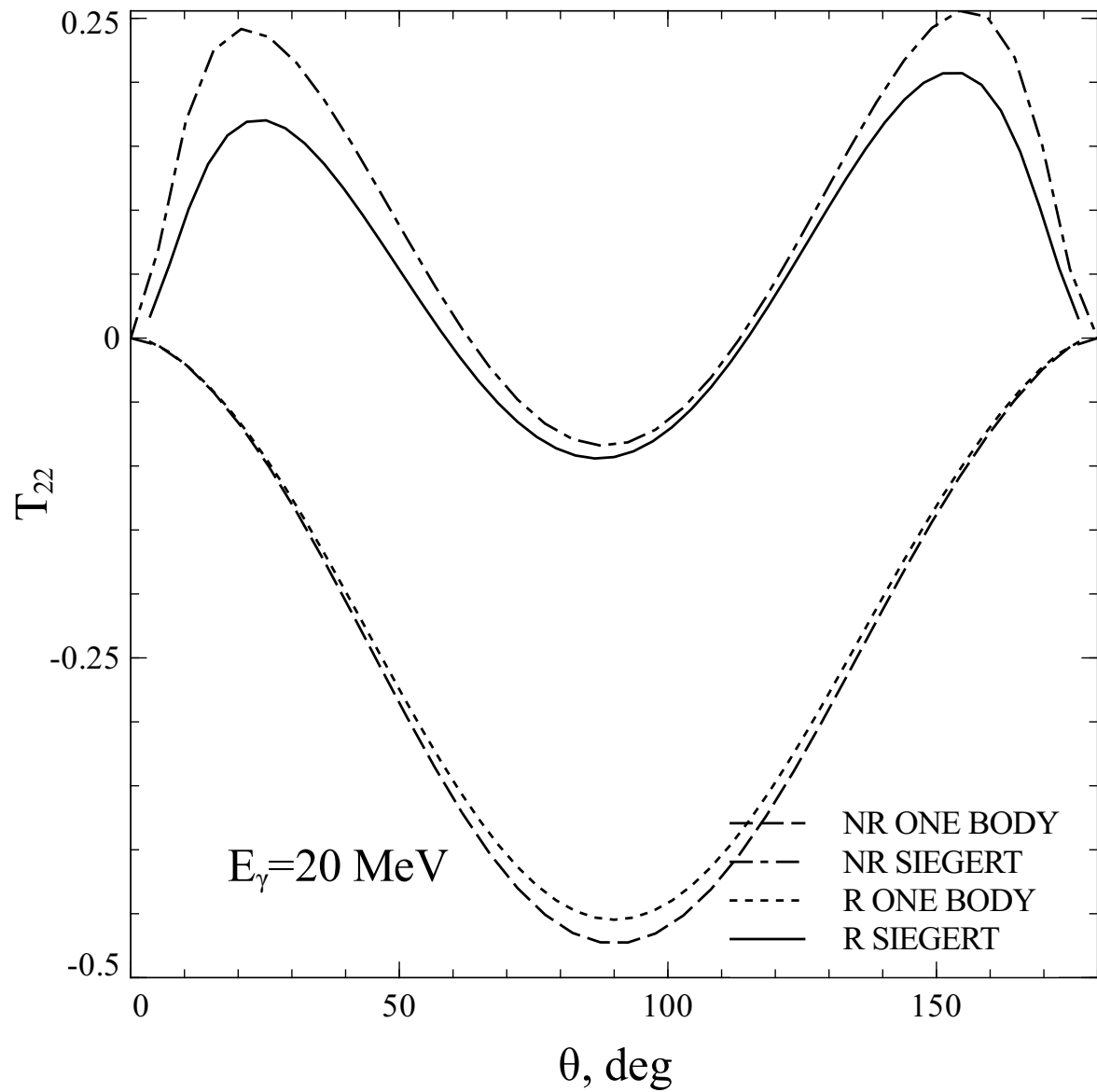
Angular distribution with $E_\gamma = 20 \text{ MeV}$



