

*ISHEPP XIX
JINR, Dubna*

***Study of Exotic States of Nuclear
Matter using Lobachevsky
Geometry. Separation of Narrow
Resonances. Data Bases of
Experiments with Bubble Chambers***

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30 September 2008



Institute for Advanced Studies: Relativistic Nuclear Physics Research

- Educational programs
- Planning of experiments
- Verification of theoretical models
- Search of exotic states of nuclear matter
- Lobachevsky space
- Grassman and Clifford vector algebras
- Image recognition

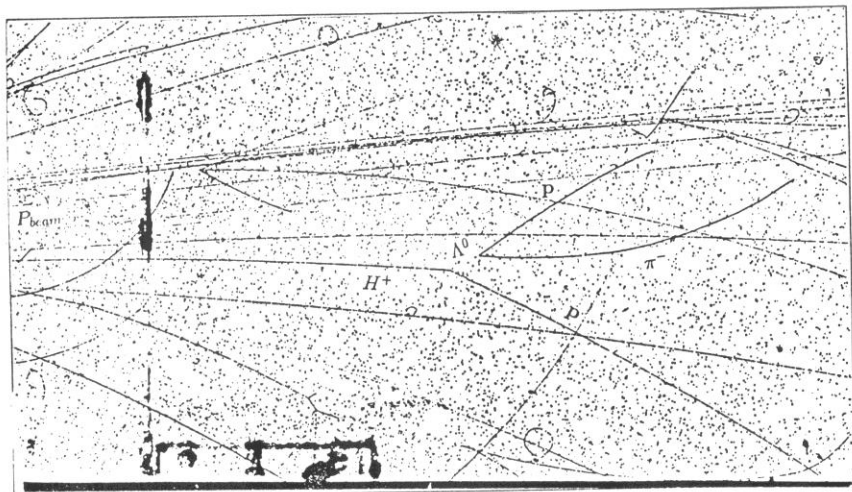


Figure 3: Three-body weak decay of the heavy, stable, positively charged dibaryon fits possible for two hypotheses: $H^+ \rightarrow p + \gamma + \Lambda^0$ and $H^+ \rightarrow p + \pi^0 + \Lambda^0$.

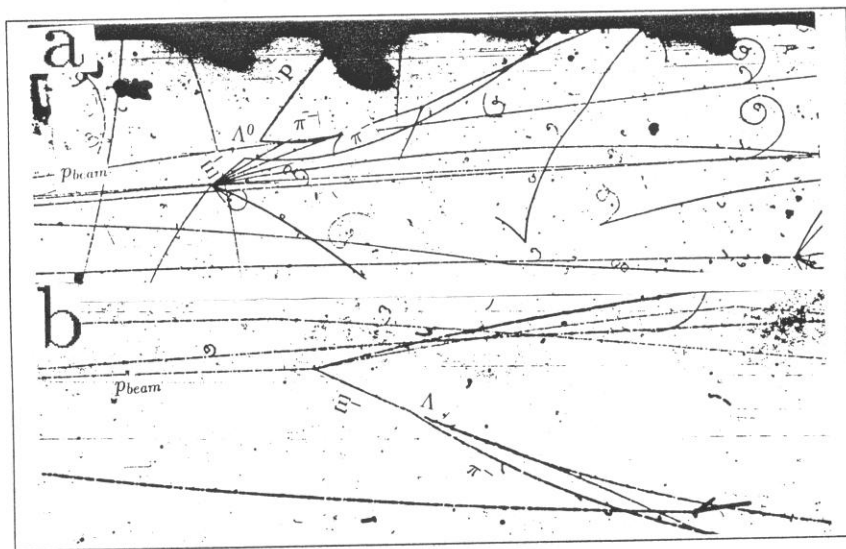
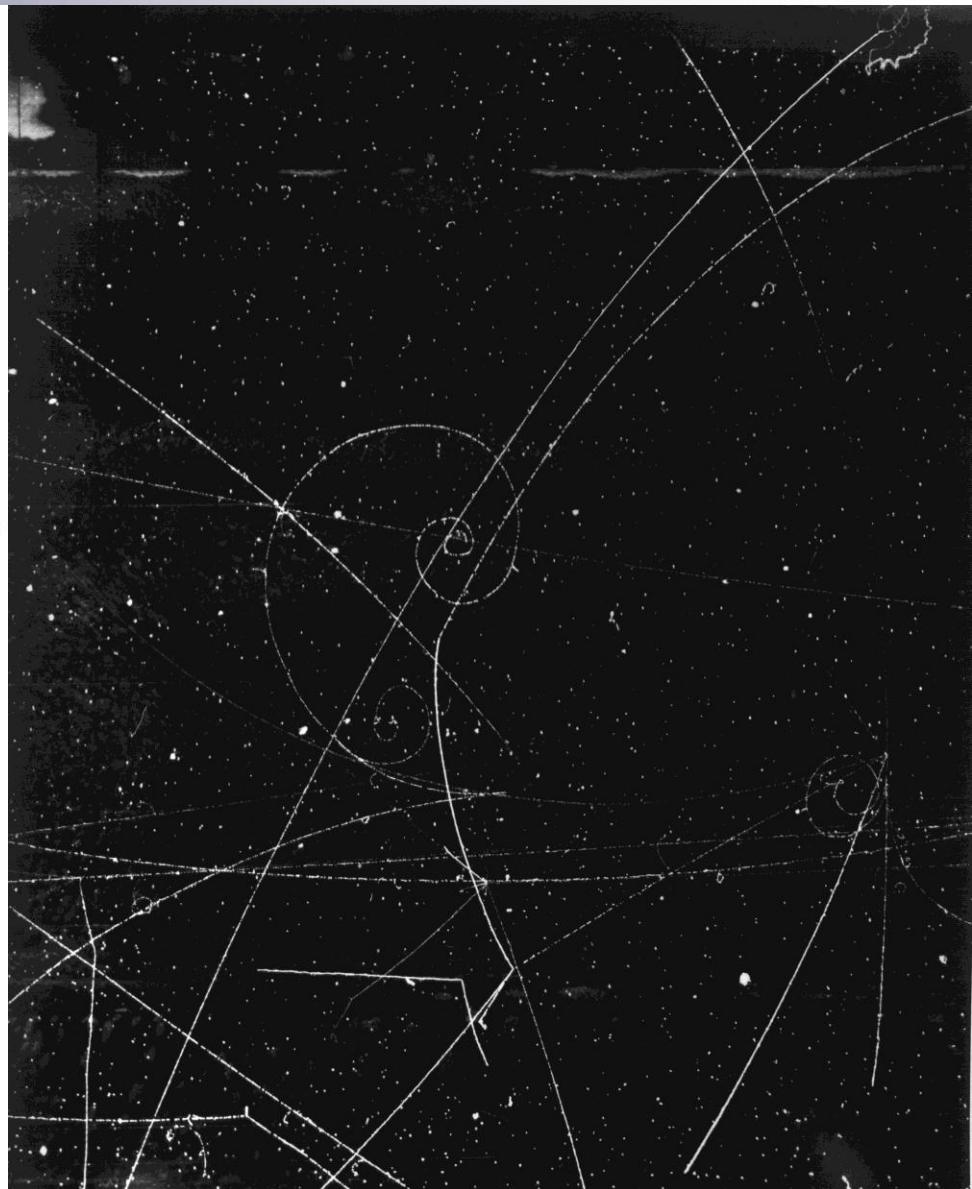
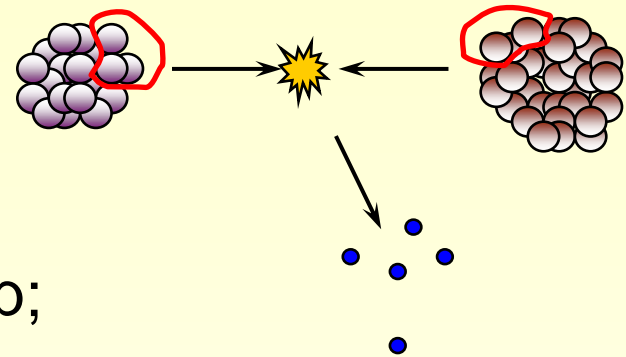


Figure 4: Two body weak decay Ξ^- hyperon $\rightarrow \pi^- + \Lambda$: a) first event; b) second event.



Data Bases of Experiments with Bubble Chambers

- 4.2 GeV p, d, He, C, Ta + CH;
- 4.2 GeV p, C + Ta;
- 10 GeV p + CH;
- 40 GeV π + CH (Protvino);
- 5.2, 3.8, 2.2, 1.7, 1.4 GeV/c n + p;
- 2.2, 1.7, 1.4 GeV/c d + p .



Data obtained at BNL, CERN;
Mirabell

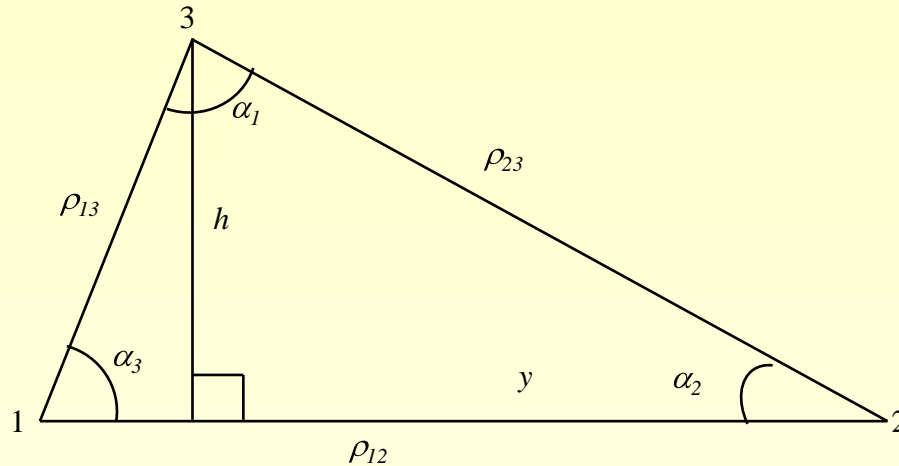


Collaboration

- Kazan State University
- Lobachevsky Institute of Mathematics and Mechanics
- University of Bucharest
- Maritime University of Constanta
- Fock Physics Institute, St. Petersburg State University

- Institute of Nuclear Physics, Moscow State University
- Samara State University
- Perm State University
- CERN