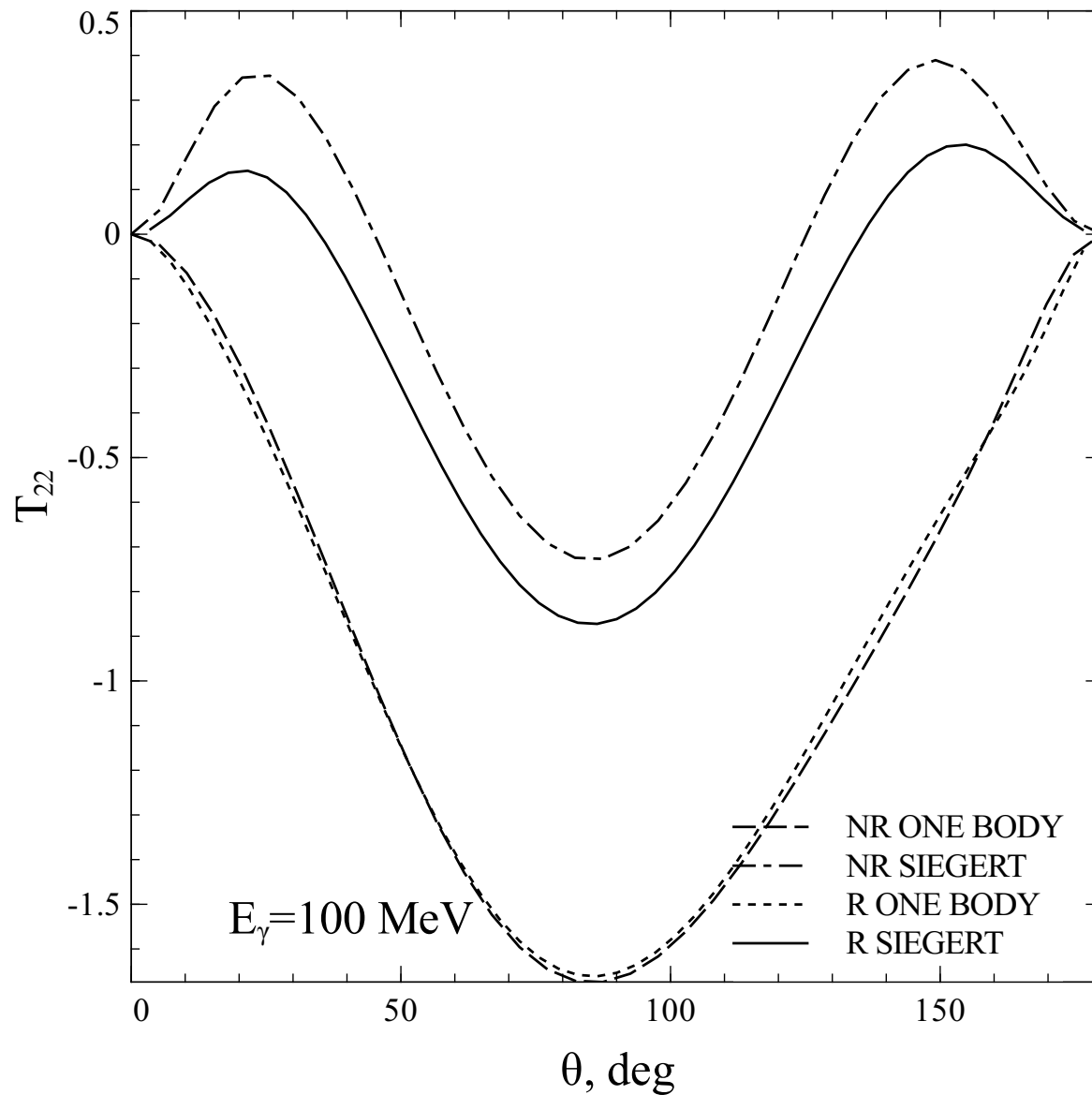
Angular distribution with $E_\gamma = 100$ MeV