Lobachevsky Space



Longitudinal rapidity

$$y = \frac{1}{2} \ln \frac{E + p_{\parallel}}{E - p_{\parallel}}$$

$$defect = \pi - \alpha_1 - \alpha_2 - \alpha_3$$

Transverse mass

$$m_T = \sqrt{m^2 + p_T^2}$$

$$perimeter = \rho_1 + \rho_2 + \rho_3$$

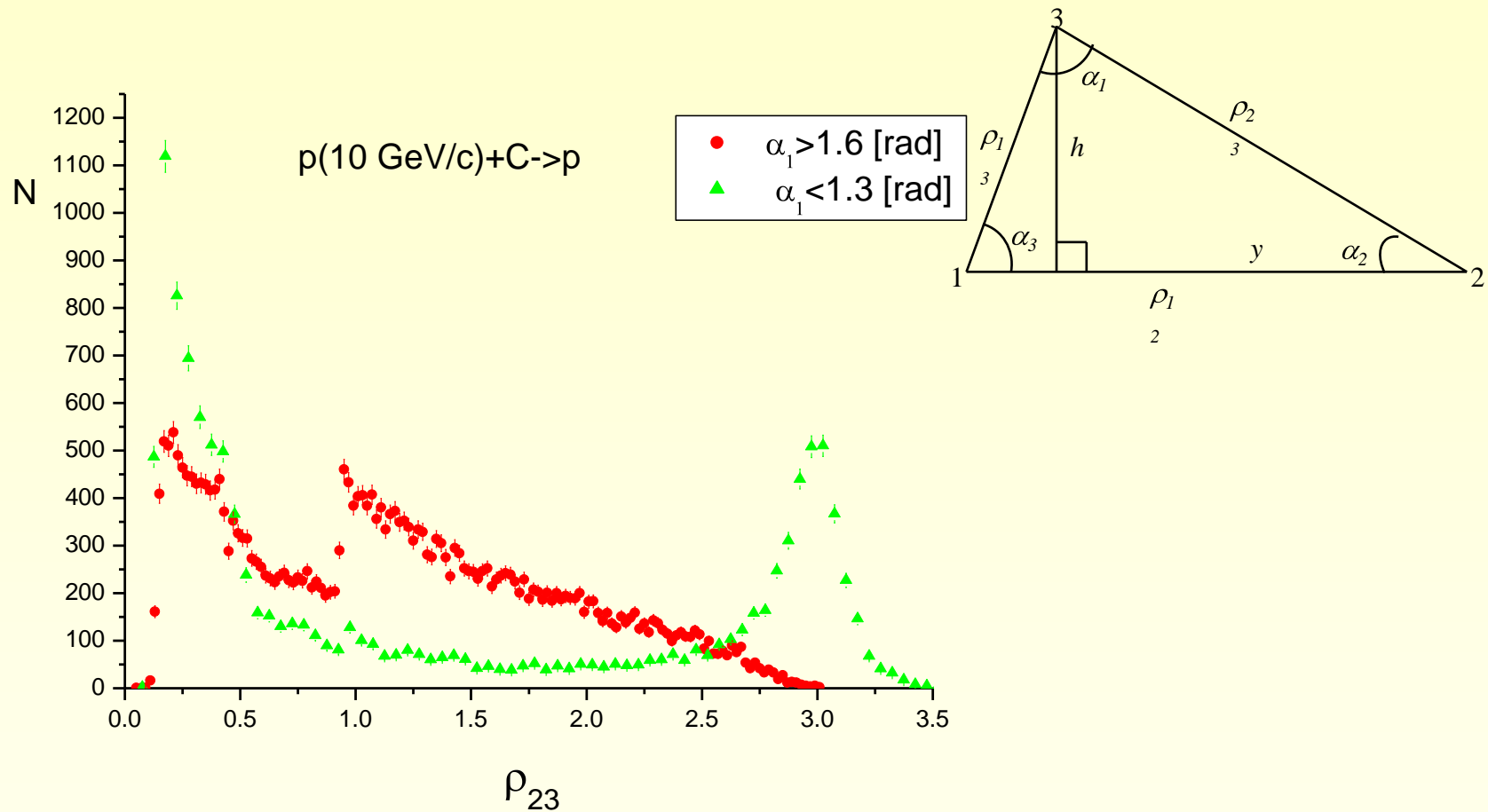
Transverse rapidity

$$\text{ch } h = \frac{m_T}{m}$$

Angle of Parallelism

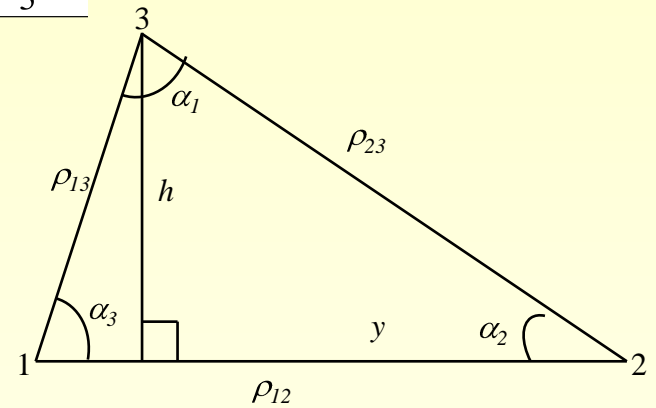
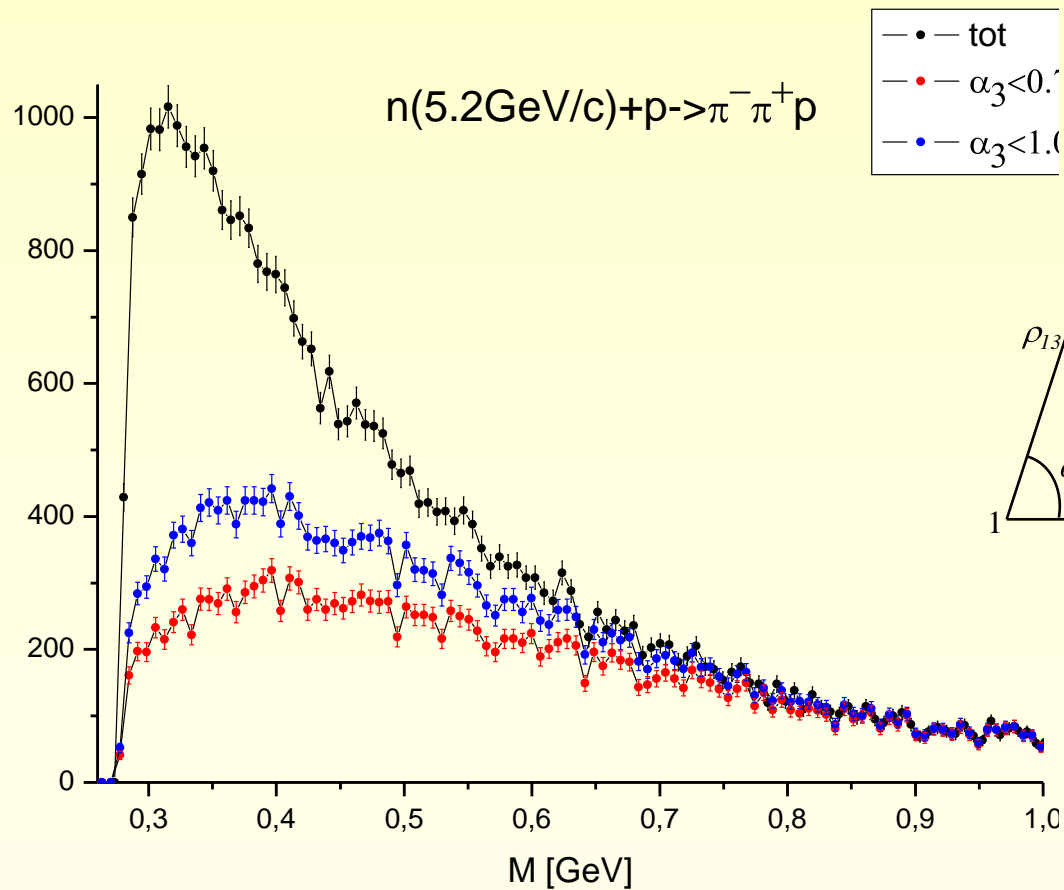
$$\Pi_L(h) = 2 \cdot \arctg \left(e^{-h} \right)$$

Proton distribution for two angular intervals in $p(10\text{GeV}/c)+\text{C}$

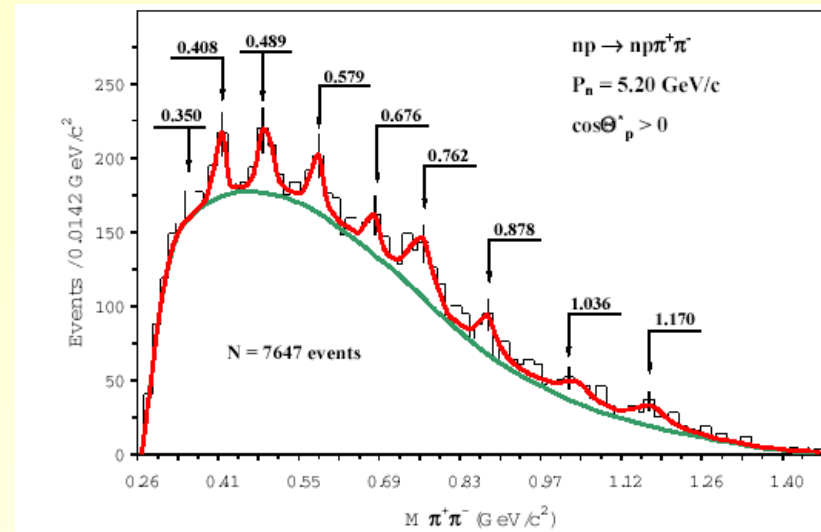
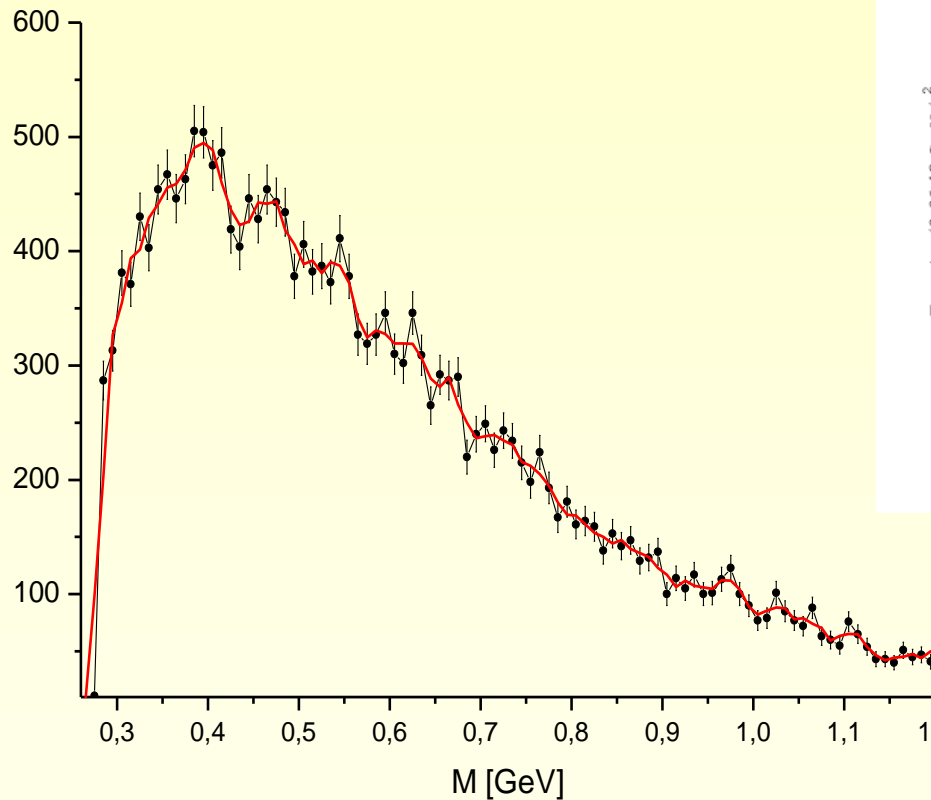


A. A. Baldin, E. G. Baldina, E. N. Kladnitskaya, O. V. Rogachevskii,
Phys.Part.Nucl.Lett., vol. 1, no. 4, 7-16 (2004).

$n+p \rightarrow \pi^- \pi^+ p$ 5GeV



$n+p \rightarrow \pi^-$ 5 GeV



LOW-MASS ($M < 1.2 \text{ GeV}/c^2$) σ_0 - MESON PRODUCED IN THE SYSTEM $\pi^+\pi^-$
 FROM THE REACTION $np \rightarrow np\pi^+\pi^-$ AT $P_n=5.20 \text{ GeV}/c$

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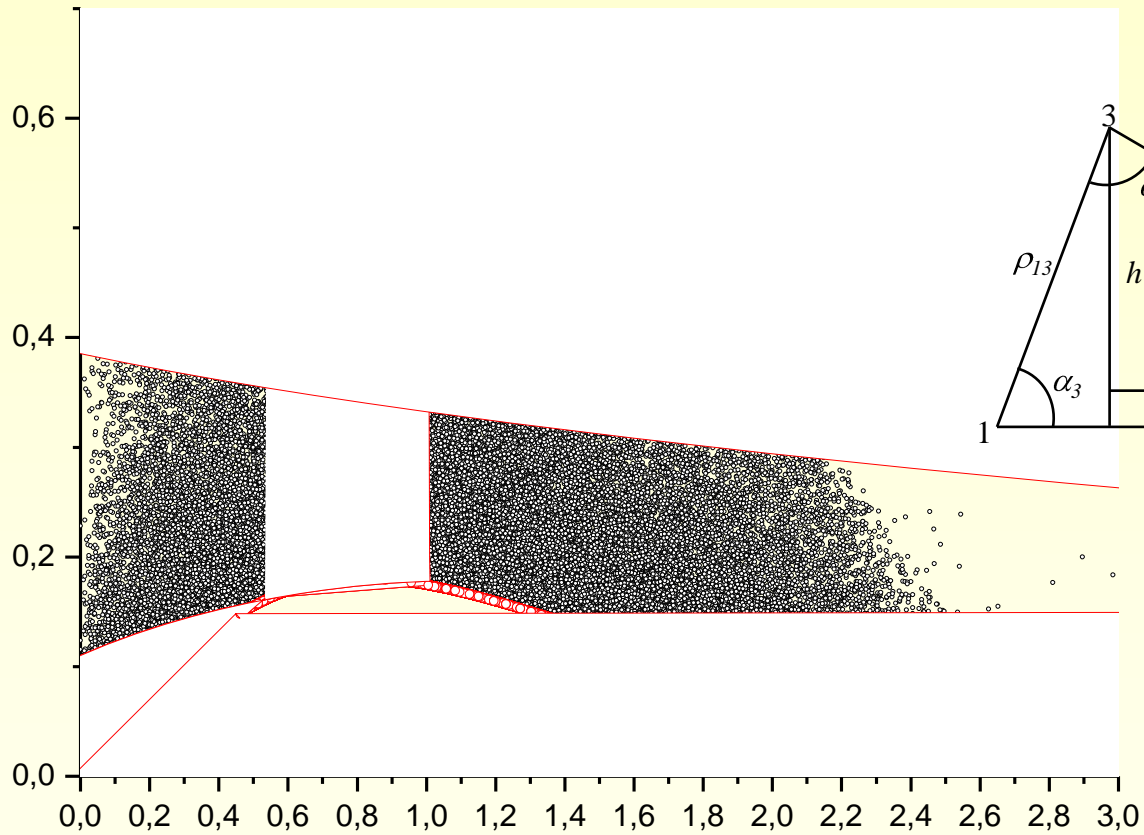
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The investigation has been performed at the Veksler and Baldin Laboratory of High Energies, JINR Dubna, 2006.