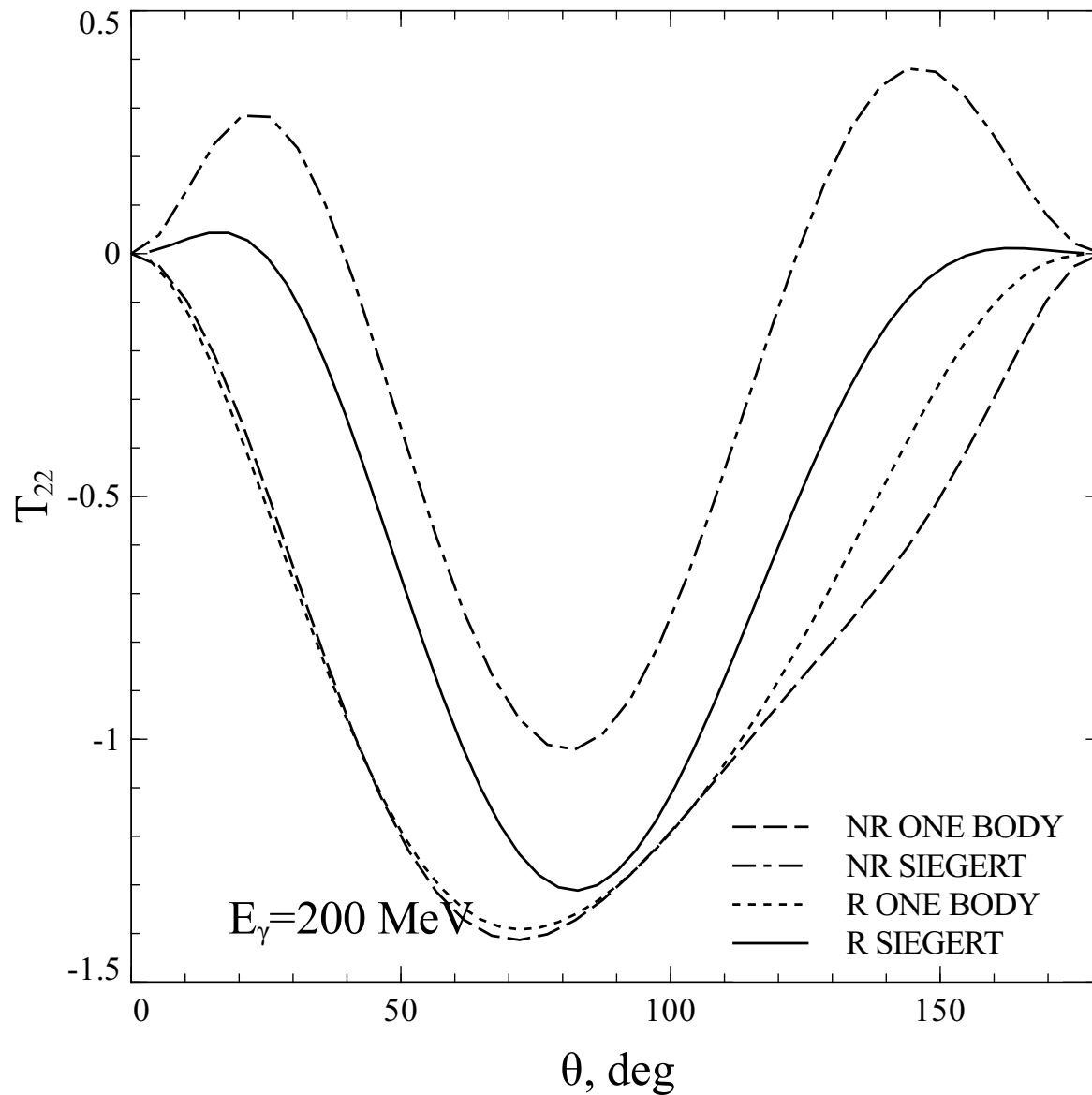
Angular distribution with $E_\gamma = 200$ MeV



Component T_{22} of the deuteron tensor asymmetry with $E_\gamma = 20 \text{ MeV}$



Component T_{22} of the deuteron tensor asymmetry with $E_\gamma = 100$ MeV



Component T_{22} of the deuteron tensor asymmetry with $E_\gamma = 200 \text{ MeV}$

Conclusion:

- effects of the two-particle current are investigated for reaction of the deuteron photodisintegration by applying the extended Siegert theorem;
- the contributions are found to be positive and rather large for the cross section and deuteron tensor asymmetry.