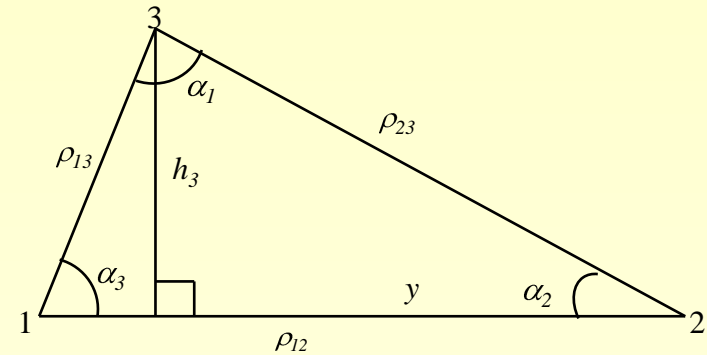
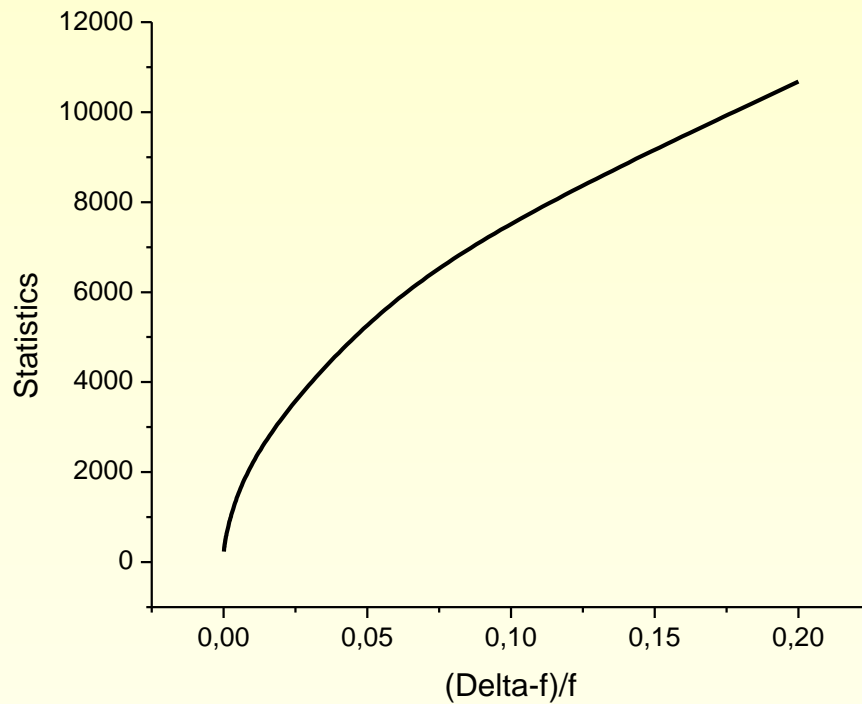
Lobachevsky Space

$n+p \rightarrow \pi^-$ 5GeV



Lobachevsky Space

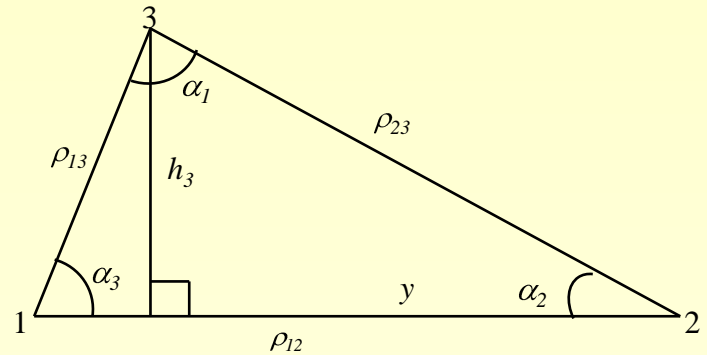
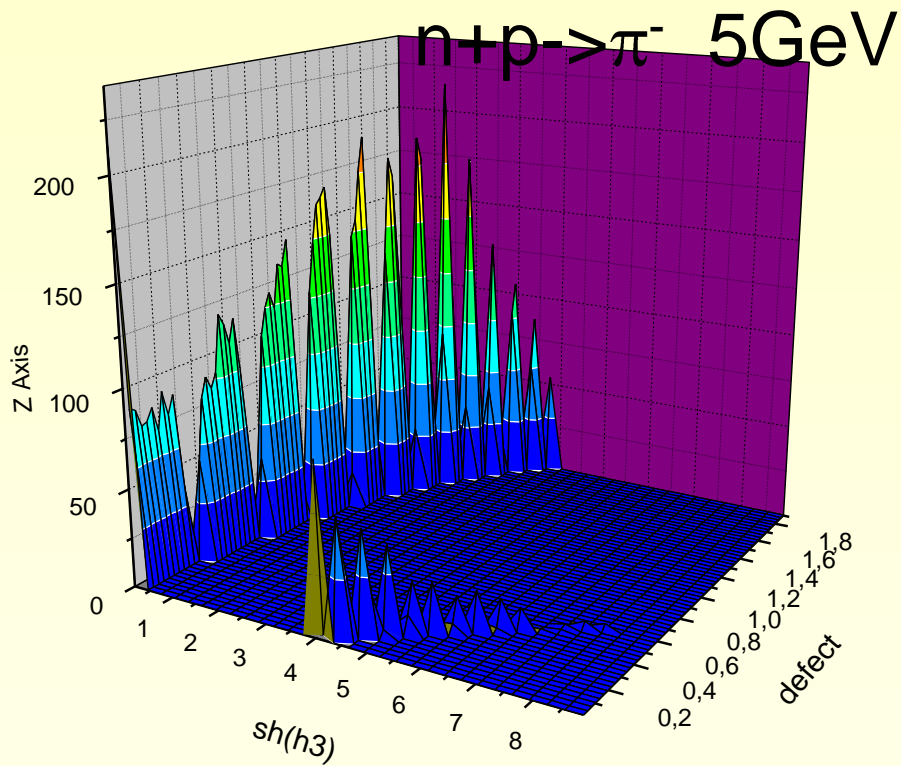
$n+p \rightarrow \pi^-$ 5GeV



$$\Delta_{12}^3 = 2\Pi_L \overset{\curvearrowright}{\curvearrowleft} \alpha_3$$

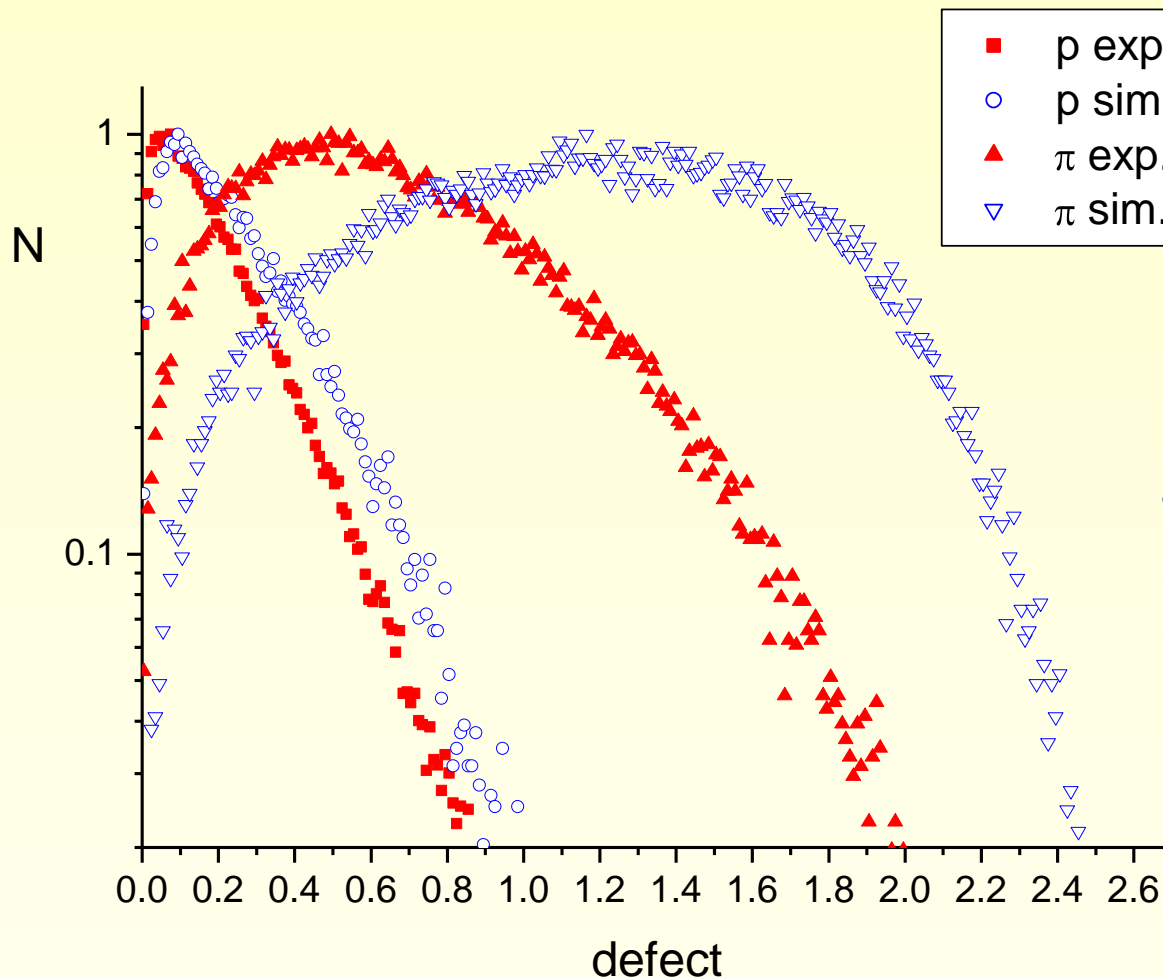
$$f \overset{\curvearrowright}{\curvearrowleft} = 2 \left(\Pi_L \overset{\curvearrowright}{\curvearrowleft} \arctg \frac{th\left(\frac{\rho_1}{2}\right)}{sh \overset{\curvearrowright}{\curvearrowleft}} \right)$$

Lobachevsky Space

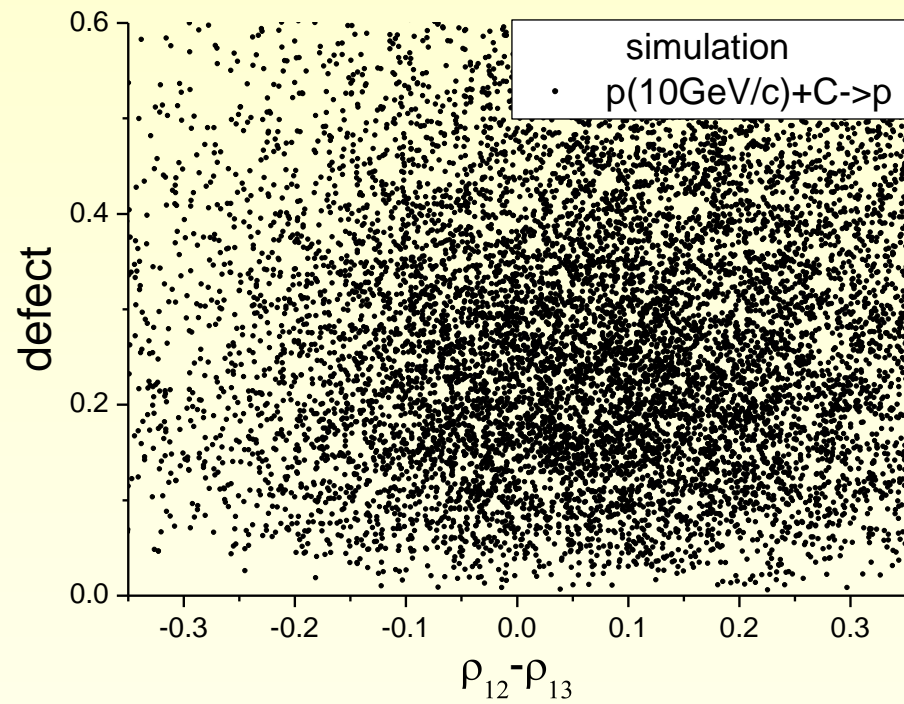
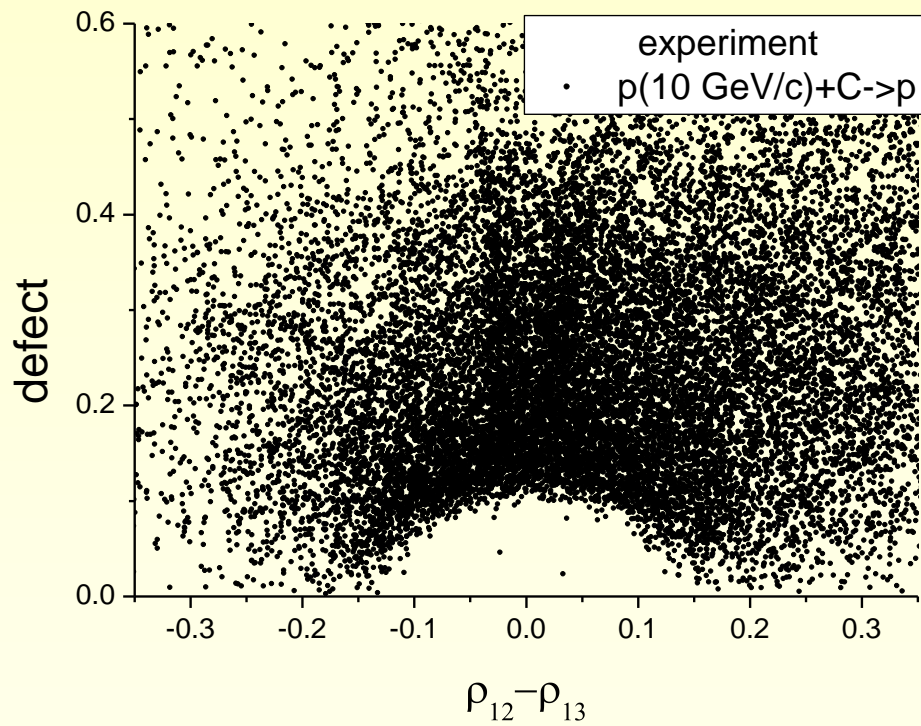


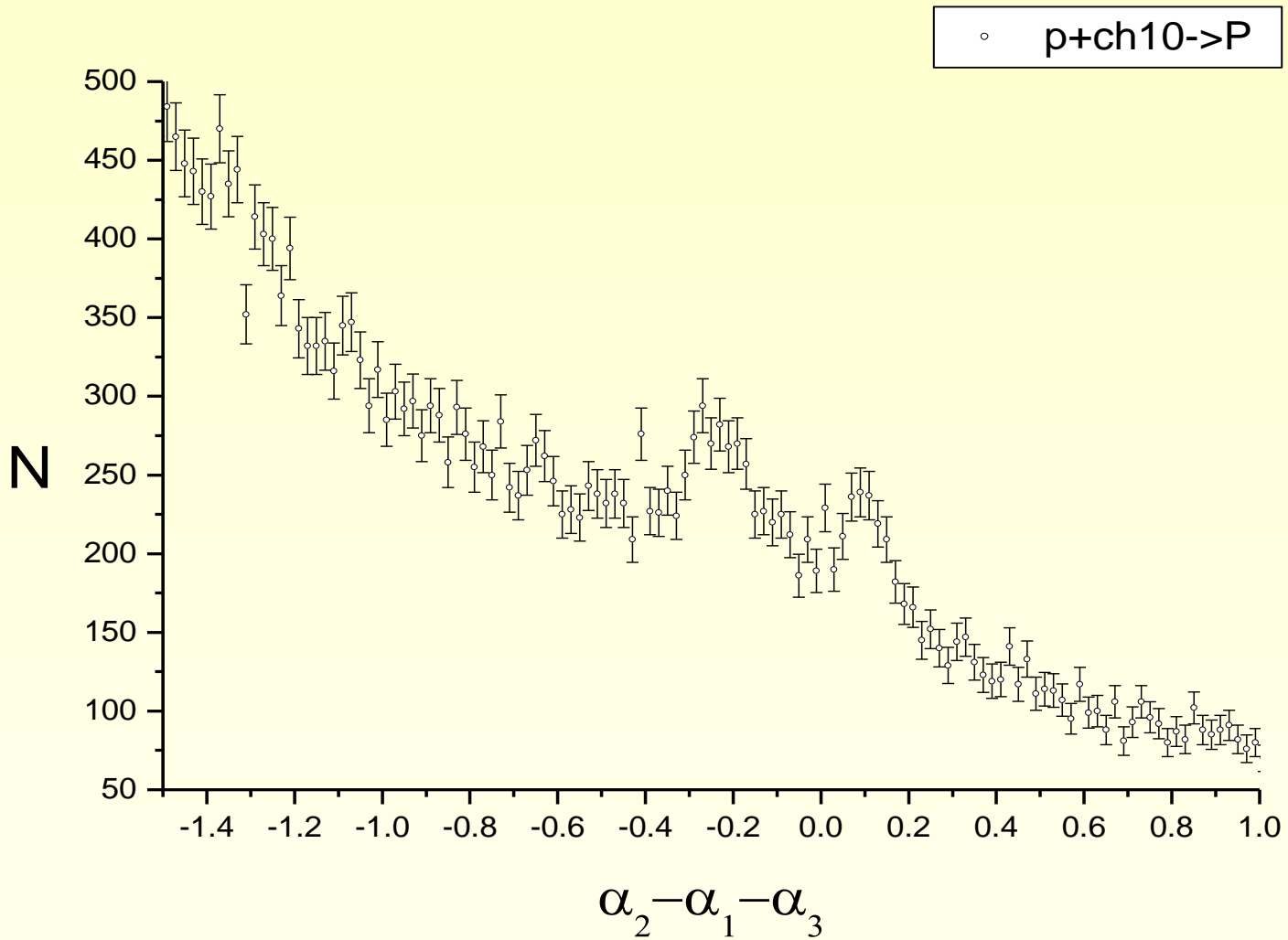
$$defect = \pi - \alpha_1 - \alpha_2 - \alpha_3$$

Normalized distributions of defects of triangles formed by all combinations of protons and all combinations of mesons registered in $p(10\text{GeV}/c)+C$



Note, that the model adequately reproduces inclusive spectra of both protons and π -mesons. The distribution of trios of π -mesons, however, differs noticeably from experimental data.





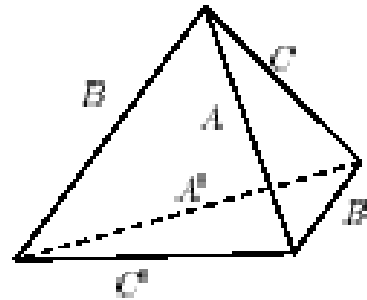
Volumes of tetrahedra

Algebraic & Geometric Topology

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ATG



$$\begin{aligned}
 \alpha_1 &= \exp(i\overline{AB}); & \beta_1 &= \exp(i\overline{BA}) \\
 \alpha_2 &= \exp(i\overline{BC}); & \beta_2 &= \exp(i\overline{CB}) \\
 \alpha_3 &= \exp(i\overline{CD}); & \beta_3 &= \exp(i\overline{DC}) \\
 \alpha_4 &= \exp(i\overline{DA}); & \beta_4 &= \exp(i\overline{AD}),
 \end{aligned} \tag{17}$$

we obtain

$$\begin{aligned}
 0 &= \frac{1}{\alpha_1\alpha_2\alpha_3\alpha_4} - \beta_1\beta_2\beta_3\beta_4 + z^2 \left(-\frac{\alpha_1}{\alpha_2\alpha_3\alpha_4} - \frac{\alpha_2}{\alpha_1\alpha_3\alpha_4} - \frac{\alpha_3}{\alpha_1\alpha_2\alpha_4} - \frac{\alpha_4}{\alpha_1\alpha_2\alpha_3} \right. \\
 &\quad \left. + \frac{\beta_1\beta_2\beta_3}{\beta_4} + \frac{\beta_1\beta_2\beta_4}{\beta_3} + \frac{\beta_1\beta_3\beta_4}{\beta_2} + \frac{\beta_2\beta_3\beta_4}{\beta_1} \right) \\
 &\quad + z^4 \left(\frac{\alpha_1\alpha_2}{\alpha_3\alpha_4} + \frac{\alpha_1\alpha_3}{\alpha_2\alpha_4} + \frac{\alpha_2\alpha_3}{\alpha_1\alpha_4} + \frac{\alpha_1\alpha_4}{\alpha_2\alpha_3} + \frac{\alpha_2\alpha_4}{\alpha_1\alpha_3} + \frac{\alpha_3\alpha_4}{\alpha_1\alpha_2} \right. \\
 &\quad \left. - \frac{\beta_1\beta_2}{\beta_3\beta_4} - \frac{\beta_1\beta_3}{\beta_2\beta_4} - \frac{\beta_2\beta_3}{\beta_1\beta_4} - \frac{\beta_1\beta_4}{\beta_2\beta_3} - \frac{\beta_2\beta_4}{\beta_1\beta_3} - \frac{\beta_3\beta_4}{\beta_1\beta_2} \right) \\
 &\quad + z^6 \left(\frac{\beta_1}{\beta_2\beta_3\beta_4} + \frac{\beta_2}{\beta_1\beta_3\beta_4} + \frac{\beta_3}{\beta_1\beta_2\beta_4} + \frac{\beta_4}{\beta_1\beta_2\beta_3} \right) \\
 &\quad - \frac{\alpha_1\alpha_2\alpha_3}{\alpha_4} - \frac{\alpha_1\alpha_2\alpha_4}{\alpha_3} - \frac{\alpha_1\alpha_3\alpha_4}{\alpha_2} - \frac{\alpha_2\alpha_3\alpha_4}{\alpha_1} + z^8 \left(\alpha_1\alpha_2\alpha_3\alpha_4 - \frac{1}{\beta_1\beta_2\beta_3\beta_4} \right).
 \end{aligned} \tag{18}$$

The Regge symmetry is a scissors congruence in hyperbolic space

YANA MOHANTY

$$\begin{aligned}
 \overline{AB} &= \frac{A + A' + 2B'}{4}; & \overline{BA} &= \frac{2\pi + A - A' + 2C'}{4} \\
 \overline{BC} &= \frac{A + A' - 2B'}{4}; & \overline{CB} &= \frac{2\pi - A + A' - 2C'}{4} \\
 \overline{CD} &= \frac{-A - A' - 2B}{4}; & \overline{DC} &= \frac{2\pi - A + A' + 2C}{4} \\
 \overline{DA} &= \frac{-A - A' + 2B}{4}; & \overline{AD} &= \frac{2\pi + A - A' - 2C'}{4}.
 \end{aligned} \tag{21}$$

$$\begin{aligned}
 (T) &= \mathfrak{Jl}(\overline{AB} + \arg z_-) + \mathfrak{Jl}(\overline{BA} - \arg z_-) + \mathfrak{Jl}(\overline{BC} + \arg z_-) \\
 &\quad + \mathfrak{Jl}(\overline{CB} - \arg z_-) + \mathfrak{Jl}(\overline{CD} + \arg z_-) + \mathfrak{Jl}(\overline{DC} - \arg z_-) \\
 &\quad + \mathfrak{Jl}(\overline{DA} + \arg z_-) + \mathfrak{Jl}(\overline{AD} - \arg z_-) + \frac{1}{2} \left[\mathfrak{Jl}\left(\frac{\pi + A - B - C}{2}\right) \right. \\
 &\quad \left. - \mathfrak{Jl}\left(\frac{\pi + B - A - C}{2}\right) - \mathfrak{Jl}\left(\frac{\pi + C - A - B}{2}\right) + \mathfrak{Jl}\left(\frac{\pi + B' - A' - C}{2}\right) \right. \\
 &\quad \left. + \mathfrak{Jl}\left(\frac{\pi + A + B + C}{2}\right) + \mathfrak{Jl}\left(\frac{\pi + C - A' - B'}{2}\right) + \mathfrak{Jl}\left(\frac{\pi - A' + B' + C}{2}\right) \right. \\
 &\quad \left. - \mathfrak{Jl}\left(\frac{\pi + A' + B' + C}{2}\right) + \mathfrak{Jl}\left(\frac{\pi + A' - B - C'}{2}\right) - \mathfrak{Jl}\left(\frac{\pi + A + B' + C'}{2}\right) \right. \\
 &\quad \left. - \mathfrak{Jl}\left(\frac{\pi + A - B' - C'}{2}\right) + \mathfrak{Jl}\left(\frac{\pi + B' - A - C'}{2}\right) - \mathfrak{Jl}\left(\frac{\pi - A' - B + C'}{2}\right) \right. \\
 &\quad \left. + \mathfrak{Jl}\left(\frac{\pi + A' - B + C'}{2}\right) + \mathfrak{Jl}\left(\frac{\pi + A' + B + C'}{2}\right) + \mathfrak{Jl}\left(\frac{\pi - A - B' + C'}{2}\right) \right],
 \end{aligned} \tag{23}$$

where the quantities with bars are given by (21), and z_- is the solution of the quadratic equation (18) with the negative square root.